

Simon, Newell.

$$P \rightarrow q \quad \stackrel{=D}{\uparrow} \quad \neg P \vee q \quad \text{Page 232.}$$

$\rightarrow$  implies  
 $\neg$  not  
 $\vee$  or  
 $P, q, r, s$  } propositions.

dot convention,  
rules

1. Substitution

2.

$a \rightarrow b$  ... ~~means~~

if  $a$  <sup>is a prop.</sup> then  $b$  is a prop.

3. ~~(replacement)~~ (of a symbol by its def.)

2)  $a \rightarrow b$  means if  $a$  is a valid prop., then  $b$  is. (detachment) [not used at first]

3) replacement of a symbol by its definition. ~~is used much at first~~

$\vdash$  means that a prop. is being asserted (Russel)

! will be used here instead of  $\vdash$ .

1.2  $(P \vee p) \rightarrow p$  Axiom.

$$(\neg p \vee \neg p) \rightarrow \neg p$$

$$(P \rightarrow \neg p) \rightarrow \neg p$$

1) Find "similar" theorems. (Page 29)

2) Match them. (?)

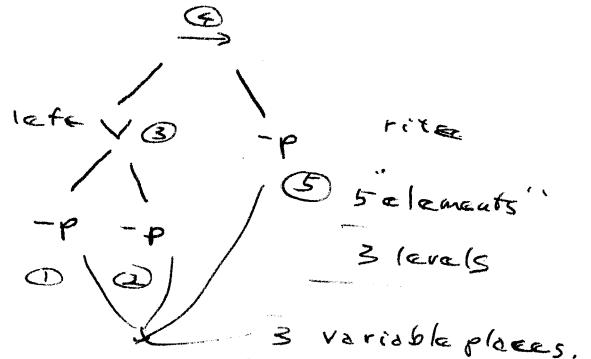
Page

$$(P \vee p) \rightarrow p =$$

$$\begin{aligned} K &= \text{no. levels.} & 3 \\ J &= \text{no. names.} & 1 \\ H &= \text{variable places.} & 3 \end{aligned}$$

tree notation  $\Rightarrow$

1 name.



description is  $\frac{K J H}{B_1 B}$ .

try to prove

$$(P \Rightarrow \neg P) \Rightarrow \neg P$$

A (~~rep~~) means subs. has not been made.

$$\begin{array}{c} A \vee \neg A \\ \hline (\neg B \vee -B) \Rightarrow B \end{array}$$

$$(A \vee \neg A) \Rightarrow A$$

$$(\neg B \vee -B) \Rightarrow -B$$

$$(B \Rightarrow \neg B) \Rightarrow \neg B$$

$$\therefore P \Rightarrow \neg P \Rightarrow \neg P$$

Page 38

2.06

QV  ~~$(P \Rightarrow q) \wedge ((q \Rightarrow r) \wedge (P \Rightarrow r))$~~

?  ~~$(P \Rightarrow q) \rightarrow ((q \Rightarrow r) \wedge (P \Rightarrow r))$~~

Detachment

using 6  $\frac{a}{a \Rightarrow b} (a \Rightarrow b) \rightarrow b$ .

"Similarity" means only triple R./not descriptions are identical.

Machines would not consider

$$a \Rightarrow (b \Rightarrow a)$$

and  $(P \Rightarrow q) \rightarrow (b \Rightarrow (P \Rightarrow q))$

using detachment:

to prove

b

, try to find a  $P \Rightarrow q$

$$a \Rightarrow q \sim b$$

then from to  $c \Rightarrow b$  and try to

prove c.

use around page 40

1.2  
① look for theorems with n descriptions  
then try substitutions. (3):  
will prove many of the theorems  
in chapter 2 of Principia (about  $\frac{1}{3}$ ).

(1.3)

1. substitution method

2. Detachment "~~≡~~" P 350, 393. ~~By~~ Chaining method. ~~Right~~  
to prove  $a \rightarrow c$   
prove  $a \rightarrow b$  and  $b \rightarrow c$ 

Once can work from both ends.

Lattice Theo.	$\nabla$	$\cap$	$\cup$		$\leq$	$\geq$	$=$	$\top$	hull	univ. classe.
Set algeb.	-	$\cap$	$\cup$							
Intuitiv.	$\sim$	$\wedge$	$\vee$							
Prop. Calc.	$\neg$	$\&$	$\Rightarrow$	$\Leftrightarrow$	$\vdash$	$\vdash$	$\vdash$	$\vdash$		
Synt. calc's	$\nabla$	.	$\delta$	$\Rightarrow$	$\Leftrightarrow$	$\vdash$	$\vdash$	$\vdash$	$\vdash$	$\vdash$

\* p # q

means we haven't yet proved  $p \vdash q$

no. of stars before a prop. indicates no. of assumptions it uses.

Fine branching. branching by simple process.

*	a			
*	*	b		
*	*	*	c	
*	*	*	x	↓

1. Substitution of any valid expression

2. Deletion ( omitting intermediate steps )

e.g. if  $A \supset B \supset C \supset D$

Then  $A \supset D$ .

Some starting points:

\* p  $\wedge$  q

\* p

\* p  $\wedge$  q

\* q

\* \*

\* \* p

\* \* q

\* \* p  $\vdash$  q ← indip of q.

Quine  
Fitch  
Cope

proposed this  
method in 1952  
(?)

