

of 166. One imp idea is that I have (via MCT) many modes of lrng possl., So I can take an advanced part of a TSO, - decide what into it needs to precede it, then get that into TM - in any of a variety of ways.

Re: "T. Discovery of t. laws of Algebra" This turned out to be diff. Perhaps it is because t. laws of Alg. were invented rather than "discovered"? No! T. operations of Alg. were defined before t. Laws were dec'd. I think t. discovery was that (perhaps) that t. laws could be extrapolated to Literals.

A nice way to do a TSO: First write an ordered list of problems & concs I want TM to know. Then devise a machine that can "do" that list. Each part of t. list can be done in t. most convenient way - or attempts to do it via lrng. Then I began to replace "expert-system-like" parts w. true lrng. As part of t. list, I do include imp. concs. So even after TM has acquired t. info in a rather ff. way, it can learn rather well

Our TSO direction ANL conc. of "Quantity" & Sample linear eq. soln. To solve: More diff. in untangling equs in 1 var. 2 linear equs in 2 vars, 3 equs in 3 vars, also any quadratic, cubic, quartic equations. Plus single heuristic. Also, very complicated equs in 1 or 2 vars. But we solve

24 So, Get Q<sub>2</sub> <sup>(Roman?)</sup> meaning clear: lots of disparate examples: → Also Note: 173, 10-16  
Q<sub>2</sub>(3) = 3? answer 3. ; Q<sub>2</sub>(7+5) = 12

26 If x=3 Then Q<sub>2</sub>(x)=3. Note 2 meanings of ff, Then:  
1) 26L 2) If x=3 Then y=4+1 : Give them diff. notations  
Q<sub>2</sub>(3x(7+3)) = 33 : Learn about paren. Also how related to stack.

(Then) If x+3=5 Then x = 5-3 = 2. (Chain of simple ops).  
If (x+3)x5 = 50 Then x =  $\frac{50}{5} - 3 = 7$  (more complex equs)

Laws of Alg? If x=y AND y=z Then x=z  
How to teach this. Meanings of AND, OR, NOT.

37 If x=3 Then Not x=6 ; If x=3 AND y=7 Then x+y = 3+7 = 10 → 168.21

→ 24 - 37 should keep me busy for quite a while!  
{ common notation = is <sup>assignment</sup> and == <sup>equality</sup> }

So first write t. TSO, (perhaps teddy how many examples of each kind of prob.) What I want here is an instructive idea of what t. TSO is supposed to convey.

Next, do a detailed descr. of what each concept means. Its properties,  
 — The meaning of any expressn. containing it.

.02 To deal w. roundoff error! for ~~linear~~ linear eqs usually, use for rational fractions  
 instead of floating pt. (values of integers). TM has builtin routine for  
 removing common factors of Numerator<sup>or</sup> denominator.

.05 — But this will not work for irrationals. — So may use idea of approximate equality. → (.18)

.07 "Discovery of Laws of Alg." was diff to formulate for TM because ~~with~~  
 w. large nos. had so little cc for it. We can, hvr, reproduce condition of  
 Human discovering l. laws, by ad-hock making cc of ~~with~~  $\gg$  cc of  
 simple logic of l. laws of Alg."

.12 For Humans, large cc of ~~with~~ of large nos. was Heuristic! — We have

.13 to simulate this heuristic for TM! But may be no need! → (.23)

An analogous situation: Euclyz ~~is~~ "impt heuristic" "state  $\epsilon$  problem  
 exactly": For TM, this can't be done.  $\epsilon$  problem is ~~not~~ noted exactly & really!  
 For TM to know is to "state  $\epsilon$  problem in its ~~own~~ original form,  
 in which ~~the~~ associations w. other ideas are expressed in ~~its~~  
 form of  $\epsilon$  state output.

.18 (.05) Re: .02, .05! At an advanced state we can let TM use floating pt.  $\hat{=}$  "digital"

.19 that if 2 nos are very close they are "probably equal". → (.33)

.21: 167.34: An additional concept "Truth": ~~True~~  $T(3=33/11) = 1$  (true)

.22  $T(3=5) = 0$  (false). → (.36)

.23 (.13) If we use floating pt. in 486 or Pentium, ~~with~~ takes  $\sim 100$  times longer  
 simple logical reasoning! Hvr, it might be well to simulate Mult & Div  
 taking much longer than Add, & subtract: In floating pt, they take about  
 same time: If we don't do floating pt, Add, & subtract are as fast as  
Logical statements, but Mult/div takes longer.

If +, - takes  $\gg$  longer as logic, then ~~3+7=7+3~~  
 $x+y = y+x$  would not be discovered.

Hvr, in SAARB, I found a way for TM to Discover laws of Alg, because

.31 they were useful in solving equations. This is a somewhat different

.32 path from Human Discovery of l. laws.

.33: (.19): Well, in most cases, if we use floating pt and  $(A-B) < \frac{10^{-n}}{A}$ , then  $A=B$ .

will work  $\hat{=}$  (most always): For each power errors use double precision  $\hat{=}$  smaller threshold.

.35 (.332)  $\hat{=}$  probably good enuf for ~~most~~ early works.

.36 (.22) The 167.24-.34 would be an Alg. (perhaps w. True( ) added)

for me to begin to teach English, it would be easy to ~~extend~~ extend that algebra

.38 in many ways: eqs, drs, cubic quozes;  $e^x$ , ln x, complex nos, trig, and h trig.

$\hat{=}$  trig is really proving. A/O several ques in several units (linear/non-linear; Matrices, Vectors, etc.)

Anyway; for time being, assume that I can deal w. Equality (168.02=06, 187.19, 33=35) and assignments of arby cc. to various Arith. Operations (168.07=13; 23=32)

103 [ I want to avoid that much detail, at this pt, in my Analysis ] → 180.24

OK. So start TSP.

Def: "Q" mean "Q" mean "Quantity of" or "evaluation of". Normally it is a number: (real or complex); Whether I want it to be able to be true, false or a string (that might be the output of an algm) is not at present, clear.

So Q(4) = 4 ∴ 4 is correct reply to "Q(4)=?"

Initially TM knows ~~numbers~~ v.s. non-numbers (≡ strings).

Def: Q(4) = 4 has 6 symbols; 2 are nos, 4 are non-nos. Hence term "=" means logical equality. "←" is an assignment statement.

Q(4+5) = 20, Q(5\*8) = 40, Q(9-3) = 6, Q(7÷3) = 2.3, etc.

We may want to teach one operation at a time or a mix.

w. TM Q(4+5) = 20 TM learns ~~Q(4+5) = ?~~ has encoder # 4, 5, add. This is observed by taking 2 numbers in

"Q(4+5) = " and adding them. The rest of the symbols are irrelevant.

Then Q(8-2) = 6 ... Q(4-7) = ? TM says "11" since 4+7=11,

This is, hvr, wrong. After Q(8-2)=6, hvr, it's clear that simply adding the nos. in "Q(8-2) = " will not always work. After a few examples of " or one example of high precision, TM finds that Q(8-2) = gives

10 ~~the~~ a fraction of time and 6 another fraction. This is the best model, until we do more search and find whether it's "8, 2 sum or 8, 2 sub depends on whether a "+" or "-" occurred in the data of the corpus.

(The mechanics of this decision is as yet, undecided/inclined).

After Q(8+2) is learned w. 100% accuracy (very short code)

Let's try Q(8\*2) = 16 & note: 2nd time TM looks at the codes representing "-", "+", "\*"; If "\*" is most similar to the code, it will give hvr

pc to ~~8\*2~~ 8\*2, sub into 8\*2, add. (hvr, as more examples of "\*" (20 more precision), TM looks for a better code and finds that the symbol \* makes 8, 2 mult. the correct response.

Similarly, it finally has ~~Q(8/2) = 4~~.

32 One thing is unclear: Just how much cc TM spends on these searches.

After being five Q(8+2), Q(7-3) cod., it could stay with 50% accuracy.

Perhaps I can arby give it a threshold of p = .9 or .1; or p = .99 or .01 for its productions.

T. .99, .01 can be obtained without (igger & 2, or more precision (no. of bits) → 171.34

36 m examples of corpus. This seems to solve it for Algebra is much of Math! → 170.01

37:108.12 [SM] Cheapness of Ram & disc storage makes for a very low heuristic for sparse

text. Compression techniques. Cheapness of high speed computers is very heuristic

for learning efficient use of machines.

(37) Negative Case Counts

(06) TSO's: <sup>possi.</sup> Extensions of them

.01: 172.37 "one-way" connection from A to B could be a ckt. w. A as input, these "drives" B in a way that a cap of size C would drive B from A. If simulator 1. cap acting from B to A, we would need another ckt of this kind. The value, 'C' of the cap. is a voltage input 00f.

.05 Simulating ckt.  
.06: 172.17: <sup>173.10</sup> 167.24 - .34 is initial **TSQ** Some other relevant values, <sup>extensions</sup> additions:  
167.34 - 168.05, 18-19, 33-34 || 168.07 || 168.21-22  
.08 Extensions: 168.36 - 169.03, 190.24, 190.5

.10: 167.24 Another possi part of early TSO!  
~~3=3~~ ; 3=? ; x=3 ; x=? ; 3=? [ y=x, x=3, y=3 | y=x, x=7, y=?

.12 Would it quickly learn x=y, z=y, w=z, x=? ; w=? i.e. a long string of equalities. [ Advanced Algebra <sup>23, n unknowns</sup> ] <sup>know</sup> quadratic equations, ex. dx, complex nos, trig identity proving,  $\rightarrow$  (180.34)  
Also I may want to introduce <sup>for real</sup> "If, Then/notation. (not control of Pen)

What is another good name for it? ~~Imp~~ Cond imp.  
.10 Condition, implies. Cond, Imp. / Cond means "for this problem only".  
Goal Hvr, just what is for "this problem only." How much can be ~~transferred~~ (learned) to other situations?

A real possy: That Ordinary (human) induction ~~is~~ (even in a pure math setting) involves very many assumptions (i.e. "Common Sense"). While it may be quite important & very pervasive, it may be possi. to list the assumptions made.  
e.g. in cond  $x=3$  ~~imp~~,  $y=x$  imp  $y=3$

We carry  $x=3, y=x$  into ~~the~~ imp side of the cond, imp. —  
[ ~~But we do not carry~~ ] we then want TM to carry the transitivity of =, that was found here, into future problems, but not carry  $x=3, y=x$  etc into future probs.  
How serious a problem is this? It will be clear "By induction" i.e.

