

Uses, say, 3 coeffs (quadratic regression, if a function of 1 variable), is a special way of inserting apri. info.

It seems ~~is~~ very probable that if one stated exactly what all of one's important apri assumptions were, that one could get optimum regression curves and their variances.

Stated exactly, it means that one has an apri density in function space, and a "probability of error" function [this means the probability that if th. "true" function were  $y=f(x)$ , that th. pair  $x_0, y_0$  could occur], then one could easily find th. right regression curve, using Bayes inverse probty,

16 from (15).07 I guess: that ~~needed~~ expected fractional error in variance = expected fractions / ... - No., its a rather complex problem, but th. ansr. can be found in any statistics book.)

From Cramer: p 349 eqv 27.4.5:

observed Expected value of variance (for normal distrib) of true variance  $\sigma^2$ , is  $\frac{n-1}{n} \sigma^2$

Expected second moment of th. variance =  $\frac{2(n-1)}{n^2} \sigma^4$  ( $\approx \frac{2}{n} \sigma^4$ )

Th. s.d. of th. variance  $\approx \frac{\sqrt{2}\sigma^2}{\sqrt{n}}$  for large n.

On P. 382 (Cramer)  $\frac{n s^2}{\sigma^2}$  has a ~~chi~~  $\chi^2$  distrib w/  $n-1$  d.f. of freedom. I guess  $s^2$  is R. observed variance.

$$s^2 = \frac{1}{n} \sum_{i=1}^n x_i^2 - \left( \frac{1}{n} \sum_{i=1}^n x_i \right)^2$$

We can, then, look upon th. variance as a quantity of mean  $\sigma^2$  and s.d.  $\frac{\sqrt{2}\sigma^2}{\sqrt{n}}$ .

I think it is th. variance of a quantity that determines

I think th. statistical wt. of ~~quantities~~ <sup>reciprocal of</sup> observation is directly prop. to its Variance.

It may be poss. to arrange th. measures of one's coeffs,  $\rightarrow$  as one's sample size  $\uparrow$  one tends to use more coeffs - in a certain linear order.

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The prob. of page 13) is this: From a "certain source" one gets  $U_{\text{apri}} \text{ and } \frac{1}{\sigma^2}$  ( $\equiv$  wt. to be assigned to  $U_{\text{apri}}$ ). One observes some statistical data on  $U$ , which we will call  $S$  — this data is to be given weight  $n$ , since there were  $n$  observations. Th. best estimate for  $U$  is then

$$\frac{\frac{U_{\text{apri}}}{\sigma^2} + nS}{\frac{1}{\sigma^2} + n}$$

We want to know how  $U_{\text{est}}$  differs from  $U_{\text{apri}}$ , on pg.  
 average for many estimates of  $U_{\text{apri}}$  that come from this "certain source". When we find this  $\frac{(U_{\text{est}} - U_{\text{apri}})^2}{(\frac{1}{\sigma^2} + n)^{-1}}$  ← taken over th. output of th. "certain source",

We will set this = to  $\sigma^2$  for th. entire source.

Let  $U_{\text{apri}_i}$ ,  $n_i$ ,  $s_i$  be th.  $U_{\text{apri}}$ ,  $n$  and  $S$ , assoc. with th.  $i^{\text{th}}$  output of th. "certain source".

then  $\sigma^2 \approx \frac{1}{r} \sum_{i=1}^r \left( \frac{\frac{U_{\text{apri}_i}}{\sigma^2} + n_i s_i}{\frac{1}{\sigma^2} + n_i} - U_{\text{apri}_i} \right)^2$

( $\approx$  because  $\sigma^2$  → there may be some  $\frac{1}{n_i}$ 's or  $\sqrt{n_i}$ 's in this  $\approx$  eqn.)

$$\sigma^2 \approx \frac{1}{r} \sum_{i=1}^r \frac{(s_i - U_{\text{apri}_i})^2}{(\frac{1}{\sigma^2} + 1)^2}$$

Th. formula isn't exactly right. There is, I think, some kind of proportionality constant betw. th.  $\frac{1}{\sigma^2}$  weight, and th.  $\sigma^2$  due to deviations betw.  $U$  and  $U_{\text{apri}}$ .