\* \* \* p

p  $\vdash$  q

\* \* q

To prove

$$(P \wedge q) \vdash (q \wedge P)$$

$\vdash$  suggest to look at  $P \wedge q$  (because  $\vdash$  is a main connective)  
 Assume  $P \wedge q$

Then

$$\ast P \wedge q$$

$$\ast P$$

$$\ast P \wedge q$$

$$\ast q$$

$$\ast P$$

$$\ast q \wedge P$$

~~\* P~~

$$\ast (P \wedge q) \vdash (q \wedge P)$$

Then deletion:

Also work backwards

This connects with

$$\begin{array}{c} \uparrow \\ \ast q \\ \uparrow \\ \ast P \\ \ast q \wedge P \\ (P \wedge q) \vdash (q \wedge P) \end{array}$$

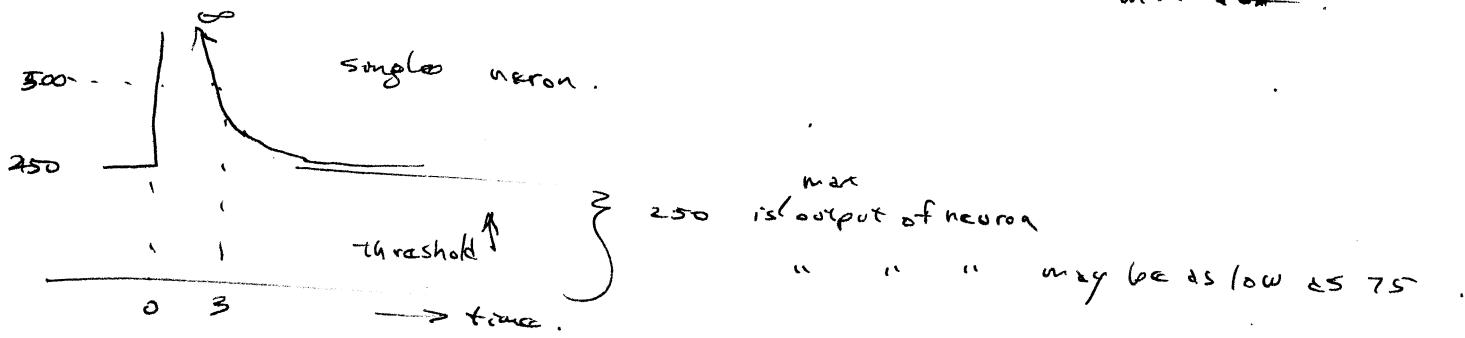
$$\begin{array}{c} \ast P \wedge q \\ \ast P \\ \ast P \wedge q \\ \ast q \end{array}$$

Simon, Newall.

- Subs. method
- 1) Str. first, most imp. metric.
  - 2) If not matching connectives, try  $A \rightarrow \neg A$
  - 3) ... " " try subs. & definitions for ~~some~~ <sup>non-matching</sup> connectives

N. Rochester:

Attempt to check Habb's model of neural behavior with ~~real~~.



Each neuron ~~stim.~~ 10 others (completely random).

6 by cur. 63 zero interval.

Axon  
many efferents

each neuron has many output levels - 1, for each neuron.

it syns. upon.

$\sum$  output<sup>from A to B</sup> / every time A synapses B. Every once in a while the  $\sum$  output are reduced to some fixed level by subtraction of some small amt. from each

1) state of recovery  
2) .. " fatigue

2 nos.

rel.  
size of 1st is time  
of 1st is time

Fatigue state is added to threshold.

thresh ↑ & every firing

but uppercut

↓ b " at not firing. lower inputs.

Habb wanted to account for

D Lashley's results on brain exterpation.

~ 10K neurons in a "cell assembly". Arrousal of "cell assembly" is used for short-time memory. Cell assemblies are not physically localized.

inputs:

25%

12%

12%

50% random.

Model is for discrimination % abstraction

When A fires B many times A tends to fire B more easily

- trys of ~~different~~ not perturbed slightly,  
— nets diverged from original rapidly.

Conclusion was that the net would need more non-random structures if it was to exhibit cell-assembly.

### Second Model for

John Holland, with Hebb.

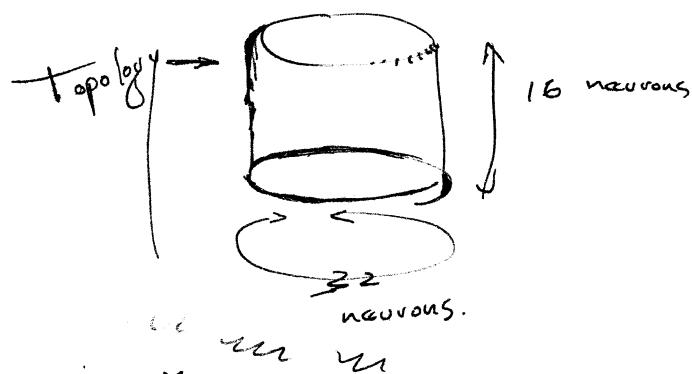


both excitatory, inhibitory stems: internal self-activity of cell  
excitatory. Betw. cells — inhibitory.

Output was betw. -1, +1. with  $\sim 30$  steps.

512 neurons used. Each neuron has a frequency of firing assoc. with it.  
Also distance bias put in.

Random connections except within distance of 8.



4 areas chosen to act as receptors.

connections ~~were~~ become excitatory  
when  $\pi$  cross corr.  $\pi > 1$

inhibit when " " "~~cross corr.~~"  $\pi < 1$ .