.28 Learn from t (examples) alone, <sup>(or inducible)</sup>  $\rightarrow$  174.04  
Each induction problem has to be defined either by EB or by compression Expected. — Otherwise TM doesn't know when to stop searching.

On OSL: A very common use of OSL is in Heuristics — someone successfully worked a problem a certain way in the past. This is about 6. same as "Case Based <sup>(Learning)</sup> Reasoning". The practical aspect is predicting events/processes, so they can be retrieved for (C BR / OSL)

.37 (SN) Du Negative SSZ: using b. D.F.  $p^A (1-p)^B$  as approx.  
is eqnt to SSZ of A+B: This D.F. w.  $A \circ / \circ B < \phi$  could be meaningful. It would mean calculation of PC  $\neq \phi \neq 0 \neq 1$  (Not unusual: Particularly in Mod).  $\rightarrow$  174.01

01:178 to Another kind of "hint": Hard or soft (i.e. prohibitive) restrictions on set of concs  
a/o methods of combination of concs used to solve a problem. An extreme  
case would restrict TM to search for a known (to teacher) soln.

In general the value of TM's such for a soln. to TM, is reduced  
(sometimes considerably) by t. giving of "Hints" - so when  
we give hints, we should try to minimize this bad aspect  
of the hints.

Also poss. Sdn. is MAD (Mutually Assured Destruction). Each opponent  
is unsure that he can completely destroy all all adversaries, so it he tries &  
fails, the remains of the Adversary(s) will try to destroy him. - In this case,  
best concentrate on defense & development of more powerful weapons  
(weapons) (defence/attack) & (offence/defence) race (arms/defence) race.

Mrs. Whitten  
Perris  
CIA  
copy  
to "CIA".

A search is "Of Value" if (1) It discovers new heuristics/concs. (2) or it  
changes params of old concs. (3) Discovery of Solns to probs that are different  
from those obtained when Hint(s) were used. (This is maybe a subset of (1))

- .17 "Am. Junkies" I don't expect ~~search~~ searching will be at all "interesting";
- .18 TM will simply find concs that are composition of other concs, Later, I  
expect that TM will watch (another person) work a problem & induce  
(by OSL or ~~concrete~~ Multishot (ing) ) a way to do a search on a  
set of rules or heuristics for ~~prob~~ solving probs of that type.

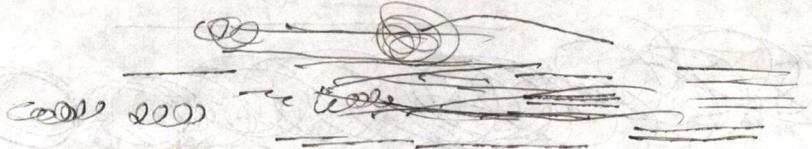
Big Complaints I had about the TSO's design at SAARB!

- .22 1) Had to write (MCT is supposed to fix that!) (3) It was beginning to be a "badly  
pe's of concs. was getting too small  
as TM had more & more  
of organization on  
TM's part"
- 2) It only found concs that were solving to problems in the TSO.  
This second complaint is (partly at least) dealt w. in (.17). I need more  
complex probs before I begin to notice useful sub-procs in solns.  
also I need more complex probs before TM begins to discover  
stuff like .18 - 20.

A big thing will be for TM to discover Ramanujan's "education" George Shookbridge Carr  
total 176  
what a "Proof" is  
or just proof out!  
And, of course, if TM could usefully go thru Carr's book(s), it would be a major

Break thro.  
List of Recent TSO refs: 172.09 - 27; 172.27 - 40  
174.30 - 40; 173.10 - 16; 173.06 - 08  
176.21 is how TM works  
involves advanced search  
gives refs from 167.24 to 169.03  
character operator  
U.S. Standard set  
of finite c's, etc

From .37 I should make list of (conc, example sets) and  
try to order them in a reasonable way. I have been concerned w. f.  
exist. details - thm DONT BE. Just write t. TSO & put  
TM to work on it. TM should be able to work it even if it's not  
exactly right! I may discover some very scarce data. (80.01)



01: 179.40 in t. TSQ's: But 0.4.: Then maybe fix it. ← (But perhaps generalize first — like 0.11 AF)  
02: Also, I want to Address the "scaling" problem (of 179.22 R) ← (A very Serious Problem)

02: Involves finding ways to categorize concs., ways to know when they are likely to be used. I should be able to get ideas about PUs by examining my own workings of the probs. in the TSQ.

06: So make a list of actual problems in 179.37: Hvr, do it on a tabular editor, so I can insert lines. In Rosa notes, write

08: Comments on the Set of Tqs - Examples.

T. Q of Operator v.s. Unordered set of sets seems impl: Penk about it? [ABCDE]

11: Otherwise, just write the TSQ and worry about 0.22, when it occurs.

But when it occurs: Try to get a good perspective of the Problem — "IN ENGLISH" (as best) — But look at it in the most GENERAL Poss. way.

T. way it looks Now: That the details of the TSQ are not very imp. — That is does hvr, have to have the needed info in it. If it does not, PUs will become apparent in the mode of failure of TM's "attempts to predict/track" it.

Hvr, the scaling problem of 0.22 can be serious.

Also note that in order if we run into .16-.17 (need not put into in corpus), the MCT should give us <sup>several</sup> ways to get needed info into the corpus!

24: 169.07 SN on Extending the TSQ!  $x^2, x^{\frac{1}{2}}, x^{\frac{2}{10}}, x^{\text{real}}$   
 $e^{px}$ ;  $\ln x$ ; hyperbolic trig funct. (Laplace x fun?)  
complex nos. ("||" & ("||") (L x fun)

So before I introduce complex nos, hyperbolic trig & Laplace x fun are definable. (Also for Laplace, I need to define Integrals — maybe not — use real analog of Fourier Series.)

Also note: Solns of polynomials can be extended via complex nos. This does not need  $e^x$  or  $\ln x$ . So maybe introduce complex nos before "polynom. soln". Then  $e^x, \ln x$  etc.

34: 173.12 → Q: Could I Get TM to invent Complex nos, etc.? This is in T. direction of the "creative" M. M. (Constr's "Am") → 176.01 (Ramanujan) — I don't think about how TM could invent complex nos: What would be the motivation & how, & how to direct it to the best known way to go complex nos.?  
Any other ways to ideas of a "seru" of a poly, can be extended?

8/10/00 Bulg.

→ anyway I dealt w. my personal "Scaling" problem! When I (run a new, useful conc. (idea & category), I try to think of all the areas of enquiry in which it could be useful. This could be very narrow area or very broad problem area. This process of suggesting application areas ~~is~~ is solvable by Inductive Inference. → Infant TM has not too

.01: 180.90: Re: transcendental functs: There is a nice, fast computer way of calculating them all (I think it's Cordic Method). Another (or perhaps the same) way, generates  $e^x$  by  $e^{x/2} \approx e^x(1+x)$  loss are reduced by expansion of binary nos. Multiplication & division are done by a kind of successive approx used in A to D converters,

Small size for induction in this area — But infant TM doesn't yet have this "scaling" problem → 183.07

.06 More on "Scaling": T. Scaling problem is one aspect of "Too large CJS": In the past, I'd dealt w. this by a pc of concs by factoring them, then make a TSQ to discover the factors & make them a by pc. Hvr, even this technique will fail for "Scaling" reasons —

.10 i.e. if we don't find ways to categorize, to narrow down the search for a conc (i.e. "narrowing down" should be (stochastic) ~~not~~ soft rather than hard. = deterministic)

.13 Hvr, it may be that for a Young TM, there is not enough SSZ for useful categories, to do this.

.14 Note that this "Narrowing Down to Search Space" is one of the commonest types of hours. — But for a young TM, we will probably have to use the needed hours. — because (.13-14) TM will not have enough experience to sort the relevant hours. itself.

.19 So the "Scaling Problem" may be equiv. to "Having Adequate Hours"

An adequate soln. to this scaling problem implies that the CJS of most problems stays about the same as it grows

So start of TSQ: file C:\[redacted] (on Zennith laptop) 167.24-.34 I had idea that the conc. of "Quantity" would be useful.

but I'm not so sure of this now! — It may be that TM could (run these TSQ's "about as well" w.o. that conc. Part of my objection to it was that I don't know exactly how I want to define it.

Qd (3) = 33: Conc X=3 (imp Qd(X)=3 But also "X=3" So I'm not sure what Qd(.) is about! Usually, if not always, if a "Qd(.)" are removed, the expression is still true (a very loose sense) so it looks like it's redundant.

— The redundancy can have hour value, this ~~is~~ seems vacuous! (Pro I'm not really sure).

Anyway: [redacted] 2, m, n are say 32 random bit nos.

.33 HVR: Many of the properties of =, +, - are discoverable by TM, comparatively. T. way I'd considered doing this (most recently) was to have +, -, x, ÷ be very expensive relative to logical reasoning.

In the present case from "TSQ1" TM "learns" laws of Alg but the learning is of a "Skinnerian" kind (small cjs, very little cleverness)

.37 In .33 one way to do this is to have TM try to find ways to do arithmetic "fast". Probably, it would be a good idea to try Boole (.33.37) and e. method of "TSQ1" (191.5)

This will be an ordered list of problems, tasks, definitions, ...

--- toward the construction of an initial TSQ for TM.

167.24-.34

l, m, n are 32 bit random numbers ( <sup>IEEE</sup> or 36 bit reals? ) 0 Basic 32 Bits per sig for prec.  
64 " " double precision.

u, v, x, y, z are variables

":" separates examples. ", " separates data within an example

cond means "conditions for this problem"

imp means "what is implied by these conditions"

n=n e.g. 3=3, 7=7

cond x=n imp n=x

"[" and "]" are "metasymbols" [3+5] means "8"

l+m=[l+m] e.g. 4+5=9 --- learning Addition 4+5=?

[l+m]=l+m e.g. 9=4+5 --- Equality Commutes ? = 4+5

cond x=y imp y=x Equality Commutes

l+m=[m+l] Addition Commutes

x+y=y+x Addition Commutes

x+m=m+x Addition Commutes

l+(m+n)=(l+m)+n Addition is Associative

cond x=m imp x+n=m+n --- if equals are added to equals the sums are equal.

cond x=y, u=v imp x+u=y+v --- as in previous example

l-m=[l-m] learning Subtraction

m-m=0 meaning of Zero

x-x=0

cond x=m imp x-n=m-n -- if equals subtracted from equals, remainders are equal.

Optim Techquest: .08

(205 : row

Also Note Method of such for peak.