Let us get more specific: say  $U \equiv$  th. mean no. of "cases" per unit time (actually, this may not be such a good def. of what I want, but let it go for awhile).

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Say we have had  $\uparrow$  q. elements up' to time t.

If we have had c cases for a certain pugm, then

$$s_i = \frac{c}{t} \text{ and the stand.dev. variance is } \sqrt{\frac{c}{t}} = \boxed{\text{ }} \cdot \frac{\sqrt{c}}{t}$$

Th. variance is  $\frac{c}{t^2}$

~~This might go to this~~

Now if  $\sigma^2 = \boxed{\text{ }} \overline{(U_{\text{aprop}} - U_{\text{actual}})^2}$

Then the estimate must be 
$$\left[ \frac{\frac{U_{\text{aprop}}}{\sigma^2} - \frac{t^2}{c} \cdot \frac{c}{t}}{\frac{1}{\sigma^2} + \frac{t^2}{c}} \right]$$

$$= \frac{\frac{U_{\text{aprop}}}{\sigma^2} + \uparrow}{\frac{1}{\sigma^2} + \frac{t^2}{c}}$$

$$= \frac{U_{\text{aprop}} \frac{c}{t^2 \sigma^2} + c}{\frac{c}{t^2 \sigma^2} + \uparrow}$$

Then 
$$\left( \frac{U_{\text{aprop}} + \uparrow}{\frac{1}{\sigma^2} + \frac{t^2}{c}} - U_{\text{aprop}} \right)^2 = \left( \frac{\frac{U_{\text{aprop}}}{\sigma^2} + \uparrow - \frac{U_{\text{aprop}}}{\sigma^2} - \frac{U_{\text{aprop}} t^2}{c}}{\frac{1}{\sigma^2} + \frac{t^2}{c}} \right)^2$$

*(This is probably the best estimate of  $U_{\text{actual}}$ )*

$$= \left( \frac{\frac{t^2}{c} \left( \frac{c}{t} - U_{\text{aprop}} \right)}{\frac{1}{\sigma^2} + \frac{t^2}{c}} \right)^2$$

say  
 $U_{\text{aprop}}$   
 $N \approx \frac{c}{t}$   
 no. of cases |  
 wt. |  
given to  
 $U_{\text{aprop}}$   
 $\approx U_{\text{aprop}} / \sigma^2$

.30 So  $\sigma^2 \approx \frac{1}{r} \sum_{i=1}^r \frac{\left( \frac{c_i}{t_i} - U_{\text{aprop}} \right)^2}{\left( 1 + \frac{c_i}{t_i \sigma^2} \right)^2}$

This equ. is of the form

$$x = \sum_{i=1}^r \frac{a_i}{\left( 1 + \frac{b_i}{x} \right)^2}$$

$x, a_i, b_i$  all  $\geq 0$ .

.38 Actually, th. equ.  $\boxed{\text{ }}$  have more in it. In determining  $\sigma^2$ , each pugm. cannot be given = wt. - because first, th. approx. of ultimate are not equally good, and secondly, all pugms are not of importance.

This seems kind of wrong - i.e. I feel that  $\sigma^2$  should be "open loop" and not "closed loop" b/c a function of itself. In a sense, it isn't much of a function of itself - assuming ~~the~~ (18).30 is correct (~~the~~ ignoring the comments of (18).30).

$\sigma^2$  is almost an average of  $(\frac{c_i}{\tau_i} - U_{\text{app}})^2$

When  $c_i \approx \frac{\tau_i}{f_i} \gg \frac{1}{\sigma^2}$  [i.e.  $\frac{c_i}{\tau_i^2 \sigma^2} \ll 1$ ]

say  $\frac{\tau_i}{c_i} \approx \frac{1}{f_i}$  [ $f_i \rightarrow U_{\text{ultimate}}$ ;  $\tau_i \rightarrow \infty$ ]

then we want  $\frac{\tau_i}{f_i} \gg \frac{1}{\sigma^2}$  for  $\sigma^2$  to be not ~~very~~ dependant on  $\sigma^2$ , and for eq. (18).30 to be easily solvable.