There was development of localized, connected ~~regions~~ regions.  
~~that~~ groups had 50-75 neurons in them.

~~REVIEW~~  
~~QUESTION~~  
~~ANSWER~~

McCarthy

2. ~~parameters~~ constants.

$X_i$  vars.

L. Labels. (predicates)

→ implication

wff. = well formed formula  $A_1 \rightarrow A_2 \rightarrow A_3$

where  $A_i$ 's are strings without arrows.

Axioms : Some set of wff's.

Rules of inference.

1) Detachment

$\Delta$

$A \rightarrow X$

gives  $X$

$A$  is / <sup>always</sup> string that doesn't involve  $\rightarrow$

$X$  " " " may " "

2) Substitution : any string in  $\Delta$ .  $A$ 's may be sub.

for any  $\Delta$   $X$

Assume

("words")

only

Let  $S(L_i)$  be  $\Delta$ . set of wff's in  $L_i$ .  $i \in L_i$  is a theorem.

Metatheorem: If. set of theorems in any logical lang. is  $S(L_i)$  for some  $L_i$  among formal systems.

Problems: Trig. identities.

McC wants machine to keep record of trials that were used and score kept — this will govern order of trials.

Then, I think he wants to go to hyper and hyper order computers; each level writes trial programs for the next lower level; derives usefulness of each hierarchical program on the basis of experience. This gives machine that will improve itself.

Smolyan  
Formal System

- 1) how to perform induction
  - 2) Th. min. machine and info packing approach
  - 3) How ~~solve~~ solve.
- Solu. to the induction prob. gives solu. to search problem
- a) by suitable stat. q's.
  - b) by using some of Th. abs's. of induction for search.
- 4) A M.C. method of realization.
  - 5) Way to divide induction problem into 2 parts. — a) Abs. construction
  - b) B.G.

There seems to be big - hassle about ~~whether~~ terminology of "programs" at various levels.

McC is much interested in the Smolyan system because it can refer to itself - presumably so that the lower order machines can be used to improve the higher.

One idea of method of proof is, say in group theory -  
suggested finite to try sub-theorems on a specific group.

1) try to find methods to improve proof search procedures.

~~Note~~ i.e. Make machine's task to improve own programs to improve own programs ...

It must also have some other task. -

McC believes it should be the Smolyan formal systems, because they are simple, but yet very general. This is ~~is~~ very improbable, since all the info. the machine could possibly gain, would be info about these Smolyan formal systems. It is improbable that such rules about program improvement would be useful in, say, solving ~~first~~ logic

Trig. identities.

McC mentions methods of deciding upon subgoals.

~~...of Minsky~~

Samuels' checkers player: IBM 704 - uses all 36 bits of each word - plays all sequences & moves out. Evaluates moves for best evaluation on ~~end~~ end of 5 moves.

~~def.~~ <sup>defn.</sup> Def. of knowledge

Defs. of info: how intuitive idea is simply close as to what might be useful. - That "true" def. is dependent upon usefulness in some situation.

M's Goal: to define self-awareness and see how much a machine can gain by introspection.

Actually what he is saying:

1) Psych. Theories and Physics Theories are much different in content, method. This is because Psych is more complex - in the sense that ~~observable behavior~~ macro behavior in physics is not distant from micro behavior. One can easily combine atomic laws to get <sup>reasonably reliable</sup> macro laws. In psych, however, animal behavior is a very complex ~~is~~ function of atomic behavior. So one makes semi-macro behavior entities in Psychology. These entities, like "Id, ego, reinforcement" are entirely different in their laws of combination, from yours.

2) It is reasonable that man should ~~not~~ consider mind & behavior as essentially different, and since they have entirely different kinds of theories for their behavior.

3) This "dualist" state should exist until science advances to the point where ~~it~~ <sup>will</sup> bridge betw. Human behavior and atomic behavior is made. At this point, scientists should become monists. Until then, they may be monists by faith - i.e. they may think that ~~material~~ materialism is likely, but they have not yet proved it.

## + Selfridge

says he is interested in the learning process. While his general statements are good, his specific statements and projects don't seem to be very good. Realizes that pattern learning in itself is not imp., but methods of learning is.

 This was also true of his west coast comp. conf. paper.

Tsots Rask

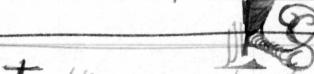
- 1) T.R. ~~Blank~~ (Blank sheet of paper)

- 2) R.M. Reasonable machine (Game player)

(a) Lays: about world.

 S. mentioned desire to build a T.M. before "others" did; since he trusts himself and not "them".

Imp. words used in project by many  
 "Metric"  
 "Sub Goal"



Talks about what sentences are close to given sentence.

1) tries substitution of n words for other words.

2) " " " " phrases " " " " phrases

What is a reasonable lays. for a game?

Consider 5-in-a-row

[Rouse Ball] says 1<sup>st</sup> player can always win, ~~but not with~~  
 Math. rec.  
 [also Kratchar]

4-in-a-row  is a useful word.

3 " " " " " " "

Also it is bad to let him get (5 in a row)  
 (4 " " " )

S. feels that deductive logic is rather useless.

Substitution

Substitution

Database

Database

Chaining

Probably chaining

Mars and N.

Mars : Intends to extend to further,

hyperlogical operations.

Some ~~basic~~ basic philosophical orientations.