.01 In S78 I showed  $n \in \frac{1}{\epsilon} (r_T - p)^2$  was  $< \max \ln \frac{p}{p_T}$   
 $n$  is max value of ratio of

.03 A Q was what about  $E \in (\ln \frac{p}{p_{True}})^2$  ?

.04 Actually, S78T3 proof should  $E \in \ln \frac{p}{p_{True}} < \ln \frac{p}{p_T}$   
which was  $>$  than  $p_{True}$  .01. The .04 is not necessarily (apparently)

.06 comparable to .03, it does suggest that  $\ln \frac{p}{p_T} \rightarrow 0$  rapidly

on ordering of nodes for OT probs.

.08 152.24 On finding peaks of a function; Assume a certain value

.09 for  $\epsilon$ :  $(f(x+\Delta) - f(x))/\Delta < \epsilon$ . (x by  $\Delta$ )

Using this  $\epsilon$  value, do a search w. mesh edge  $\delta$ . Find  $f_{max}$  for that mesh. ~~Because of~~ <sup>.09</sup> certain regions of the mesh, we know can't have pts w.  $f > f_{max}$

.12 Do search w. mesh edge  $\frac{\delta}{2}$ . ~~Over regions of net~~ Over regions of net for which  $f$  could be  $\geq f_{max}$ . This  $\frac{\delta}{2}$  search yields new  $f_{max}$  (maybe  $\geq$  old  $f_{max}$ ) and gives (perhaps) new regions where  $f$  can't be  $\geq f_{max}$ .

To do the search: Make a "linked list" of regions in which  $f \geq f_{max}$  can occur: Each such region has a  $\Delta$  value and 2 end values  $f_1, f_2$ ;

Also, peak poss =  $\max(f_1, f_2) + \frac{1}{2} \Delta \epsilon$ : We elim regions from our linked list when ~~max~~ that becomes  $<$  latest  $f_{max}$  found.

So, we do the whole space until all pts are covered that could have  $f \geq f_{max}$ .

Then we do  $\epsilon \rightarrow 2\epsilon$ , and we redo the whole search.

We then re search for new  $\epsilon$  than  $\epsilon \rightarrow 2\epsilon$  is redone again.  $\uparrow$

.23 This continues until we find no new peaks w.  $\epsilon \rightarrow 2\epsilon$ . .32

.24 MORE GENERALLY: R.E. OT's: An OT is impossible.

over a continuous space unless one makes some constraints on  $G(x)$ .

Otherwise  $G(x)$  can be anything at any point and into about some pts. does not

consist of value at other pts, so no search method is poss. (Other than random or exhaustive <sup>at hand/precise reason</sup> search).

In Approximating Functions / using linear sums of other functions; It is well to know the constraint on  $f(x)$  is design't. "Basis" functions. <sup>Basis</sup> This is true for <sup>for those constraints</sup>

.31 Neural Net approx as well.

.32 : .23 A weaker assumption than  $f(x+\Delta) - f(x) < \Delta \epsilon$ : Constraint on "second derivative" of  $f$ . So if  $\Delta f$  has been large in an adjacent mesh region, we allow

$\Delta f$  to be  $\epsilon \times$  larger than in int. present mesh.

"Second Deriv" may have to be "Second Difference": The details of how to use a "linked list" (or some similar data str.) would have to be worked out.

01: 199.40 This defines  $R_s$   $\equiv \Omega$ . Symbol set that precedes  $S$ .

Next: Define the symbol set that follows  $R_s$  ( $R$  will be a number).

Call it  $T_F$ : So we can make the context product set  $R_s \cap T_F$ .

So, we have folg. ways to create (features) contexts:

- 1) All prim symbols are contexts w. 1 member.
- 2) T. set of symbols (or contexts) that precede or follow a given context.
- 3) The AND/OR of 2 contexts.

Note: These "contexts" are really "BAGS": so its easy to "OR" them but "AND" is not so easy has no obvious Defn. (I wrote about this in the past)

Maybe see notes on G. Wolff.

To define  $\alpha_F$  (i. set of symbols that follow symbol  $a$ ):

we write  $\alpha_F$  better coding to corpus: every time  $a$  occurs, we code it.

following symbols as separate Bernoulli seq. If this method of coding  $\alpha_F$

$\alpha_F$  of corpus, then  $\alpha_F$  is a legit context.

How we define & evaluate  $R_s$  (i. symbol set that precedes  $R_s$  is unclear)

SN I do want to find ways to effectively "undo" part of the Gram. Grammar.

Otherwise, I will simply accumulate errors. Could "Reversing" be of help?

PSG rules are of 2 types only:

$A = C \cap D$
$A \Rightarrow C \cap D \cap E$
$\Rightarrow$ PSG

concatenation of 2 NT's  $T =$  concat of 2 NT's.

NT = Boolean AND of several NT's or of several contexts.

So: A cond could be a small (usually) set of Grammar rules.

A mut/recond could remove grammar rules as well as add or modify them.

A loop  $A \rightarrow C \cap D$  is same as any other Grammar rule.

How. Every loop should have at least one production that is not in that loop!

ex.  $A \Rightarrow A \cap D$  But in general when there are many loops, it's very cumbersome to assure meaningfulness, are complex.

It's not that I want to know rules so I can avoid making trial modifications (conds) that are meaningless.

UNGENERAL! Explain how to obtain a larger

LATER! Road 149.15 - 40, 161.01 ff. when starting on PSG-dizy

I think there are some Good ideas here: some need development how:

I vaguely had that idea, how. But PSG dizy may not be critical to TM or

TM's (traps of language) since it will not (run) cause by looking for ways in

& a large corpus: It will learn by associating English Q's, A's w.

Things it knows about.

1 to	<del>267</del>
141	267
148	268
158	274
<del>159</del>	
159	
162	

01 : 159.40 : 153.01 ..... 157.19 Discusses ways to get Ross 2 kinds of approxs of  $G(x) \approx P(G, K)$

154.01 : On relation of Mutations/Crossover to  $P(G, X)$  &  $G(X)$  approxs.

157.24 - ~~157.24~~ : That 4. Treatment of ~~Optim~~ Peak finding of 152.13 - 156.05 Doesn't do

"Experiments" : How to deal w. Poly ( $\geq 6$  bits).

157.28 - 158.06 Suggests ~~and~~ poss. Genl approach to "EXPERIMENTS" in t. treatment of 152/13 - 156.05

160.01-06 ON Sol 78 ~~TR~~ : How to deal w.  $\approx (\ln \frac{f'}{p})^2$  error criterion !

161.01-40 P S G discovery : (Continued 149.13 - 40)

Review of Reviews. T. pp of reviews: 140, 141, 142 <sup>158</sup> 159, 162.

140 details from 117.21 to ~139.40.

159, 162 " " 142 to 161

141 Discusses several Models for  $G(X)$ . (easy to find  $K \ni G(X)$  is  $\approx$  Max.)

148 Gives an ~~overall~~ view of Motivation : Why this stuff is imp.

158.13 : A repeat of  $\approx$  148 : Perhaps slightly diffrt.

72  
52

Now, I want to outline a final T.M., based on MCT. <sup>(probably)</sup> ~~(perhaps)~~ Lsach.

First a rough outline, then progressively more detail.

T. main idea is to do a T.S. ~~from~~ starting w. Algebra.

Using various techniques to reduce CJS. Mainly lang. definitions by induction: then giving problems in which those defns. are useful.

{ Also, we want TM to be able to devise complex (perhaps recursive) concepts to solve problems. { look at Koza's ~~ideas~~ methods for some ideas on how to do this - (if it isn't obvious!) }

After TM understands some Algebra, begin teaching English, by asking Q's in English & expecting answers (in ~~TM's~~ TM's normal mode of ~~first~~, but later, in English). See how far we can go w. this.

See if TM can work hard probs (eventually). Since Koza seems to be able to work hard probs, using a rather unsophisticated such system (i.e. it doesn't learn hours to guide such), I think that it should be able to do far better.

.16

A VERY IMPT. fundamental idea: That I want TM to learn things the way I think humans do. — So if there's some reasonable, good, way to solve a problem, perhaps using ~~the~~ hours based on ~~the~~ experiences of TM w/ to the Scientific Community — I want TM to learn to use those hours. — ideally it should learn them from its own experience — but if the CJS is too large, I will give it "hints" to do CJS.

— The default "hint" is to be ~~the~~ "opening" TM is arranging for it to "discover" the desired conc. I will probably be giving lots of "hints", but I expect that eventually TM will be able to discover some serious, large CJS concs, "on its own".

At first, TM will solve all induction problems by simple Lsach. Hrs, as TM matures, it should be able to do "proofs" & "finding solns" that it does by inducing from examples. This induction is done by Lsach, then the Algs (found by Lsach) are used to solve the problems.

— A simple case would be soln. of linear eqns. — or perhaps numerical &/o literal evaln. of an alg. expressn.

→ Perhaps look at latest version of the "Paul-Solomonoff" paper for some useful ideas.

Re: Alg Notation Lang: A new idea was to teach the idea of "quantity" — which makes ALN a lot easier, & it's a conc. that is very useful later.

perhaps Review Sach Notes.

ANOTHER impt idea: Be sure to RETAIN PERSPECTIVE. Don't get bogged down in picky details. Keep discussn. in BROAD, "English" terms as long as possl.

# GA

uuuu  
uuuu

Evolutionary  
Computing

01:162 to On Speeding up GA: Paper in Recent ~~IEEE~~ <sup>Evolutionary Computing</sup> on E.C. July 2000 p. 188  
Uses "Momentum" concept from Back Prop in ANN. to speed up GA such: In the cases they report "The speed ups enormous, — but of course they present only the cases

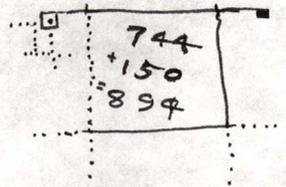
where it worked. Still it would seem like a G.Y. idea. P.09  
They suggest that derivatives from Back prop. be used for GA. ~~P.09~~  
Perhaps partial derivative idea?

Poggio wrote a paper showing how ANN, radial Basis functions, fuzzy (logic controllers) were all very similar. Also paper by Farmor(?) on similar theme.