More exactly, we want  $\frac{\tau_i}{f_i} \gg \frac{1}{\sigma^2}$  for most pugns

Woops!  $\tau_i = \tau$  is the same for all pugns.

• or • ~~unless~~  $\tau_{\sigma^2} > f_i$  for most pugns.

note  $\tau_{\sigma^2}$  is indip. of  $i$ .

Of course if  $\tau_{\sigma^2} \gg f_i$  for most  $i$ , then

$$\sigma^2 \approx \frac{1}{r} \sum_{i=1}^r (f_i - U_{\text{app}})^2 \text{ is good enough!!!}$$

What we really want is to be able to get a reasonably good  $\sigma^2$  as soon as poss. - i.e. with as small  $r$  as poss. - which is the pt. of all this mathematical refinement. Th. q. is - is formula (18).30 ever any better than?

[ Well, our main goal ~~is~~ here, is to ~~minimize~~ <sup>define and use</sup>  $\sigma^2$  in such a way as to minimize prediction errors. ]

This seems like a fairly straight forward problem in statistics — I suspect that (8).30 with, perhaps, corrections in line with (8).38, and also corrections to give various things different weights since they occur with different frequencies and are of different "importance" statistical problem: There exists a platonic set of numbers,  $f_i$ . ( $\sum f_i = 1/r$ )

We have one source that gives us  $U_{\text{apri}}$  which form a normal distrib. about  $f_i$ 's — all with the same  $\sigma^2$ .

We have ~~another~~ another source that gives us  $S_i$ 's that are also normal about  $f_i$ 's but each ~~has~~ has a known  $\sigma^2 = \frac{1}{n_i}$

Given all the  $U_{\text{apri}}$ 's,  $\frac{1}{n_i}$ 's and  $S_i$ 's: to find  $\sigma^2$ .

This seems O.K., except for ~~these~~ reservations and probability

(8).30 is a reasonable soln., within the reservations.

Thinking about it some more: what (8).30 does is assuming  $f_i = \frac{U_{\text{apri}} + b S_i}{\sigma^2}$  ( $a$  and  $b$  are proper wts.).

and then get  $\frac{(U_{\text{apri}} - f_i)^2}{\sigma^2}$ . This is very probably

, 30 } not correct in general. The correct way is to try all  $f_i$ 's and  $\sigma^2$ 's and find P.  $\sigma^2 \rightarrow$  P. observed

phenomena are most probable (integrating over all poss.  $f_i$ 's with, perhaps, suitable wts. for various  $f_i$  regions).

This may not be so hard: fix  $\sigma^2$ , then integrate over all  $f$  space to find out how probable P. observed info is. This integral will be a funct. of  $\sigma^2$ . Find  $\sigma^2 \rightarrow$  P. integral is max.

The integration isn't diff. — Use p dim. vectors, and multidim. gaussian dists. — However, each dim. appears to be indep.

There is a more extensive discn. of this on page 121

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I don't think I should bother with the ~~maximization~~ integrations and extremaizations [They might be done simultaneously] except, perhaps, after lunch. They are of the type  $\int \left( \frac{1}{x} e^{-\frac{x^2}{2}} + \frac{1}{x^2} - \frac{(x-a)^2}{x^2} \right) dx$ . It might be more imp. to look into 18). 38. The first q. of 18). 38 is probably included in the soln. of the problem as stated in 20). 30. The second q. in # 18). 38 isn't so clear. I must state exactly what I want  $\alpha$  to be.

But I think that I have gone far enough into this problem for the present. The imp. pt., is that it is a definite math. problem, without and no additional assumptions need be made.