1) Randomness is unimp. except as simple programming method (sometimes),

2) Math. logic is unimp. ~~except~~ except as an inversion problem,

3) For intelligent behavior either

a) Universe must be special to fit machine

b) or machine must be gen. info about universe.

This suggests that McC's machine that was brought up systems is unlikely to do well in other fields. — unless by coincidence —

4) Canonical methods



a) Factoring. ( $\rightarrow$  (str., ntpsts))

b) Evaluation of factors.

c) Inverses as a method to get str., ntpsts

d) Some str., ntpsts. to start with.

I.e. physical world is not w  
to logic.

5) Occam's Razor — just how it is tautological — the idea of simplicity [look at old lecture notes]

6) Idea of working on many / problems likely, to find out what they have in common, rather than initial intense work on any / problem. Emphasize how human works problem, rather than any easy trick ways to work problem that may be peculiar to that sort of problems. This has been (for my own orientation) a great overemphasis of specific problems peculiar difficulties peculiar to Th. prob. worked on rather than prob. diff. peculiar to all probs.

7) Recent approach via evolution and non-redundant coding  
How this evolved into Neural net approach.

8)

Some specific Machines.

a) Th. hyperorder recent. Machine from "Notes on H",

b) Th. Math. machine.

c) Th. evolutionary Machine

d) " elev. of Th. random not machine."

neural nets  
non-redundant  
coding  
for evolution  
T.M.

Th. recent.  
Machine  
by  
"Notes  
on Mmach"

Method  
of eval.  
of efficacy  
of prediction.

Solu. of  
B.G.

{  
Blindly  
General?

## Organization

### 1) Gen. Phil. orientation

a) Randomness unimp. - is artifact ~~assoc.~~ assoc. with my unconscious search procedure

b) Computer must have info on world built in <sup>much</sup> <sub>in general</sub>

→ how  
this  
applies  
to  
info,  
learning  
thinking

c) Emphasis on learning <sup>1. Meaton (Samuels)</sup> rather than peculiarities of individual problems. <sup>2. [ ]</sup>

d) Math logic isn't too imp.

e) Use of definitions - ~~rigerorization of intuitive def.~~ as <sup>rigerorization of intuitive def.</sup> as good approx. for useful sc. object

Ockham's Razor  
into search  
for good  
trials

2) Some learning problems Problem of 1<sup>st</sup> or 2<sup>nd</sup> kind. ← Good Thinking

a) the search problem (how to get quick solns)

b) ~~[ ]~~ Time series prediction

① Continuous

② Double digital.

Chess, other games.

## M.C. Methods



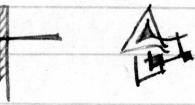
3)

## What is Learning? ~~+~~

a) Use problem of 2<sup>nd</sup> kind as example.

b) Division into problem of ① Expected & of a

etc. etc. try ② Experimental problem.



What are prob. of interest?

1) Search prob. of 1<sup>st</sup> kind.

2) " " " 2<sup>nd</sup> kind. (optimization)

3) Prediction : Time series [or multi-dim]

a) continuous

b) semi continuous

c) ~~double~~ doublely digital.

4) Evolution : as <sup>sort of</sup> problem of 2<sup>nd</sup> kind.

Go into self-reprod. machines and ~~"low-redundance"~~ "codrus".

A

### Occam's razor

Sc. method: 1) Start with basic set of entities, methods of combining them.

2) Each entity method has params. assoc. with it.

3) Try / combinations in science problem; several params. of components in view of efficacy in problem solving.

4) Using new entities and methods and new levels of old ones, try solving new problems.

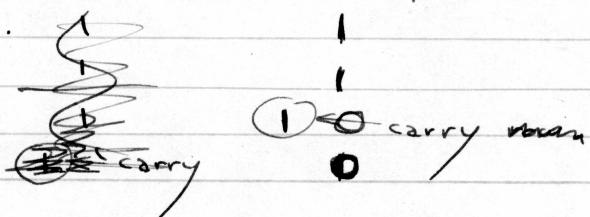
5) Continue.

Explain a "gp" as used in prediction.

Give example from Math T.M. of what prob. is

for  $=, \sim, \beta \Xi, \beta \Pi, +$ .

Use  $\boxed{?}$



Some initial g.p.s.

" " repeats n.gms

" " n.tpts

" " strts., strsts

How to get new entities from old.

$\beta \Xi, \beta \Pi, \text{Cart } \Pi$  (for n.tpts), convolution for strts,

The concept of factoring:

$$\left( \begin{smallmatrix} 1 & \beta & 1 \\ 1 & \beta & 1 \end{smallmatrix} \right), = \left( \begin{smallmatrix} 1 & 1 \\ 1 & 1 \end{smallmatrix} \right), \left( \begin{smallmatrix} 1 & \beta & \beta \\ \beta & \beta & 1 \end{smallmatrix} \right)$$

$$= \left[ (1,1), (1,\beta,1), (1,\beta,\beta,1) \right] \times (1).$$

$$(1\beta 1) \times [ (1,1)(1,\beta) (1,\beta,\beta) (1,\beta,\beta,\beta) ] =$$

$$\left( \begin{smallmatrix} 1 & \beta & 1 \\ 1 & \beta & 1 \end{smallmatrix} \right), \left( \begin{smallmatrix} 1 & \beta & 0 \\ 1 & \beta & 0 \end{smallmatrix} \right), \left( \begin{smallmatrix} 0 & \beta & 0 \\ 0 & \beta & 0 \end{smallmatrix} \right), \left( \begin{smallmatrix} 0 & \beta & 1 \\ 0 & \beta & 1 \end{smallmatrix} \right)$$

How analogy can be created by str, n.tpts.  
The use of definition by inversion.