09: 04 Re: "Momentum" This is essentially a derivative of G. They multiply it by a constant,  $\mu$ , to obtain next jump size. The constant  $\mu$  is chosen by user. If they had second derivatives they could do optimum jump. Hvr. second derivative are very noisy. One has to pool data to ↓ noise: 3 kinds of "pooling" ① Over time of same vector components of  $\vec{x}$  ( $\vec{x}$  is the desc of t. cand) ② over different components of  $\vec{x}$ , ③ Betw.  $\vec{x}$  components in ~~with~~ nearby or more distant regions of  $\vec{x}$  space. (We are doing a STEIN analysis).

Also Two books on GA Theory: ~~One~~ <sup>One reviewed in recent</sup> ~~IEEE~~ <sup>IEEE</sup> ~~Trans on Evol. Comp.~~ <sup>Trans on Evol. Comp.</sup> ~~Other (by reviewer) was referred to.~~ <sup>Other (by reviewer) was referred to.</sup>  
Also look at a book that <sup>called</sup> "Searching W. Probabilities" Andrew J. PALAY 1985  
↳ This uses Chess as Example Source of Problems.

① Michael D. VOSE  
M.D. VOSE  
② Hans-Georg Beyer  
Beyer | Springer V.  
2000



164 is a  
 "Speeding up GA"  
 see earlier Bulg files

.01: 163.40 E.G.: I want TM to learn meanings of various <sup>(Terms)</sup> definitions in Algebra. In many cases, exact definitions of what I want, are quite diff. ("Set" is a good example: even "set of numbers") In these cases, I could just use ruff definitions; give some reasonable examples, w.o. my really understanding how to complete defn. could be understood by T.M.

So: TM would at first have very narrow ideas of what a "set" was, & would later have to "Generalize" this concept. T. simplest way to Genz. is to remove constraints; but this is certainly not the only way.

.11 I might just give a few examples of a concept, then see how T.M. has done on it by asking about new ~~cases~~ cases. — Then I could see if it (T.M.) made any errors in the concept. This could go back and forth w. errors by TM. Hrrr, if it does go "back & forth" many times, I'm afraid of getting close to "Skinnerian lingo" — w. T.M. ending up w. a long defn. w. many special cases.

.15 What To do: I do the "Bad" lingo of .11-.15: This teaches me how my examples are inadequate. I then mind-wipe TM of that part of the TSO (if this is poss!) — Tho I could store TM's mind before I do this section of TSO. — So easy to erase subset. ~~██████████~~ "Maltroy". ← ("Mal-troying"?)

I want to keep ~~my~~ my defns "in English" so they are as "rigid" (≡ general) as poss. In the case of "Set", it's <sup>maybe</sup> hard to define it w.o. using the concept itself! — So maybe it's a "Primitive concept". So — if I run into trouble deriving an "ENGLISH" definition, Consider the possy that it may be a Primitive concept!

Another Impt. idea is that I needn't be very careful about introducing concepts that may have to be discarded or grossly modified later. TM should be able to deal w. this, & not "get stuck" somewhere by "Painting itself into a Corner" ☹.

.32 So what are some preliminary concepts/defns? — What are some preliminary probs?

first: Quantity:  $\equiv Q_0(3) = 3$  or  $Q_0(3) = 3$   
 $Q_2(3 \times 7) = 21$ .

If  $x = 3$  Then  $Q_2(x) = 3$ . The If, Then idea

The If gives a scope & universe. "Then" gives some conclusions about it.

The idea of parentheses. Also ideas of a "Stack" T.M. should im to 166.01

~~Stack~~ stack STACK THE PRIME HEURISTIC

21

01:165.40 relate a stack to parenthesis.

If  $x=3$  Then  $4 \times x = 12$

If  $5 \times x = 12$  then  $x = 12 \div 5$ .

Perhaps just try teaching numbers, + (and perhaps -) Then,

~~12~~  $Q_2(3)$  is 3. If  $x=3$  then  $Q_2(x)=3$

Plan eventually: If  $x+1=5$  then  $x=5-1=4$ .

07 Maybe use "=?" as way to ask Question. This is a reasonable induction Question form.

So list some Con Concs I'd want TM to recognize;

Some kinds of Behavior: kinds of Inging.

$Q_2$ : The idea of Quantity or "evaluation" I'm not entirely sure what I mean!

The idea of Parenthesis: a perhaps related stack. This could be very imp! Very useful in ordering tasks.

165.32 - 166.07.

~~Ability~~ Ability to solve simple equs, then more complex equs. After equs w. +, - are solved, x, + are introduced more complex equs are solved.

Another trick: TM learns to solve  $x+3=7$ ;

Then we teach mult, div. & so on if it learns to solve ~~12~~.

$x+3=7$  faster. Then it had to solve  $x+3=7$ . The  $Q$  is: does it recognize the similarity? (A variety of "(shot long)")

21 The PRIME HEURISTIC: "All the info is in p.d.  $\leftrightarrow$  such is the best way to solve the problem"

Apparent Exceptions (like Quick <sup>off</sup> abort) can be dealt w. by properly defining the problem. In this case, one redefines the problem to be ~~part~~ to cc solve of problems (not necessarily max  $\frac{pc}{cc}$ ).

MCT makes it relatively easy to put any kind of info into the P.D.

Hm, Note that Most INV probs. are solved as OS probs. amount.

27 Perhaps: First write fair amount of ruff & s.c. Do this before working out any "details". Start like 165.32 ff, but more "complex" something close to what I expect to feed to TM.

For 27 ff: In later (or even perhaps earlier) sections of the TSCQ, Tell just what Hours are expected to be used (if any!).

Look at those 3 or 4 TSCQ's I worked on in SAARB: To what extent can I use them or (parts of/ extrapolate) them?

Promising Approach: Write TSCQ's for an Advanced TM, first. Then work backward to get to Primitive Concs. & use many "Hints" to & CJS of ~~Advanced~~ Solns. to "Advanced" Problems.

Sol 89 had some reasonable ideas about TSCQ's: perhaps reread it. I had different Phases of the expected TSCQ - culminating in Ability to read/understand English text books.

.01: 169,36! So, next,  $Q(3*(4+2)) = 18$ .

✓ "feel"

The idea of introducing  $Q()$  notation was to ~~give TM~~ a "feel" for "Quantity" — but my guess is that ex. examples up to this point, would not do that, is so it. concept of "Quantity" would not yet be used as a noun in .01

So try this: "If  $x=3$  then  $Q(x)=3$ ."

If  $x=Q(5)$  then  $x=5$

Q: Do I want to give occasional negative cases? A neg case means that code should not give by pc for those examples. — T. idea of neg cases may have arisen whenever we are fitting "concepts" (in Valiant's sense) to data. Winston used it in his "Arch" v.s. "not an Arch" paper. Also Grammer to Corp.

↳ neg case example is unconvincing for pure Math. A neg. example is

possible case of "Not (a concept)". Pos & Neg cases have interesting property with

Maybe partly too complicated

well:  $T(Q(7,7)=1) = \text{false}$  (Truth of  $(Q(7,7)=1)$  is "false".)

172,03 Maybe getting too complicated!

$4 * Q(4+5) = 36$  : So Actually "Q" acts like parentheses.

in (.15 L) — omitting +. Q would give correct expression.

What I've been trying to do is get TM to understand what a "Quantity" is:

We: say  $x=3+5$  what this really means is that  $Q(x) = Q(3+5)$

so:  $x$  is a symbol:  $Q(x)$  is its "value" "3+5" is a symbol.  $Q(3+5)$ , its value.

Would things be easier in RPN? T. system is certainly less so. Then normal Alg. notation.

↳ An advanced problem would be for TM to learn to XIT from RPN to normal Alg to Polish notations.

Remember: T. pt. of all of this was to reduce to CJS — (=  $\frac{CJ}{P} = \text{Least}^{-1}$ ) of learning Alg. notation. I felt that Quantity was an imp. conc. that

was more generally useful: — say in explaining to TM what

"solving an eq." means. — And this is why I want to "go over" a large part of CJSQ, to see when certain cases are important in many phases of  $4+5Q$

.32 Perhaps "Built-in" concept: T. idea of "localization" = Soluble subnet

Another possy is that idea of "Quantity" is ~~to~~ inherently difficult to teach.

— ~~Problems~~ So — .32 — need to "build it in" somehow.

Or, I could just write out the soln. that I want TM to require it go on from there. — In fact, it would be well for me to write a P.S. Q., write a series of like TM to acquire, then look at CJS's invariants, then see what I can do to reduce them.

What I much want is the CJS that seeing Small to a human,

is also **Smalltalk** TM.

Thy it could be that reason certain CJS's are small for a Human is that ~~he has other~~ Inst instances that are not immediately apparent.

Re: ANL: Say I use RPN or ~~or~~ / cons: notation w. Parans.

(like LTSP): If TM learns  $+(3,4)$ ,  $*(7,5)$  etc, then I.

~~the~~ ideas that sort of parts of strings ~~are~~ (sub-execs) that have been much used in the past, have high pc for future use. This might be an adequate user for ANL. That is, idea of "quantity" into ~~the~~ same as I.

"idea of" sub-tree. — which will (probably) be a built-in heuristic.

**SN** If I use 1 example w. hy res. v.s. many examples

at low rate, ~~the~~ pc of ~~the~~ needed ~~concept~~ will ~~end up~~ the same.

~~But~~ The pc of discovery of the conc will be the same ... but for combining w. other concs: — T. fact that a given conc. has used many times in the past (even at ~~low~~ low ~~rate~~ rate ~~examples~~ examples) is important — it would seem to give it higher pc v.s. use w. 1 hy res ~~example~~

Exp. ~~example~~ in the past.

Actually ~~the~~ ANL can be expressed as a stack operator.

$f(4,3) \rightarrow$  add 4,3. ; fact (the mechanism of Plus is unclear!)

Anyway, after it acquires the operators for  $+(4,3)$ , it will be able to require f. op for combinations by combining sub-operators. ~~is~~

It may be that in my Sub approach, I used a common "Memory" for concs, so I did not really ever learn proper pc's —

— In particular I didn't give them Conditional pcs (which functioned so as to narrow down their expected applicability ~~to~~ to ~~the~~ the ~~pc's~~ pc's in a gn. applic. (v to idea of "directives")

Hvr., I'd like to avoid that much detail — but I do wanted ~~to~~ some to get pc's of the conc rate, so they ~~are~~ indeed much warp (likely to be used as parts for candidate concs.

→ 1:169.35 1) On the mean 10% or 1% pc of error at 169.32 - .36 ; In general, our ability to get % certainty in prodn. will depend on SSZ of examples used for how conc.