At the present time, the most imp. single problem seems,

What is  $U$ ? Some discu. on pp. 6), 7), 8), 9)

Also, try to define  $U$  for non-Math-T.M. — i.e. probabilistic prediction. Try to fix it so it is easy to isolate out the  $U$  of a particular pugm. — even since this ~~solves~~ solves problem ~~of whether~~<sup>how</sup> to retain a word that is not the "best," but still O.K. ~~Also~~ Also B.G. becomes easy: i.e. by <sup>making</sup> each prediction depend on a single pugm.

A way: In the gen. T.M. (not Math-T.M.) case: Each pugm. has a prediction vector assoc. with it. To find the  $U$  of a ~~pugm.~~ take a McMurphy-like avg. over all cases in which it applied. This gives a certain amt. of money ~~for~~ for the value of that pugm. Then choose a set of pugms.  $\Rightarrow$  their total worth is maximized. In cases where ~~they~~<sup>2 pugms that were chosen</sup> conflict, then take ~~an~~<sup>wtd.</sup> average of their prediction vectors. Wts. to be decided on the basis of some sort of  $U$  criterion — No one should try to choose a set of pugms so that they do not often cover the same case. If 2 pugms have the same prediction vector with as well  $\beta \leq \text{them}$ .

How does one get prediction vectors? — simple th. ~~distribution~~ distribution over the history of that pugm.

So the big problem, then, is to decide which ~~a~~ set of pugms to use, and how to weight them when 2 apply to the same ~~case~~ <sup>opposite</sup>.

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This isn't far from th. ~~the~~ U problem in Math T.M. as discussed on pages 8) and 9)

What one will get, is several sets of pagans. Each set can be used fairly well for prediction. What happens when new pagans are devised, however? — Don't they have a very poor chance of being useful, since most possibilities are already covered by the old pagans — though even tho. some are not covered very well, will each <sup>set</sup> of pagans have its own set of U's for all of the pagans, stirs up lots?

But th. imp. q. is: Just how are new pagans introduced?

from 15 SN: In  $U_{ij} \approx U_{s,i} + U_{n,j}$   $(i, j = 1/n)$

(2) 40 we wrote

$$U_{s,i} \approx \frac{1}{n} \sum_j U_{ij} - \frac{1}{n} \sum_i U_{ij}$$

$$U_{n,j} \approx \frac{1}{n} \sum_i U_{ij} - \frac{1}{n} \sum_j U_{ij}$$

It must be noted that the criterion for fit is not for the goodness of the  $U_{s,i}$ 's and  $U_{n,j}$ 's as individuals, but for how good  $U_{s,i} + U_{n,j}$  is, which is easier. It may be possl. to show that something like       , perhaps itself, is, indeed optimum.

Also, ~~the~~ How to form the sets in a convenient way.

There is th. q. of whether to take all ~~and~~ and select out the "good" ones and use them only, or use all of the pagans, but use wts.

~~In this new method, there is th. q. of how to group together pagans that don't have th. same prediction vector?~~

Th. q's are 1)

2) It is felt better, epistemologically, to use as few words as possl., to cover as wide a range of phenomena as possl.

3) This conflicts with th. idea that one can usually get very good prediction by th. use of very small sets of phenomena, so that <sup>n. members of</sup> each set are very much ~~like~~ alike, and so that

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one can get very fine differences between cases by using many very small sets.

Discn: It may be that what were few in number, are the objects from which one forms th. sets. ("sets" = pgms) (objects = ngrams, strings) Examples: Red bike, old orange.

• 07 ~~from 0 > 6.02~~ ~~15~~ ~~mid~~ ~~work until 11 P.M.: eat 11 P.M. - 1 A.M.~~

~~sleep 15 - 8 AM: work 8 AM - Noon; Eat Noon - 1 PM.~~

~~work rec. 1 PM. - 5 PM: work 4 PM. - 11 P.M.~~

4) On the other hand, if many interesting statements have few words in them, then the words must be many words and .. small sets corresponding to them (?).