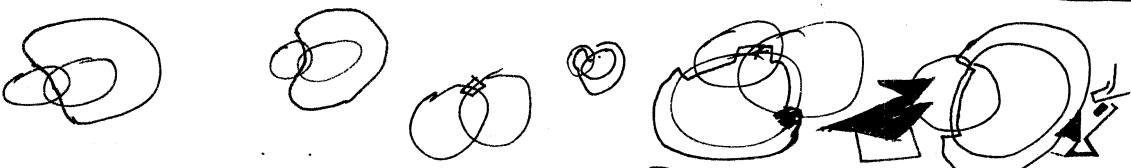
## M.C. methods:

- |  |                    |                             |
|--|--------------------|-----------------------------|
| 1. — simple search.                              | (non-(exhaustive)) | $\sum \frac{1}{k}$ trials]  |
| 2. — "   | " (non-")          | $\lceil n \rceil$ " ] Ashby |
| 3. — weighted "                                  | (non ")            | $\lceil n \rceil$ " ]       |
| 4. weighted "                                    | (exhaustive)       | ?                           |
| 5. by a non-linearly weighted search, exhaustive |                    |                             |
| 6. I do!, ordered exhaustive. <del>etc</del>     |                    | { first moment }            |
- only powers do this.

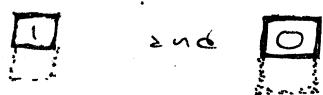
Probably M.C. search worked on by Op. res. theory.

Additional Note on my approach :

- 1) Explain concept of "simplicity" and "ad-hocness", giving various examples.
- 2) try to show that Ockam's razor is a trivial statement i.e. one couldn't possibly try all complex combinations of old good ideas, because there are too many.
- 3) Application to problem of how many params. to use in curve fitting, and fallacy of dividing data in 2 - one for param. determination, and 1 part for checking.



2 correct answer. For instance, the pair of diagrams



and

would give probabilities of  $\approx 50\%$

for both 0 and 1. This question bears a

(SN) What about use of the diagram pair , ?

Is this legal? I think it is "legal",

and that any gp. set can be used; (in one assign)

$\Rightarrow$  strong resemblance to ~~the prob. that of the~~  
2 prize filters with 80% and 70% wins, respectively.

> prediction params. to single g.p.s. or can one just do so for pairs of g.p.s.? Note that within this system the diagram is very useful in prediction, and it makes many other digits useful — say . If is used, becomes no more useful than . As long as there are only the 2 possibilities of 0 or 1, ~~the~~ is of much more use than .

$2 \times 8 \times 3$

What about v.s. ? Shouldn't this

be  $\approx 300\%$  as v.s.  $\leftarrow$  which is the

same as ~~skew~~ What probty. & distrib. one gets for  
.

One cannot ask an equivalent for



This is perhaps why one feels that and ought to be imp. Also, is of higher order than ,

(but not much)



Paying Th. weberman.

$f(q_k)$  If we want to pay  $f(q_k)$

where  $k$  is R. weather than that actually occurred.

$$\sum p_k f(q_k) + \lambda \sum q_k$$

$$p_k f'(q_k) + \lambda = 0$$

$$f'(q_k) = -\frac{\lambda}{p_k}$$

$$\text{if we want } f'(p_k) = -\frac{\lambda}{p_k}$$

$$q_k = p_k$$

→ If we use

Payoff of  $f_j(q_1, \dots, q_k)$

if  $\neq j \in$  event occurs.

$$\text{Then } \sum_j p_j f_j(\vec{q}) + \lambda \sum q_j \text{ maximized.}$$

$$\frac{\partial}{\partial q_r} : \sum_j p_j \frac{\partial f_j}{\partial r} (\vec{q}) + \lambda = 0$$

$$\text{we want } f_j' \rightarrow \vec{q} = \vec{p} \xrightarrow{\text{"true prob."}}$$

$$\therefore \sum_j q_j \frac{\partial f_j}{\partial r} (\vec{q}) + \lambda = 0.$$

solu. if  $f_j = \frac{\partial}{\partial q_j} f(\vec{q})$ . where  $f(\vec{q})$  is homogeneous of 1st.

Expected payoff =  $\sum_j p_j \frac{\partial f}{\partial p_j}$  which =  $f$ . (By ~~calculus~~)

$$\frac{\partial^2 f}{\partial q_i \partial q_j} x_i x_j > 0$$

so  $f$  must be simply convex.

This has direct intuitive significance.

Are there 2 different cost-of-observation functions for Th. weberman, are there 2 different  $f(\vec{q})$ 's  $\Rightarrow$  his expenditures on different kinds of observations will be the same?

Also, if Th. payoff funct. for Th. weberman is constrained (say  $\geq 0$ ), what is soln.?

For Simon, Newell.

- 1) Improvement of program by comparing it with their own intuitive processes.
- 2) They should compare their own programs with Mora's in as great generality as possl.

McCarthy.



Objectives ~~program~~ project:

To devise machine to do

McC is still involved with concept of simplicity, quickness of machine as criterion of intelligence, rather than goodness of soln. He is thinking of "well defined" problems.

McC still doesn't think probability of much use.