39 2) In discovery new concs: A (Human-type) "soln" is not complete until I have some way to narrow down the concs that were used ~~in~~ in the new conc and conc. This can (perhaps usually will) involve categorization of concs, and for each category, conditions in which it is likely to be relevant. This (category/condition) ~~set~~ set will be a heuristic and will operate in a Bernoulli seq - (like human). → The utility of a (ie. the way I code a Bern Seq.)

11 also see 171.34

.01: 171.40 Most of this kind will depend on its efficacy in pct of past

.02 Solns. of induction problems → .11

.03: 170.12: Part ~~of~~ any thing must be one or the other but not both. These are

"Category" cones — the kind defined by Computational Logic Theory ( ).  
Now These cones are e.g. Number, v.s. not number, even v.s. odd not even, etc.

[ If I use, here, normally, a more General defn. of a cone. It is a tree or subtree. It is a part or whole of a computer prog. It is a string of op-codes.

Give special names to cones. This pertains to universe in eoz parts

Def I like this: Call them P-cones. (PARTITIONING cones) — They write do ≥ 2 partitions. [ A "P cone" may correspond to an "OB" ] <sup>off. ob. of Algebra.</sup>

.11: .02 → So: Re hours: # I want to first design TSQ, & I have for each problem not a Human heuristic soln. — So it seems reasonable that a Human could make a nice epistemological jump — so it seems like to CJS for Humans is acceptable/reasonable. Then I have to problem of converting (apparent) human hours into TM-type hours. If I have trouble w. this, it is clear that I don't completely understand

.12 6. Human-hour! → 173.06

Put back to this as one of work on GA

.19: 164.40 SN On GA: Design of filters/electronic chks could be much speeded up by using RW components ~~with~~ ( not RW chks) for Cands.

This is because (A) Spice is very slow (B) RW can implement things Spice wouldn't be able to think of. Putting components together could be done by retrays at scaled-down speeds. For faster trials, we would have to find electronic ways to simulate hoza's trials.

(NB) At present, there is research effort to design <sup>devices</sup> components that can easily be switched from ~~being~~ being a computer say to a fm radio, to a GPS station, etc. — find out how this works — it would be great for GA work!

Another idea in this ~~from~~ GA is use of Analog signals on digital components & GA's w. analog output but digital switching.

Another posy is to use GA for Analog inputs as well as digital inputs to circuits.

It might be expensive to have Variable LCR, & in chks, but we can make analog chks that convert from voltage to L, C, R. ~~App~~ connecting a C, say, of such a type betw. 2 pts, can be not so easy!

.37 — Maybe not so diff! Say we want a cap betw. A & B. → 173.01

.01: 173.40: Hvr, if  $A \in \phi$  then  $A \rightarrow A+1$  will  $\left[ \frac{p^{A+1}}{p^A} = P \right]$   
 $\downarrow$  pc of  $p^A (1-p)B$  which is weird

Hvr, its true even if  $A > \phi$ ! Perhaps its ugly to Norme.

.04: 173.28: 173.10-.28 seems to be a real ditty - in the sense that I will often have an induction problem in mind, so I think I know what the  $\phi$ , & I know what answer I want - But in fact, I really haven't factored out just what the constraints on the problem are.

This is like the "Robot's Dilemma": T "FRAME ~~PROB~~ Problem A.I."

When Given a new problem in a sequence, the Robot doesn't know what features have changed & what ones have remained the same.

In 173.10-.28 the Q is: "Just what are the constraints in each new problem?" It may be that this can be answered by a more **GLOBAL Induction**. - But "an analogy" there isn't much copos to make "Global Induction" on. - So I have to be careful starting out:

Poss. troubles: ① I don't put in v. constraints so it fails:

② I inadvertently put in extra info, so it works, but it contains seeds of future failure.

Another Way to write (Human-ish) TSQ's: For each problem, separate

write the necessary info needed as well as the search procedure.

A prime ditty, it may be that we will not have any idea of how many & what assoc. pc's, resources for the other (not "correct") concs, so we can't have estimates for

Cost of the expected "soln."  $\rightarrow$  On the other hand, we could make as part of the "problem soln" various hints to the pc's (for that particular problem) of the concs used in the soln. - This last is certainly an important part of the soln. of any largish problem.

$\rightarrow$  Hvr, even w. (2+5) .20-21 could be a useful way to organize a tsq.

Some small TNG Tasks:

1) Equality:  $3=3$ ; ~~cond  $3=3$  imp  $3=3$~~ ; ~~cond  $3=3$  imp  $2=9$  low pc.~~

$3=3$  hyps  $3=4$  low pc  
 $\rightarrow$  See 178.09 for disj.

2) Intro of cond, imp formalism:  $\text{cond } (3=x) \text{ imp } (3=x)$   $\leftarrow$  "Cond, imp" Defn

$\text{cond } X=3, y=x \text{ imp } y=3$  } other problems involving transitivity of "=" }

3)  $3+4=7$  ||  $\text{cond } X=3 \text{ imp } X+4=7$

4)  $4-1=3$  ||  $(\text{cond } X+3=8 \text{ imp } X=8-3)$   $\leftarrow$  Downward move TNG before this?

if  $\text{cond } X=3+4 \text{ imp } X$   $3-3=\phi$   $3+\phi=3$ ;  $\phi+3=3 \Rightarrow$

01: 174.40: Poss. Notation used L, M, N are ~~by processing~~ <sup>32 bits say</sup> random sets, = 16  
 — So a single description  $L=L$  is equiv to a complex set  $[L_i = L_i] \text{ } i=1 \dots$

02 For realization of a Turing Alg; TM can take a 2 (for L's states)  
 general terms: ① In one it hunts for <sup>lowest</sup> operators  $\rightarrow$  w. input string "N=?", output will be "N".  
 ② In a second, it tries to find various Nos for "?" that will give <sup>entire</sup> corpus by pc.

06 #2 is, perhaps, a more general soln. for a problem. Usually, #1, the operator form, is insensitive to regularity in the input. ~~part of~~ <sup>one simple</sup> part of a corpus.

For a  $N=N$  corpus, the  $N=?$  problem has soln: Look at input string; find first number: this will be output.

For #2, we find repeats in input: this could be useful for producing long term trends in the types of problems being given. — it could be used to predict types of future problems <sup>that will be</sup> — up to the future limit of the "Horizon". This could help in a long-term optimization of TM's behavior.

What are the MAIN IMMEDIATE PROBLEMS?

- 1) Choice betw. ① & ② Model types in .02-.06
- 2) Choice of what parts of 174.31-.40 to use, to start on
- 3) Fear that Choccam ② would get me "stuck" in an "Non-English Level" Aspect of TM. — That I would be getting "Too Specific" for this phase of TSG writing.

Perhaps for the probs of 174.31-.40. For each problem, write out the kind of behaviour I'd like to be elicited from each ~~new~~ <sup>new</sup> ~~idea~~ <sup>idea</sup> ~~concept~~ <sup>concept</sup> introduced.

In some cases, I don't know just which properties I want to introduce "at the beginning": e.g. Commutativity of Addition? (probably)  
 $x+x = 2x$  (probably note: this involves  $x+x = 1 \cdot x + 1 \cdot x = (1+1)x = 2x$ )  
 If TM learns  $x+x$  this way, will it really be able to "count" objects? Perhaps I could introduce the counting process (later or earlier or in a "separator stream") & then have it somehow register w. the idea of .28R.

For "counting" TM could do " $j \leftarrow j+1$ " every time a new "X object" was found.

Also, I could introduce multiplication via  $3+3 = 2 \times 3$ ,  
 $2 \times 3 + 3 = 4 \times 3$ , etc counting

I want TM to know all these aspects of arithmetic operators.

i.e. to get sum of a bunch of 3's: count the no. of 3's, then 3x the counter no.  
 For this trick to succeed CC, "adding 1" must have  $\ll \ll$  than "adding 3".  
 We can use "adding N" where N is base binary no.

.21 HOW TM CODES NEW DATA  
(Steady State Learning)

Ramanujan!

Synopsis of Elementary Results in Pure and Applied Mathematics, 2 vols (1880-1886) 6,000 items upto 1860  
By George Shookbridge Carr (Maybo Camb. Univ Press)

On the other hand perhaps TM (as a Corpus) should

get a lot of emotional excitement from discovering their facts, rules, laws about Arithmetic. - A Ramanujan-like goal! Srinivasa Ramanujan 1887-1920

Evaluating the values of those "discoveries" is difficult:

Leont's "AM" did it, hr., in a not unreasonable way). It's even.

rules for "interestingness" it had hours for developing them.

A TM w. very low TSC would itself discover heuristic rules for telling whether a conc. was "interesting" or not. For 2.0 instant TM, hr., we will have to insert some of these heuristic rules "in advance".

Q: How far can TM go w. Leont's hours of .04:10? I'd sort of like to make a "Minimal TM" to start off.

I could just put a reasonable no. of concs into Corpus & see how well TM does!

Suitable TSC, I could use GA to find a population of low k cost.

As new examples appeared, the population would evolve to track the new data (as well as better fit for the old data). This might be a good way to start TM.

Re: way I envision TM naturally working: Say its looking for operators that map input problem into output soln. We start, doing an L search for an operator that solves problems well. When we augment the corpus, I expect that small changes will be made in the data of the operator (= "soln."). This is essentially pure mutation.

Re: .21 In coding Sequential Corpus, when the corpus is augmented, normally, the code is simply augmented w. minimal search needed.

hr., occasionally, when a new section of the corpus comes in a large part of the code must be rewritten. This can be done by using smaller parallel codes that were not the shortest for the "post-receptor" corpus augmentation. (This is an aspect of "Theory Revision").

A related technique is OSC. OSC is usually simpler than other kinds of "Theory Revision".

In .20-.27 we add Non-New Definitions, both in .28-.32 (including OSC) we add new definitions & delete old ones.

A common type of Theory Revision, for which OSC is an extreme case, occurs when the SSZ is given a definition in the existing corpus & too small to warrant redefinition, but for recent augmentation of the corpus the SSZ for new data, so it becomes large.

Another kind of Simple "Theory Revision" occurs when we notice

01:176.40 A/O we may break codadown (code) into smaller operators & try to reassemble it in a better (hyper PC) way.  
regularities in the code of f. corpus (so we write a shorter code or f. code), previous.