I think this is all being very el.. Th. final def. of  $U$ , is how useful the object is in prediction. I am afraid, however, that this ends us up in the "swamping out" problem. Th. way to avoid this problem, may be to put one's words into GPS, so that each op. has a  $U$ . - But then there the prob. of how to introduce new words into the GPS.

This method turns out to be (case that suffers from "swamp out").

A reasonably good method of prediction for th. Non-Math T.M. Most objectives seem overcomable. Each program is given an apri. prediction vector, and an apri.  $U$ . ( $U$  is a funct. of prediction vector, and freq of occurrence of th. program.). For a given prediction, th. "best" program that applies, is used.

To get away from "Swamp Out": every program (good or bad) will have assoc. with it, a param. that tells how useful it would have been, if it were used every time it was applicable (whether it was "best" or not). This param. will be used to determine th. apri. that this program will be useful in

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~~Thus~~ forming new pograms — via, nips or ngsms.

Also perhaps This  $U'$  will be

~~that~~  $f \leq \sum p_i l_{p_i}$ , where ~~is~~  $\vec{p}_i$  is  $i$ th prediction vector  
and  $f$  is  $i$ th freq. of ~~the~~ applicability of this pogram.

Also, perhaps, when ~~all~~ pograms are formed, their aprie  $U$ ,  
will be  $i$ th aprie of This  $U'$ . In this way, one will,  
as before, try to get pograms with as by  $U'$ 's as possl.

But in each case of choice as to which pogram to use,  
one will chose  $i$ th one with greatest  $\sum p_i l_{p_i}$ , not,

th. one with greatest  $f \leq \sum p_i l_{p_i}$ .

There is a serious q. here! Do we want to get  
pograms with by  $\sum p_i l_{p_i}$  or with by  $f \leq \sum p_i l_{p_i}$ ?

If  $\sum p_i l_{p_i}$  is too low,  $i$ th pogram will not be used, so that  
its  $\Delta U$  will = 0. Also if  $f$  is too low, even if  
 $\sum p_i l_{p_i}$  is by,  $i$ th pogram will not be often used, so  $\Delta U \approx 0$ .

$\sum p_i l_{p_i}$  is by, Both.  $f$  and  $\sum p_i l_{p_i}$  are imp., but it is not clear  
that this product is  $i$ th best representative of probable  $\Delta U$ .

It may be possl. to show that it <sup>should</sup> ~~would~~ be  $\propto f$ .

$\therefore$  th.  $U'$  would =  $f \cdot g(\sum p_i l_{p_i})$ , where  $g$  is some  
function to be determined — it would depend on  $i$ th distribution  
function of  $\sum p_i l_{p_i}$  for ~~all~~ pograms.

Another ~~obj~~: Trouble with above: One cannot group  
together pograms that don't have  $i$ th same prediction vector —  
certainly this is bad. An ad-hoc way to avoid this <sup>that doesn't look too bad!</sup>

Each pogram prediction vector has only 2 components —  $i$ th component  
of interest (which we want close to 1), and ~~the~~ 1 minus  
that component — This prediction vector, has, then, only 1 component.

We can then group say pograms together that we like —

Say  $\boxed{1}$  and  $\boxed{2}$ . In  $i$ th first case,  $i$ th.

measuring of the prediction vector is one thing, in P.M. second cosa, another. The  $g \in P_2(n_p)$  ~~is~~ of 24.30 becomes simply ~~one~~  $g(p)$ .

This all seems to apply very easily to Math T.M., as a special case. If we use  $f(g(p))$  as a measure of utility, then in math T.M.,  $g(p) = \text{constant}$ , so utility is  $\propto f$ , which is the criterion we were thinking of using before. Since all ~~the~~ "consistent" pugns have the same  $g(p)$ , then ~~most~~ all pugns of  $g(p) < \max$ , are ~~discarded~~. The only choice is of  $\alpha = \text{value for making a decision}$ . The probability that they are, indeed, both of  $\neq g(p)$  lies in the probability that they are, indeed, both of  $\neq g(p)$  — i.e. one or both may not be "consistent" — This is a q. of sample size — ~~but, was discarded~~ — or, more exactly, the "expected error" in  $g(p)$  — which would be given by the "expected mortality" of a pugn for a given sample size.