Few advantages listed for various possl. problems.

Design problems.

Inventing possible theories

The day of proposed proof machines

Certain probability problems: Involve taking certain verbal descriptions of ~~numbers~~ integers, and translating them into integers. E.G. "All integers  $\leq 5$ ,  $\geq 1$ " would give  $\{ 5 \}$ . Here we try a set of xfrns. on th. verbal expression, in attempts to get it into ~~another~~ one of a set of expressions that has a known no. assoc. with it.

This, then, is "a problem of th. 1<sup>st</sup> kind" Th. method of Soln. is very  $\approx$  to that of Simon - Newell - Mccarthy with. McC, Minsky refinement in particular.

NOTE: We have, then a kind of machine that can be designed to work very many types of problems of th. 1<sup>st</sup> kind. That a large class of prob. probs. can be put in this form is imp. It will be well to make a list of problems that can be put into this form. Altho these machines are not very "creative" they will work most problems much more rapidly than most humans who work on them.

General note on Neurological Models of behavior proposed by psychologists: That they tend to rephasize the "law of Use" [ I.E. if an animal does a certain act many times, he will be more likely to do it in th. future. ] This view does not take reinforcement - or results of this action - into account. Wiener's Theory of th. effective force mechanism is about th. next level of sophistication.

I think Habb's theory was a simple "law of Use" theory. [this is confirmed on th. bottom of p & end top of s]

□ □ □



**B**

$G = \text{"Good"}$ ?



~~a)~~  $G$  eval. for statements

b)  $\rightarrow$  " " " terms

if we have 2)

2 term is  $G$ , if it can be easily generated  
from things.

A term can be  $G$  in 3 ways (at least).

1) Simplifying expression of one or existing terms.

2) Simplifying expression of many old theorems

3) Expressing old statements using this term,  
enables one to prove theorems quicker, easier.

$\Sigma N$

2 and 3 may usually ~~not~~ imply one another.

A statement is  $\in \mathcal{E}$  if<sup>\*</sup> (It is a suitable sub-goal)

- 1) It is th. theorem to be proved ( $G = \emptyset$ )
- 2) " " "close" to a  $G$  statement.

[ Closeness has several different meanings ]

a) Logical equivalence. (?) [ trouble is that if  $A$  is  $G$ , the other may not be  $\in \mathcal{E}$ , because of its unwieldiness. ]

b) Asymmetrical closeness.  $A$  is close to  $B$  if  $B$  can be somewhat easily proved from  $A$ .

c) That 2 theorems (combined with some other fixed statements) can be both used to prove (using standard machine methods) ~~fixed~~ theorem  $T$ , in about the same no. of steps.

Another way to say this, is that these 2 theorems are about the same (upper) distance from  $T$  on the lattice. If ~~are~~ 2 theorems

on  $\mathbb{R}$ . Some dist. from many  $T_i$ 's, then they have, in a sense,  $\mathbb{R}$ . some "coordinates".

(8.3) (3)

Actually, Th. idea of  $G$  for th. "free" computer is signif. different from that for th. computer that has to prove a particular theorem. In th. "bound" case, the  $G$  is related to th. closeness to th. terminal expression.

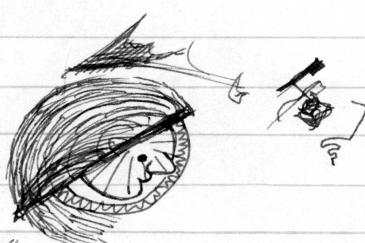
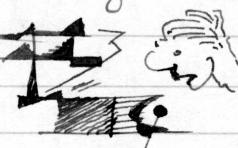
In th. "free" case th.  $G$  is defined in terms of "simplicity", "bravity", (using "simple terms"). Also by statements from th. operation about how  $G$  an expression



Thurs June 28, 1956

TSN Make small op. study to determine ways to get all members of gp. [motivated] by proper words, cues, encouragements].

Minsky:



Machine for proving theorems

- 1) Input is logical statement
- 2) first process is standard "logical cleanup" mechanism, that is used at various stages of proof.

$$\sim \sim A \cdots \rightarrow A$$

$$\sim A \cdot A \rightarrow I$$

- 3) statement then goes to "Characterizer" That ~~gives~~ puts statement into 1 or more of several important categories. Produces string of nos. to give apri categorics. Th. Categorizations methods should be improved as time goes on.

2 kinds of categories

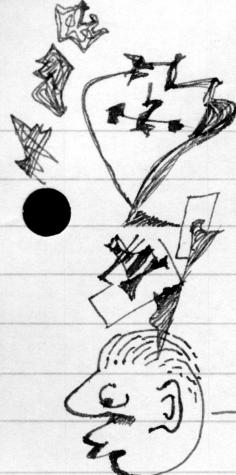
- a) Statements about statements themselves  
e.g.: ~~is~~ how many letters, how many expressions, how many levels, how many different letters.
- b) Which theorems are like it? (memory search)
  - e.g. some hypothesis, or some conclusion, or large parts that are R. same.
  - c) look for key words ~~like~~ in statement, like "probability".
  - d) To what examples does this statement apply
  - e) What statements can it prove? (if certain things are added to it).

- 4) Method box.  $M_1, M_2, \dots$

Are various proof methods.

A method transforms a statement or set of statements into a new

- 5) Success memory: Decides when a method has been useful in proving a theorem. We then score various characters of theorem assoc. w/ with that method.