.02 An indication that we need "Serious Theory Revision" - that f. very very content!  
New Corpus has many parts that cannot be predicted w. f. accuracy that we had abundant. previous corpus. (i.e. Our old theory doesn't seem to be working w. f. new data). This problem can occur in f. very beginning of f. TSD! see (205.08)  
In such a case, (if it is possibl.) we should (try to) arrange to get more of f. a different-type data (= "experiment"), to f. its ssz - also try to get more diversity in that data. → (207)

.07 In 176.28 ff I talk about (re) coding a "new section" (or <sup>sub</sup> new ~~mutation~~) of f. Corpus. The corpus hvr, may not be so "sequentially" organized, so a "f. new section of f. corpus" could include "all problems involving triangles" rather than just "f. last 1000 bytes of f. corpus". Slightly more generally "All parts of f. corpus that used a particular data. or set of data". T. code for those parts has to be revised.

.15 176.21 ff (i. 26 ff in particular) IS a VERY HIGH LEVEL "ENGLISH" descr. of TM's Operation! While it's fairly good, it probably doesn't extend very far into the Variables of TM behavior. Hvr 176.21 ff is very IMP! - I do want to continue it.

Varieties of Coding techniques:  
.20 .07 Also <sup>use</sup> .02-.07, Before trying to get new data relevant to f. new phenomena: - We look at f. old corpus for "sections"/"parts" that are usefully similar to f. new intractable subcorpus. - This is usually not an easy thing to do.

Note: 176.21 ff is on Coding a Corpus (presumably sequential, but I should think/finite objects would not change to discuss. much (if any!)).  
→ [Induction; Prediction]

.26 Hvr, TM's other usual probs are OZ probs & INV probs. INV problems can be solved via Lsrch (see previous 166.21). Hvr, note that most INV probs are solved as OZ probs

T. MCT does link (Lsrch to Optimization (≈ OZ probs): Enables our (in theory) to give probly that a gn. O.T. will do best, w. a gn. OZ problem - So Lsrch can be done on OZ probs in a "practical" way.

Hvr., Note that f. MCT treatment of OZ is entirely Empirical: It looks at Past G results of each OT on whatever corpus <sup>was</sup> used and from this it predicts f. likely hood of any one of those OT's giving a max G of f. given OZ problem w. a stated cc. limit.

MCT does not look at the structure of each OT to determine f. feasibility of each OT for f. given OZ problem. So MCT's analysis would not suggest ways to design new, good O.T.'s Perhaps "TM<sub>2</sub>" would do it?

$(1+i)^2 = 2i$  co ;  $\text{Imp}$

UConn. javanet.com / ~ Bob mere co : imp  
Elmas Elevators

Logical Nihilism  
Illog. (2) Nihilism

So, ritanow, Major Problem areas:

1) Worry about the Learning Algm needed for General INV, O2 probs

177.26 - 40 discusses this a bit. T. General Process of 176.21 seems reasonable.

2) Concern about the epist. details of the  $\text{TSQ}$ : What do I expect F.M. to assume about the examples in the corpus. The "global" v.s. "local" variables, coacs, defined by "rng, imp" for each problem: but there may be ambiguity.

3) Which models of induction: {175.02 or .06} to use.

In the case probs w. {cond, Imp}, we want certain parts of the  $\text{rng}$ .

to be global, yet certain info applies to one problem only, (= "local")

In mathematical langs like Maple, Mathematica, Mathematica - these are ~~tricks~~ they use to make things unambiguous.

Equality:  $3=3$   $4=?$  |  $\text{cond } x=3 \text{ imp } 3=x$  |  $\text{cond } x=y, y=z \text{ imp } x=z$   
Symm | trans.

Addition:  $3+4 = 4+3$ ; (Assoc?  $(3+4)+5 = 3+(4+5)$ )  
Subtraction:  $3+\phi = 3$ ;  $x+\phi = \phi+x = x$ ;  $3-3 = \phi$ ;  $x-x = \phi$  cond  $x=3$  imp  $x-3 = \phi$   
 $3-5 \neq 5-3$   $3-5 = -2$ ;  $5-3 = 2$ ;  $2 \neq -2$ . This idea of  $2, -2$  is unclear.  $N \neq -N$  unless  $N = \phi$ .

well: I can teach these relatively A.M. Rings about the fund. coacs of Algebra!  
Will TM be able to induce/deduce certain rules in interesting Rings?  
Perhaps the main goal of the Learning of Algebra is to have a co. for TM to acquire a complex and domain of knowledge, so that I can get it to learn usefully / or to understand English's a book that domains, get it to genz. English to other domains.

Also, to be able to deal w. "English" that has errors in it.

Perhaps write down a large bunch of things about  $=, +, \text{TSQ, imp}, \times$  that I want TM to learn; so that I can order the examples so it can learn in a useful way.

Then, try to see if TM can learn it. It seems to be possible, refer to 178  
Don't get too deeply involved. At present, the problem is mainly on the adequacy of the info in the  $\text{TSQ}$ , and not on just how TM "learns".

So try juggling around / Back further. (ing sets) is modulus of the  $\text{rng}$  Algm, is a primary idea for  $\text{rng}$ .

Re: the "rng Algm": One imp. part of it tells what parts of the corpus to test when a Modif. of the coding algm. is made.  
But one kind of "hint" could help TM with this problem.  
(A "hint" is any kind of info that  $\downarrow$  cuts for the "Student")



.01 This idea of "association indexing" is very simple, but there are probably very many different methods used in human "indexing" for (relevant) recall.

One very impl. way that TM "Measures" is in its learning of many new situations in particular, original, idiosyncratic methods for categories (situations/events) to retrieval (retrieval methods) situations.

.07 In General, everytime one solves a problem, or gets of impl. info from an experience (this can be during the soln. of a problem), one indexes that event in many ways. "Many" is impl. because (a) I want it to be accessed in many different "similarity dimensions" (b) If the present/new event is similar in enough "dimensions" to an event in the past, it will have enough "code bits", "descriptive bits" in common w. that event to "qualify" for OSL.

How to discover these "categories": When I am working on problems that TM is working on, observe the associations that I make & try to discover categories that would help in that (as well as other) useful associations.

It's not clear that the forgo. stuff will be very useful for intent TM in early TS @'s. I could just assume large IPC available: say  $10^{12}$  ops/sec. Later, when the "scaling problem" becomes serious, I will certainly need "categories" to narrow down search.

.18 So: This is an imp. idea: Categories are hard to devise for early TM work, but will not be very hard. Later, however, there will be very many choices of concs to combine & categories (as other heurs) will be needed... but they should be available (from data &/or introspection) at that time..

↳ Another aspect of categories is heuristics. Whenever they are used, they not only do such things, but they narrow the probly distribn. for the answer.

For MTM this may not be critical - but in NMTM it can be very useful.

The Category/heur idea is very impl. in CREATIVE solns to probs. A good set of categories/heurs will enable rapid solns. of otherwise unsolvable probs. However, it will ↓ diversity (unless it is a e.g. set of heurs). A novice researcher will have fewer heurs & could have more diversity in search. Search will take much longer (than w/ "good" heurs), but could yield a very "Creative", "Unexpected" soln. - could be much better than the more rapid heur. search.

.33 The Methods of Conventional (not Super GA) GA may be an example of a slow, but diversity search, that can find v.g. solns.

(26.2) It is a reasonable way for TM to operate for Induction problems. For a seq. of ENU problems, we solve early probs. w. simple search, using our Appriod that we insert into our work Reference Umc. As we solve more problems, we add constraining concs, etc. (Umc/Pd) & we change pc. of older concs. Occasionally we use New Problems, which usually involve variations of small incremental Modifics. of the pd. Occasionally, like (84.01

.01: 183.40 on 176.28, we will have to "backtrack", and redo the recent string of concs. in a better way. Just ~~under~~ Under just what Conds, we decide to do this, is just how we do it, is unclear ~~what~~ 176.39 ff has some ideas on "Theory Revision". 177.02-15 is of particular interest — if can deal w. "Non-Sequential" data

.06 On 176.21 ff I have this sort of "System" by which I work:  
.07 Contrast this w. MCT analysis, in which I use at all times a "Conditional" Pd — with each <sup>new</sup> <sup>deon</sup> problem being the "condition" on the pd to be used in Learning next problem.

Well, MCT ~~is~~ <sup>distributed by</sup> is it really .07: MCT simply Gives a way to ~~deconstruct~~ take a corpus that consists of several kinds of probs. (Induction, Inv, or) is obtain a pd from that corpus. that can be used to get prodns/pd's for any aspect of that corpus. .... I need to get f. Q of .06 resolved!

I think MCT is .06 are really "orthogonal" They are on different parts of the TM problem, & they don't really interact, MCT ~~is~~ tells which needs to be coded — what code needs to be mixed, .06 tells heuristic way for minimizing that code. ||| MCT defines the problem; .06 tells an approx. way to solve the problem.

.21 On the Q of whether to model using a "Stack operator" or use the "Finite unbounded set" model. Actually, the 2nd model has the same form as the first, but uses more info — it uses info about reg's in it. [input set to stack operator]. It maybe that in both cases we end up w. a stack operator, but just to Goro's ~~advantage~~ over the universal

.26 such operators <sup>are</sup> different in the 2 cases.

.01: 184.40 On t. "Learning" part of TM!

Look at TSQ! (181.5)!

NEN (a set of numbers w " = " connecting them)

The problem is to make a "program" of primitive cons, so that

.05 Input  $n_i =$  give  $n$  as output.

[I will desc. what TM does in English; Then later isolate out the primitives needed]

.06 ① In t. case of .05 a soln. w. to be: - Since output is a number, t.

final operator must have a no. as output. (Useful in "backward chaining")

The only way to get  $n$ , is from  $n$  <sup>output</sup> <sub>inputs</sub>, so t. soln is to take t. number

in t. input & present it as output. So t. prog picks t. no. on t. input

& transfers it to output. (or transfers it as output)

.13 ② try  $3.7 + 4.1 = 7.8 \dots$  act. a long seq. of examples like this, one row by precision examples.

Again output is no. so final operator must map to nos, +, -, x, = or transfers.

Transfers don't work:  $t - k \neq 20$  has 2 inputs - num, input, 1 num output:

try all 8 possys:  $m+n = [m+n]$  &  $m-n = [n-m]$  both w. a. n.

? => Hrr. .08 no longer works on t. new examples. (which is meaning of this remark?)  $\rightarrow$  204, 29

Handwritten note: "Transfers don't work" with arrows pointing to the text above.

SN Q: How long would it take to run these things w. 6 hours?

② Under what circumstances would it run these hours?

When t. put a hour into TM! Imagine a TSQ that would result in TM (learning) that hour, & put it into TM in t. form that it would have found it.

I think this will keep TM's structure very simple! Easy to prog, Easy to understand, (Easy to Debug?)