As was discussed before, however, the likelihood of such a conflict is small, and the "jump" in contribution to the mean  $U$  of T.M.

However, the q's raised here in T.M. on P.M.

relevance of  $g(p)$ 's of P.M. 2 pugns. may be ~~written~~ important when applied to Non-Math T.M.

Def. of Non-Math-T.M.: In T.M. there is always <sup>math</sup> ~~one~~ right ans. for each  $g$ . In Non-Math-T.M., there may not be a single right answer — ~~math~~ i.e. even with the very best pugn, <sup>for a given</sup> there is not necessarily 100% prediction accuracy.

Question: Still isn't clear as to whether to use pugn count for anything — i.e. in addition to "cases". Try to see if Non-Math T.M. sheds any light on this problem. Review previous writing in these notes, on this problem.

It seems clear that  $U$  should be or "cases", but  
 P. question of variance of  $\bar{P}$  is P. problem here.  
 How does P. "count" size / determining consistency probly?

4th. suggestion of 7).22 : . to plot mortality  
 of consistency as a function of "counts" and "ages", after  
 some theoretical work to ~~get~~ get a functional  
 form.

There is no "hurry" with the above plot, since it  
isn't ~~too~~ imp. anyway. ~~that's~~ ~~the~~ ~~the~~ Mgs of  
hy count may be imp., ~~start~~<sup>and</sup> 2nd 4 in forming new  
pugs may be a funct. of ~~old~~ pugs count as well as no. of cases.  
Half 11 due to its being 4th chosen pair.

Discuss Attempts to predict /  $U$  and  $U'$  .

both  $\downarrow$  Ideal U, due to its being "4th. chosen one"  
 $\downarrow$  U due to no. of cases

to its being th. chosen  
N due to no. of cases

In Math T.M., there is also the same problem of  
over lap of programs in assigning U. If program A completely  
overlaps B, then ~~the~~. The existence of B is ~~wasteful~~,  
and certainly ~~pointless~~? except that A may "die" and leave B  
surviving. For this reason, it appears O.K. to ~~allow~~ score both

The ultimate goal of Math T.M. is to have only = consistent  
program that covers all poss. cases.

→ A and B whenever  $\#$  a case of  $B$  occurs. Another possey is to score the one with largest U. At first this would give the one with largest U a large lead — which it would always retain. If this was B, then A would occasionally score, when a case occurred in A but not in B — but only then.

Probably this: That actually one should score both A and B whenever B is scored - regardless of th. <sup>either</sup> prop. U's of A and B. ~~However~~ <sup>from</sup> the fact that A or B might have slightly more U than the other, probably it's wrong and ~~wrong~~ was <sup>was</sup> wrong!. The one that was chosen,

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probably isn't too relevant. A slight difference in  
appr. U / <sup>betw. A and B</sup> mite give — A practically no "cases" — yet  
The U of A and B mite really ~~be~~ about =. Also, they  
should have about = U in creating new pages.

Now what is done in R.W. language is that often  
A or B would be chosen and the other "swamped out." ~~the~~  
The reasons may be) that A and B are used in communication —  
not only for prediction 2) That "swamping out" one, ~~is~~  
makes more economical use of the available memory. It  
does this without much loss in efficiency (usually), since if  
A and B overlap and occur ~~but~~ usually ~~at the same time~~  
simultaneously, then usually either one can substitute for the other  
in creating ~~the~~ <sup>about the same</sup> new pages.

"Swamping out" may not usually be so bad, but I seen to  
<sup>encountered</sup> one ~~the~~ seriously bad case in the prevalence of  
ptatograms over ~~the~~ programs, in the prediction of N.  
Also I think it tends to make getting stuck in blind alleys more likely.

probably the best thing to do: keep counts on  
all programs in both Math and Non-math T.M.s. In ~~the~~  
Non-math T.M., the predictions will be made on the basis of  
the "best program", but the fact that a given program was "best"  
very often, will reflect in no way in its U or in the  
in its U for creation of new programs.