	$C_1$	$C_2$	$C_3$	$C_4$	
$M_1$	3	9	8	40	
$M_2$	0	7	0	8	
$M_3$	4	1	1	1	
$M_4$	4	1	0	1	
$M_5$	3	2	2	0	

Keep of record  
of corr. state  
between characters,  
methods. We may want  
some joint correlations.

6) Evaluator of state of system: Whether  
program has been proved.

7) A device that tries to find subgoals — i.e. states of system "one" say  $T_1$ , is initial state,  $T_2$  is desired final.  $V$  tries to find  $T_3$  such that it is easy to go from  $T_1$  to  $T_3$  and from  $T_3$  to  $T_2$ . This is done by looking over various pairs  $T_1, T_3$  in the success memory.

8)  $V$  evaluator — Looks at present situation, and desired final situation, and it gives the order as to what method to use next.



## Milner

Associationism of 18<sup>th</sup>, 19<sup>th</sup> cent. as of Hebb.

Flow something in brain can become "representative" of a certain type of stimulus.

General inhibition, and localized cross inhibition.

Golgi cells give of burst of pulses for singular pulse input.

"priming substance" lasts for ~ 1 second.

Assumption, that if A fires B many times, that this is facilitatory for that connection.

No empirical evidence for this.

Milner is using this



~ 4:30 AM Awake.

lite lunch over ~ 2:30 A.M.

first A

gives A'

Now

A and B

, then B

gives B'

in time or space

producas

intime or space

together / several times,

then if A then A' + B' almost - also

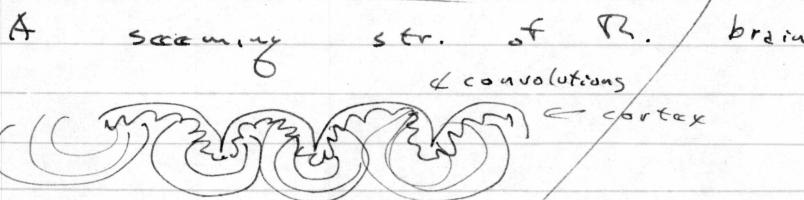
" B "

" "

" "

" "

This is called association.



cortex is mapped to some areas,

onto various str. of R. brain : e.g. Thalamus, Cerebellum  
are known for certain to have this mapping.

McCulloch says that there have been many regions found that map partly topologically onto R. brain cortex. (If they map onto R. cortex it is probable that they do so topologically)

This would be mildly like my sec. recent. T.M.  
- with R. cortex being the main mechanism, and  
R. rest of R. brain being R. sec. recent. computer.

Problem of association in this simple temporal or spatial form seems not too imp. Marr suggest some assoc.

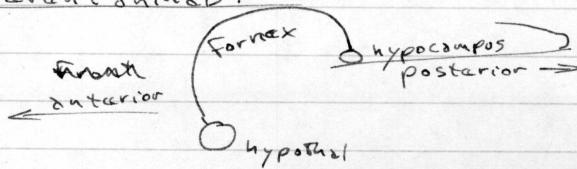
mechanisms + recent. would be useful, so working on

This is a basic hypothesis of naive Association  
learning theory: Information

→ These mechanisms of learning might also be imp.

Reinforcement "centers" in rats: Milner (assoc. with Habbitt McGill)  
Olds was early worker on this. Some work (not by Milner)  
done on cats, monkeys. Sensitive regions:

anterior hypothalamus, fornix, hippocampus. Best on / hypothal.  
Sensitive region slightly different in different animals.



(.2 to 2 Volts, 60 Hz) was  
a drug to a drug addict.

They will do or learn  
almost anything to get.

## Milner

that stimulation. They will, if nec., die from lack of H<sub>2</sub>O or food, if they can be allowed to press stim. button instead. They quickly learn mazes if this stim. is reward.

Electrodes are easy to place. One asst. of Milner has ~~an~~ 100% success in placing them. Wires are from top, from 1 spring or rubber band. — Is small impediment to animal.

In humans, accidental or purposeful cutting out of Th. hippocampus, made subject unable to learn new things, tho' he retained old learning! This is extremely suggestive, that Th. hippocampus is ~~imp.~~ <sup>along</sup> / or at one end of any reinforcement pathway. I don't know which way the pulses travel along Th. hypothal - fornix - hippocampus circuit.

→ Extremely eager maze behavior. Some tendency not to learn about dead ends in maze, and repeated making of same mistakes. — much worse than normal behavior.

R.F. (wireless) control, with antenna used (not by Milner) for some stimulation work (I don't know if in this partic. type of exp.). Trouble with ~~is~~ very non uniform distrib. of R.F. field. This would be alim. by using 60~ or higher freq. induction field, with an Fe core coil inside Th. rat's brain, for a pickup. But Milner says the wires leading to Th. animal are no cause of trouble, anyway.

## Milner.

Assoc learning, even with recent, is only a small part of Ph. no. of useful imp. epist. tricks that are use. in prob. solving. However, it is still imp.. A good idea would be to list the various epist. Golgi type = area inhib. cells.

Afferent =  $\xrightarrow{\text{input}}$  neurons

Milner theory: widespread inhib. from a gen. neuron.

Probabilistically, there will be some non-inhibitory loops formed

Saffridge suggests cross-corr. as a funct. of dist. — that for very close electrodes, cross-corr would be small. Th: Penicillate cells have large, recognizable spikes,

→ tricks that are nec., and try to complement them with neurological models. Geometric closeness is easy to model but substitution of variables in an expression is difficult. It would be

Milner: That his cell assemblies are on for duration and activity shifts from one to another in jumps.