.25: (177.40) A kind of Logic Model I've had in mind (in lines 176.21 - 177.40)

This "concept net": No feed back in net; No loops in net, but loops are a type of

**Functional** that's used to combine functions to obtain a new function.

A Net of this kind is probably limited to Primitive Rec. functs. - Rec. is not ordinary

a serious limitation (I think!)

Handwritten note: "2005 - Arith. Tabul. Rec. functs w. o. diffy" with "prim" written below.

The language assigns pc's to subsets of functions. At any time, the system

is a Bernoulli seq. of t. ~~of~~ functions ( = primitive + subsets that have been defined)

.32 a Composition of these functions.

.33 We also have a type of this sort for not "operators" but "observers"

The combn of t. is t. ob-op algebra. An ob is a function w.

output of T/F or a Pd on T/F ( = Boolean).

ob: Boolean, numerical or string input; Boolean output.

op: " " " " ; Boolean or numerical output (no Boolean output).

ob, ob  $\rightarrow$  ob; op, op  $\rightarrow$  op; ob, op  $\rightarrow$  op

The Boolean output controls which ~~form~~ of several functs  $\rightarrow$  to be used.

Handwritten note: "I think one of them functions of t. ob-op Algebra was target good cond. p's - to deal w. t. 'Scaling' problem: 229.36"

187.40: This "Selection" function of  $\epsilon$  obs. is kind of certain primitive functions used in Rec. Func. Theory. — So it may be poss. to combine  $\epsilon$  obs ops into something ~~near~~ "universal". — But ~~unimportant~~ — "Algebra" may be adequate to express all diff. kinds of "regularities" in a ~~copy~~ (including Heurs) that I want to express.

19: The way induction is done using  $\epsilon$  Conc. nat: We normally try operators in pc order (w. <sup>using</sup> the loop functional). Occasionally we notice a function that involves several repetitions of a function: we then try to find a ~~new~~ <sup>using</sup> better pc ~~version~~ version of it ~~using~~ <sup>using</sup> the "Loop functional"

20: The loop functional is a combination of a  $\epsilon$  obs and an op. The op is used repeatedly; the obs looks at some result of  $\epsilon$  op & tells it when to stop. The op is usually a vector function: w. 2 components.

23: ~~One~~ One component is used for stop criterion. This is an "Until" loop. [Also, one needs initialization of ~~both~~ <sup>both</sup> vector components]

27: One very common component of the vector argument ~~is~~ ~~is~~ ~~is~~ with  $x=0$ ; and updated with  $x \leftarrow x+1$ . The threshold for termination of the loop is  $n$ ; the loop terminates when  $x = n$  (an  $\epsilon$  obs function).

It is possibly possible to devise functionals that could define functions beyond Prim Rec. Funcs. Using  $\epsilon$  a formalism  $\sim$  to 187.10-13, but I will not go into this just now.

So, using the 2.141 model for assigning pc's to new nodes; (the details of coding the ~~subtrees~~ subtrees will have to be worked out) and the ideas of 187.25 - 188.17: Is this enuf for a major class, a complete model of "practical learning"? [It solves (or is supposed to solve) the "Symbolic Regression" problem]

What it does seem to do is give a model for learning (functions/operators / stochastic operators). This is a very large area of induction; it means that we show TM examples of desired I/O behavior: it extrapolates,

27: <sup>probably</sup> ~~probably~~ its not nearly solving  $\epsilon$  CPU or OZ problems; ~~And~~ It could  $\rightarrow$  189.01 spec

28: "Learn" to do so. Say we label all Env. problems; then give "sols" (re. traces) for solving them. From ~~data~~ <sup>data</sup> many examples of this kind [Building up: (starting w. simple more problems than building up toward more diff. TM probs.)], TM builds up a good pd to use for the standard (Srch Soln of Env. problems).

Maxed  
Currents  
Thm.

Similarly, OZ prob. soln. could be taught.

On the other hand, once TM can do "Induction" (like 187.25 - 188.17)

TM can use MCT to ~~update~~ update  $\epsilon$  cpd's needed to for ~~it~~

[such in Env. & OZ probs.]

50: Perhaps <sup>NOW</sup>  $\epsilon$  has a "Critical Mass" of ideas for TM; That for any problem that arrives, I have some ideas (that I've developed in comp. detail) that are good enuf to solve that <sup>TM</sup> sub-problem.

189.01

188.40

.01: 189.27 So; Or: Then - so <sup>does</sup>  $2.147 + 187.25 = 189.17$  give a adequate model for

Learning stochastic Operators? ( $\equiv$  functions) - Consider also, Imp. of Neurons.

[ Dropping, for t. Moment, t.  $\phi$  of (ort. detail(s) of!) **184.21 = .26** ]

One problem is t. Ordering of Function Trials for Lsearch: See 130.19 then how to count t. ~~number~~ no of operators using n functions of a s. first type, w. n.  $2^{nd}$  function type having  $\leq (J)$  inputs (i output)

156.21 talks how to construct them in BASIC

One ditty is that there will be many duplications of functions in the listing of 130.25ff! (131.11 ff for eqns). This is because per list of functions used, will contain compositions of some of the primitive functs.

"Symbolic Regression"

If we list them in PC order, the hyper PC version will be (Met. Comp. first) will contain t. composed form of t. primitives. - So we will get dupes, but later

$\rightarrow$  in the listing. - This is t. usual ditty of Lsearch being controlled by ( $\approx$  K cost) rather than P cost. My impression is that usually this doesn't cost of Lsearch by very much. (perhaps a tolerable factor of debility!)

In general, no trial operator will not contain more than 3 out functions, because t. PC  $\downarrow$  so fast  $\frac{1}{25}$  t. no. of functs considered  $\uparrow$ !

To order t. Macro functions! Assign to each funct a PC =

.17  $\frac{PC_i}{d^{(i)}}$  : PC is t. PC of drbing t.  $i^{th}$  function. d is t. no. of inputs to t. Macro function ( $i$ ) is R. no. of input of t.  $i^{th}$  (micro) function.

Actually, t. factor  $(d^{(i)})$  should be used, in being the order in which  $P_i$ 's

~~Micro function is chosen~~ - but assume that  $d \gg n$  (it will be 1 or 2 or 3) and usually d will be  $>$  that. (I GUESS!)

Anyway, use .17 for the effective PC of t.  $i^{th}$  function: Then order the listings of t. functions via Huffman (142.01 ff)

Normally, there will be a ~~large~~ long list of micro functions to be ~~combined~~ combined. Also "Normally" there will be heuristics that modify the PC's of t.  $\mu$  functions, in line w. t. "Nature of t. present problem".

So: T. induction process for "Symbolic Regression" consists of: trying to find the "Best" Macrofunction to fit t. data! We do this by first assigning PC's to t. component functs to be combined: we then order strings

.30 of them wrt.  $\frac{PC_i}{d^{(i)}} (.17)$  using t. Huffman Code technique. [The PC's of t. trial strings are first Modified by any available heuristics.]

$\rightarrow$  We test t. ordered strings of .30 using Lsearch.

We usually ~~find~~ find a good fit:

The ~~Function~~ Function grows large w. t. corpus - just as t. data. ~~is~~ in t. "Procorpus" growth  $z_i$  for  $i$  functions, t. difference is, that in case of "Symbolic Regression"

t. only Functions that ever got defined are ones that are, for a certain length of t. corpus, complete Macro functions for that chunk of corpus.

I ran into this trouble w. t. TSCQ's I wrote in SAARB, but 190.01

.01:189.40 I that that this was a fault of the TSO's! - But it was not (at least not entirely) because of Induction model used implied this "Fault"!

One ditty seems to be, that there is only one Macro function: So only 1 "conc. use." If a particular ~~primitive~~ primitive or defined Funct. is used several times in the text, I think it automatically set higher pc. Hvr, it may be poss. to examine the Macro Power to find substrings that are used > 1 time, so it pays to define them. This amounts to a Recording of the Macro funct ( $\equiv$  conc. use)

I'm not sure the Conc. use of the Macro funct. are really the same. They are not identical, but the ordering of conc. use of function definitions have <sup>(100)</sup>  $\leftrightarrow$  correspondences.



14 A vague idea: That somehow the pc of a micro funct. should be related to how often it is used in coding to corpus.

Another idea: That the pc's of micro functs should be related to the frequency with which they were successful in ~~helping~~ helping to derive (temporarily) successful Macro Funct.

Another idea: we have obs that switch ops on & off. perhaps the fraction of time that a function is switch on is comp.

I feel uneasy about the "statistics" of <sup>the components of</sup> a small Macro funct.

In a stack PSG the frequency with which various parts are used, determine their pc's. Hvr, in MTM, this may present a problem. None-the-less, even in MTM, I will have a SSZ for each "decision" - even if it's always  $\frac{15}{10}$  or  $\frac{0}{10}$ .

Also, in linear regression, the values of the coefficients are critically dependent on SSZ.

Hvr, the functional forms for linear (or nonlinear) regression: ~~what~~ what is the SSZ for these? Well one must choose a functional form for each time series produced, so SSZ = no. of Time Series produced

What is SSZ of "components" that help derive functional forms for regression? Say we used many different functional forms for regression. Then the SSZ of the components of these functional forms, would be clearly defined. Hvr, suppose we ended up with 5 different forms for regression & we used them all to their harshest. Then the max SSZ of any component function would be 1/5 only!

So: Consider LARGE, MGT-type, system, in many different kinds of problems / modes of behavior { Inv, or, induction of Macros } <sup>(191.17 spec)</sup> <sub>(Time series of uncorrelated objects)</sub>

abcdefg  
ABCDEFGFG abcdefg.

abcd. (size!)  
kind

It may be that my "intuition" is more oriented toward a system of that kind.  
This is an empt problem: In a particular, the Q of SSZ for HUMANS is empt

In Z141, ~~...~~ (w. ntop each for n >= 2), an ~~...~~ can be used ~~...~~ for production or for defn. of another ~~...~~. (In general, the process of the 2 applies can be different, but they have been the same in the systems I've analysed.)

In the T. SAARB TSO work, each function defined was defined once, used in predn once & could be used ~~...~~ to help define another function, several times

~~...~~ In Z141; each ~~...~~ is defined once, can be used several times to define other ~~...~~; can be used many times as a predicted object.

SAARB & Z141 differ in that in Z141 the ~~...~~ were both part of the corpus & objects that could be used to define more ~~...~~.

In SAARB: T. functions were used to define other functions; which could be part of the Macrofunction, that did the prediction.