Later, the discarding of programs that are not "best"  
often, or are "best" only by a small margin if ever,  
will be done as a memory economy measure.  
This decision may cause T.M. to diverge from  
intuitive methods of problem solving, so we must  
remember this decision, ~~if~~ if any divergencies or difficulties  
appear.

About the biggest Q. at the present time: What to  
do about "cases" and "counts" in evaluating ~~the~~ probability  
of death? (~~the~~ U evaluation was decided to be on the basis of  
"cases"). What I have done so far is to keep both  
"count" and "cases", but discard <sup>(= becomes inconsistent)</sup> programs on the basis of

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of "count". This isn't a bad idea - since T.M. need never get answers to its  $\square$ 's. These answers would be direct, if we are to be able to discard pages of "inconsistency" on Pn. basis of "cases". This argument is analogously true in non-Math-T.M. But it suggests a soln. to the other part of Th. Math T.M. problem!

In NMTM ( $\in$  Non Math T.M.) [ ~~$\in$~~  MTM  $\in$  Math-TM],

the prediction vector is determined on Pn. basis of "count" <sup>as</sup> Pn. UGIMP, since by going to bias the prob. distrib.

is th. expected accuracy of that vector. Analogously <sup>of th. prob. vector</sup>

Th. expected "accuracy" of a prediction vector in MTM should

be on Pn. basis of "count"! This is kind of reasonable

in a few ways, anyway. If one discards on Pn. basis of "count",

and A has listed  $n_A$  counts,  $B$ ,  $n_B$  counts, ( $n_A \gg n_B$ ), then

if A is to die next ~~turn~~ <sup>"count"</sup> then than it is much less probable than that B should die on Pn. next "count". Remember, we

have only known "count" data, as far as discarding criteria is concerned.

It seems fairly certain that th. probability of discarding on Pn.

next count would be a function of total count. There

may however, be some correlation betw. case no. and prob. of discarding on Pn. next count. (that is, because of  $\rightarrow$ )

for page P

Useful Defs: 1) An occurrence of a count /  $\in \alpha$   
2) " " " case.  $\in \beta$

1)  $\#$  than P  $\xrightarrow{\text{verb}}$  counts

2) than P  $\xrightarrow[\text{verb}]{\text{P}}$  cases (can only occur at time of a q. element.)

count no. of P = no. of times P has counted

case no. "P = " " " " cases.

for a  $\square$

Great!! So If we have 2 conflicting pages in MTM,

then th. page with th. largest count no. wins. Th. prob. ratio will be <sup>something like</sup>  $\frac{\text{th. count ratio.}}{\sqrt{\text{th. count ratio.}}}$

# Notes

Well, this looks like the last <sup>unsolved</sup> problem for a while!!.

I Trouble is, it seems to solve a B.G. problem, which I know to have no such simple soln! i.e. the Mexican Gold coin problem.

Anyway, if an event can happen in one of 2 ways, and its prob. can be anywhere betw. 0 and 1, and it happens in ~~ways~~ in the first way n times in succession, what is the prob., it will happen the same way on P<sub>n+1</sub> time?

Actually, there is more info. If the apri U is by, then it is lessening more likely that the pgnm will not have a counter case at all!

It must be noted that ~~is~~ in Math T.M. P<sub>n</sub>, ~~distribution~~ probty. distrib. of Uaprip is not uniform or smooth, since it has a big bump at zero. There is some q. about whether one shouldn't give pgnms U > 0 if they have "lasted" for a long time - i.e. remained "consistent" for a long time.

→ If one uses uniform aprip betw. 0 and 1, then using "Laplace's rule", P. "Expected value" of the probty. is

$$\frac{1}{2+n}$$

To use the Uaprip, one might want to

use  $\frac{\alpha}{\beta+n}$ , where where  $\alpha$  and  $\beta$  depend upon Uaprip.