→ fine to get a "basis" set of epist. concepts. These can be put in the motor, as well as production mode.

One has a ~~wanted~~ sensory situation, and certain motor responses have higher than normal ~~is~~ probability of firing because of this situation. This ~~is~~ I want this to corresp. directly to by a priori. If such motor responses turn out to be ~~reinforced~~ "rite" or "Good", then they are reinforced — which corresponds to an increase in statistical count. Statistically, an anomalous occurrence of only a few or one time, of cases of by a priori, ~~situation does~~ give signif. confirmation of goodness of production method.

If A caused B with reward, then we want A' to cause B' where  $A \xrightarrow{R} B$  and  $A' \xrightarrow{R} B'$

and R has been found to be a useful relation.

The basic Q. in neural nets is not how to get various kinds of "association", but it is "~~assuming~~" I can get any kind of definable association that I want, how can I get reasonably useful behavior out

## Milner.

of this?" This q. is an expt. one, and is indep. of neural mechanisms. It tells what kinds of "Assoc." might be ~~as~~ almost acc. to get observed behavior.

One simple kind of conditioning (learning): temporal sequence.

$A_{\text{sensory}} \rightarrow B_{\text{motor}} \rightarrow \text{reward}$ .

$A'_{\text{sensory}}$ ,  $A''_{\text{sensory}}$  often occur together temporally,

$A'_{\text{sensory}} \rightarrow B_{\text{motor}}$  then tends to be tried. ~~tried~~

(This ~~attempts~~ is, or might be called "substitute stimulus").

Milner:  $\sim 200$  or  $300$  synapses per cell observed

$\hookrightarrow$  Suppose one has a certain ~~and~~ sensory config  $\rightarrow$  motor config. connection. To figure out a way in which another ~~near~~ sensory config would <sup>tend to</sup> give another motor config.  $\Rightarrow$  Th. second pair were "close" to Th. first.

N. Rochester. on how to simulate Milner's nets.

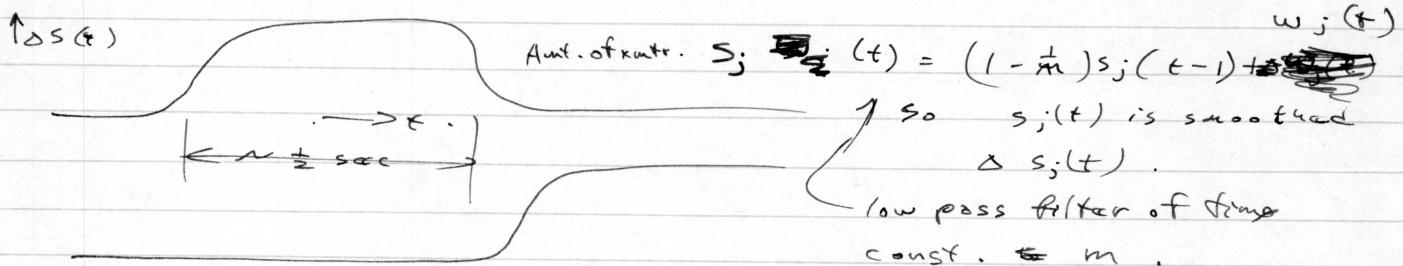
$$w_j(t) = k \sum_i x_i(t-1) r_{ij}(t-1)$$

$\downarrow$  change in amt.  
of power (xattr)

$r_{ij} = \text{size of syn.}$



Time of action of cell assembly  $\sim 10$  st.



fatigue:  $d_j(t) = \theta_2(x_j(t-1), d_j(t-1))$

$x_j$  = freq. of  $j$  at time  $t$ .

$d_j$  is increasing if  $x_j$  is  $>$  certain level

if freq.  $x_j$  is above certain level,  $d_j$  increases each <sup>by const.</sup>  
if below,  $d_j$  decreases each time.

Increasing fatigue tends to  $\downarrow$  freq., so this tends to  $\rightarrow$  some extent to keep  $x_j$  at a certain level.

$$x_j(t) = \theta_3(s_j(t), d_j(t), \text{inhibitor}, x_j(t-1))$$

and absolute

Inhibition assumed to be unconditioned/and  
special is short range effect.



→ This makes  $\Delta x_j$  an imp. contributor to learning. also  $x_j(t-1)$

Synapse magnitude  $r_{i,j}(t) = \beta_1 r_{i,j}(t-1), x_i(t), x_j(t), \sum_{j \neq i} x_{ij}$   
 Scale of long term learning. If both  $x_i$  and  $x_j$  are large,  
 $r_{i,j}$  tends to 1. This is periodically renormalized,  
 so that  $\sum_{j \neq i} r_{i,j}$  is kept  $\approx$  some constant.

A neuron gives out its local inhib. if its freq.  
 is  $> \epsilon$ , but whether  $\epsilon$  should  $= 0$ , ~~be~~ or be  $> 0$   
~~isn't~~ isn't yet decided.

Hebb wants / both short and long term memory.

For selection of "best" motor action, simply ↑ all  
 excite freqs., until a motor pattern is triggered.

Make list of sensory strings that are close in P. sense.

of having same desired motor response.

Thurs O.K. : Sun. O.K. Sat O.K. [Mon: L must be at meeting in N.Y.]