To get  $\alpha$  and  $\beta$ : Find out the expected life of any pgnm as a function of ~~its~~ its Uaprip.

Another poss. that seems non-ad-hoc. Take the pgnm that is the meet of A and B. If A and B have much U, then their meet will have much ~~the~~ Uaprip.

It may be that this looks ad-hoc, ~~then~~ - particularly if one didn't try to form the meet of A and B until an unruly member of this class appeared. Actually, this ~~is~~ O.K. One could assume that all "such" meets are made, whether cases of them occurs or not, but that this "making the class after the case occurs", is done as an economy

distrib.  
of U  
not  
posssn

Wed July 25, 1956

(Notes)

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measure - economy of both time and memory

General Principle: Any / apparently ad-hoc method may be used, providing it is shown to be a time or memory economy specific measure, rather than purely a problem solving device.

That the above problem of "counter overlap" between A and B that has been discussed above, is unimportant: In General, there will be many cases in which T.M. will make very poor predictions - and ~~that~~ it will be apparent to T.M. a priori, that they are expected to be poor. Usually this poorness will be because of small sample. In the present case, this is approximately true. - Any of the prediction refinements I have devised do not ↑ prediction accuracy much in this case. The only ~~use~~ value of them is that they may be useful in designing NMTM.

[SN] Case no. may be  $\geq$  Count in some tag segs. If this is so, then the tag seg. is

probably poor.

Whether  $U_{\text{empirical}} \approx \frac{\text{no. of cases for that page}}{\sum \text{no. of cases}}$  or not

$\frac{\text{no. cases page}}{\sum \text{no. of q. elements}}$  or etc., is irrelevant,

since we only want these  $U_{\text{empirical}}$ 's to compare pages, and the denominators are the same for all pages. However, we would like to choose a denominator for all pages. This ratio tends to remain constant for a given page.  $\Rightarrow$  probably  $\leq$  no. of cases / would be best. i.e.  $\leq$  no. of  $\square$ 's.

# Notes

$$\begin{array}{r}
 1.097 = 18 \ 10 \\
 \hline
 1.176 = 18 \ 12.5 \\
 \hline
 1.243 = 18 \ 15 \\
 \hline
 1.301 = 18 \ 17.5 \\
 \hline
 & = 18 \ 20
 \end{array}$$

(3)

## Organization of Report:

- 1) Contents : With adequate descriptions of each section.
- 2) Introduction : a) Explanation that this is a prelim. report, that several terms used will probably be soon eliminated or revised. b) That <sup>the operation of</sup> T.M. is meant to correspond to methods by which humans solve probs. That correspondence will be drawn in a latter section (perhaps this) should come here)
- 3) General description of operation. Examine this carefully, so that no wrong ideas are gotten by reader. Note to reader that section on intuitive corresp. may now be read - or preferably after definitions.
- 4) Definitions
- 5) Operation :
  - a) How new pugns, noms, strs, ntps are formed from old. How U's are determined.
  - b) How U of pugns are computed from Uapip and empirical data
  - c) How U apip for pugns is computed.
  - d) How U's of noms, strs, ntps are computed.
- 6) Examples of operation: How ~~deals~~ T.M. deals with  $\mathbb{R}$ .  
~~tug. sequence~~  $=, \sim, \oplus, \otimes, +, -$ . complementation (?)
- 7) How one mathematician uses ~~language in~~ ordinary language in induction.  
 How pugns, noms, ntps and strs. correspond to objects in intuitive induction.
- 8) Criterion of effectiveness of present program
- 9) What next ~~on~~ program : + without carry, what Mult, divide, linear notation, algebra. .... Language : simple Q's and A's about Math, then <sup>perhaps</sup> about other things. - That there is some reason to believe T.M. will not be able to ans. q's about  $\mathbb{R}$ . real world, unless it has a very different kind of input (e.g. continuous)
- 10) Use of same tug. sequence on children.