.17: (90.40) In MCT prediction, each subcorpus <sup>usually</sup> has its own prediction function.

Sub corpus can be defined from time series, ~~...~~ in the case of unordered objects predn. & each set will have a default stock set. Each OZ problem will have its own out set of OT'S.

are able to share <sup>sub concepts</sup> concepts. We want to minimize the total cost of the

Entire prediction "object". A later development will be the integration of the various sub-systems, by sharing functions - later by a unified system that modified itself in response to the nature of the

problem ~~...~~ given to it.

Say we had a "Unified System" like (23). How would we (modify/improve) it?

Wells suppose the system was a person, & was used to run his life. Part of the

system will deal w. physics. So we have these "laws of physics": we observe some new phenomena! "The error of prediction is much larger than we expected" (I don't exactly know what that means!) But anyway, we decide to try to revise "the laws of physics" we do this in the standard ways; by back tracking as little as possible & trying to modify the part of "the laws of physics" that seem most relevant. If we are successful, & (most) all of the laws will be about the same & the rest of the "human response operator" will not change. (Later we may say to integrate the "modified laws of physics" into the rest of the human response function)

Perhaps go into more detail on "Theory Revision". How it is done;

How PC's are assigned to concs.

A common way to learn: Each sub corpus has a particular

80x4 = 5120 = 5M

30M / 10 / 10 = 600k = 70 days

Macro of solving its problems: Say a function (≡ "OP"). Also we have a way (OB) to recognize that sub-corps, so we can apply this OP to it.

The main process, then, is developing obs & OPS for various sub-corps.

After we have lots of sub-corps in assoc obs, obs; we try to integrate all of this, by finding similarities in obs, ops, for diffrat sub-corps.

These similarities can be due to "Sameness" in much of the functions involved or it could be due to "Analogy" & Plan mappings from one to the other.

Think of the development of Sci & Theory revision: Do this in English.

Get forms of heuristics. Get algos for design of PC.

Consider GRUE problem-types

[Yes, I should be able to do some Analysis & Elementary Algebra TSD directly! - Perhaps do lots in 11.]

.14 One kind of activity in a (person's) life is Mathematics! - So if he is working on a general theories for physics, he will use mathematical formulas & formalisms, etc, that he is interested in! Math & Physics can be synergistic! So the idea of applying & xplan to physics is much higher & xplan has been much used in Math!

.19 In general <sup>fertilization</sup> cross-fertilizations of diffrat fields of interest ("Domains") are very ~~simple~~ <sup>simple</sup> in determining PC's, in guiding heuristic search. Perhaps this means that certain concs. that would ordinarily only appear in the ~~dom.~~ of a sub-corps, could appear in the sub-corps of a diffrat domain.

.24 Also when the <sup>sub-</sup>corps is Algebra (or other Math), there will be definitions of objects occurring in the sub-corps, that are also useful in the Macro Function for Math (as well as in other Domains)

.27 So, Math is a particularly good thing to do induction on, for this (.13, .24) reason. → 200,32

.28 While .19 <sup>seems</sup> very <sup>clear</sup>, non-trivial, it seems unreasonable that it shouldn't be able to get more (hyper) SBZ (confirmation) of concs. that are <sup>mainly</sup> used in the Macro Function.

.28-.30 seems like the present main Bottleneck!

I'm not at all clear on what objection .28-.30 is!

.33 An. Obj. related to .28-.30, that seems strange: Say concs A & B are used to define C, & are not used much after that, but C is used a lot. A & B get no more SBZ! - even tho they are part of C! - This may be ok. A & B contribute to the <sup>approx</sup> PC of C, but after C gets large SBZ, that approx. becomes much less important. → (But still A & B are "Part of" C!)

Re: .33 If C was defined in several alternative ways would we want C's by PC "feedback" in a "Bayesian" algorithm to it "determines"?

Puls

Platinum less w/500.

\$10/8.

100k = 10 kg = 20 lbs.

= 1 pint

.01: 192.40: On the other hand, if we are mainly using these concs in definitions & they don't have a large size in ~~the database~~ their capacity, then they get low pc as definition components. (I may or may not want to ~~use~~ pool data from ~~data~~ & from ~~subcorp~~ — who then I do so, depends on size — I can do both & wt. of which error is back, will depend on size in both "defns" section & "sub-corpust" section. → .30

Reasons for Publishing:  
 1) Estimate ~~of~~ of colleagues.  
 2) Need of change

3) Good to ~~some~~ ideas. Put them in ~~an~~ abstract form

In: SAARB TSO's: I did note that only concs defined were those ~~used~~ that were solns. to problems. I ~~at~~ more recently "decided" that this was not a fault of TSO, but the method used for induction implied that this would occur. — Hrr, it may not be true!  
 ① Often the Macro Op. is in sections so the soln. of a problem could, essentially, just add a new "section" on to the Macro Funct.  
 ② Secondly: After we have this Macro-Funct; we could partly or completely decompose it & re-code it in a different way do the PC in terms of functs that have been used in other parts of the "Universe" as parts of Macro Funct &/o parts of ~~sub-corp~~ sub-corp.

One point of the re-coding in .14: Mainly to ~~generate~~ find concs of hypc that are used frequently/effectively, ← (?) ... (.19 is more to the point!)  
 Also: ~~re-coding~~ gives vs shorter codes & less expected future error in productions.  
 I think I've lost sight of .19 as a Major Goal (or sub-goal).

I had been focusing on the idea of ~~inventing~~ new concs & verifying them ~~logically~~ — but this is always secondary to the goal of .19. — Getting Max total pc of codes w. f- available cc.

So: what about the diff. of 192.28-.30? Actually, look at 192.33-.40 If A & B were only used once to define a variable conc, C, then they are, indeed, not very useful for defining new concs, & they should get low pc for that applicn. — 193.01-.06 is certainly relevant (correct). Note .03-.06

on Pooling of data from 2 diffnt applicns. of the data. of a conc. →  
 A Possl Example of such "pooling": We teach TM a certain conc, by giving it examples so it can tell if an instance given is a case of the conc or not. (This is the "conc" in the sources of Computational Inference, ("Variant")) This data, then, is in the sub-corpus. We then get TM to use this data as a predictive conc &/o as part of the data of a new predictive conc. I had planned to use this method of finding very often in early (at least) TSO's. The concs, then, would be "Terminology" Terms of ~~the~~ apparent importance in Math, Algebra (& perhaps physics)

Def. Conc 1  
 All concs are concs  
 All concs used not be concs (is) hrr

So T. Q. is, in view of T. <sup>apparent</sup> resoln. of 192.28-30; (on 193.19 - 40),  
 can I start to write a complete dem of (T. initial) "Long Alg."?  
 It will be pretty much like ~~the~~ T. SAARB TQ, except that it will  
 be regular (in English) ~~more~~ - i.e. More "General"! Also, it will  
 do much ~~more~~ travelling or impt concs of meth, Alg.  
 (Also perhaps simply cases of Meth, Alg.)

Try to give Examples of the Varieties of Long Prod can be done  
 w. this method - specifically try to get beyond the SAARB TQ  
 examples. (No some of E. examples not "fleshed-out" on vol of SAARB,  
 into be worth going into now. E.g. solving of linear  $\rightarrow$  quad  $\rightarrow$  cubic  
 (is maybe 9th)) - a Morph higher, using properties of E Elliptic curves)

Write review of ~~163.01ff.~~ 163.01ff.  
~~2 parts: 1) 163.01-187.40; 2) 187.01-193.40~~ 2 parts: 1) 163.01-187.40; 2) includes 176.21-177.01-40  
 Part 1 is on TQ in General part 2 is on Long Alg. | Section 12 <sup>1/2</sup> of section 2  
 While Part 2 would seem to be a self consistent "unit" | in pp. 5000 1) = 16 1/2 pp  
 2) = 10 1/2 pp

apart from Part 1: This is not so. There is much in part 1, Part 2 impl  
 var. for Long Alg.: e.g. 182.32-187.19; on "Heuristics" "Categorization"  
 so section 2 is 176.21-177.40 + 182.32-187.19; + 187.01-193.40

176.21-177.40 is a good picture of the General operation of the "continuing part"  
 of E. TQ. 181.06-19 (Also Top of P. 181) Discusses "Scaling problem"  
 (is 181.06 Gives 2 kind of Criteria for soln. - is a very impt. problem T. )))  
 A long discn. of Heuristics Scaling 181, 182.32-183.33

There are < 10 ~~imp.~~ imp. idea in .17 refs; I should be able to  
 list them & desc. them "Briefly". [Later, make more detailed dem as a kind of PAPER:  
 for myself

- 1) T. main picture of TM operation of 176.21-177.40
- 2) Heuristics & Scaling: 181.06-19 (top of P. 181) (181.19 R)! 182.32-183.33
- 3) The diffy of <sup>190.64-40, 191.17-40-192.01 FFFF  $\rightarrow$</sup>  192.28-30, 192.33-193.06, 193.30-194.10  
 This involves pcs of concs <sup>A=B</sup> used to define (concs) a very useful conc. (C); C is used a lot  
 A & B are not used again: Should A & B have by PC?

4) Int SAARB TQ'S; T. only abss (= concs) discovered, were solns. to  
 problems. How bad is this? Can it be avoided?

- 5) The idea of Global vs. local references: T. invention of cond, imp formalism
- 6)

available  
 01:194.40 [SN] In doing TSO's, The large available HDD's (w 40 G-by) will make it easy to store TM's state after each TSO session. This makes it possible to "Backtrack" if I ~~suspect~~ suspect that I've led TM down an inappropriate framing path. I can also try sections of TSO in various orders.

[SN] Make lists of types of problems for TM; first a broad list: [Induction of a) Time series b) unordered sets; Inv probs; Oz probs.]

Then Alg, Geometry, Physics, Chemistry!... Then perhaps more specific problems in these areas:

Then: Simple induction & "learning" definitions in Math by example: Various Math problems: Exemplified by "Hints": (I can study the effects of "Hints" by backtracking to reading the problem.)

The "Advice Channel" (McCarty): Related to "Hints". Telling TM soln. - This is an extreme form of Advice or "Hint", I can either have special "channel" for this, or simply insert the soln. into TM by suitable programming of component concs.

Perhaps use term "Abs = Abstraction" instead of "Concept" - use concepts for efficient meaning in computational lang theory

"STUDY" Problems: These are given to familiarize a person w a particular domain, so he may <sup>discover</sup> learn relevant concs. Often this is done w a teacher knowing (consciously) what the "relevant concs" are. The "study problems" may be given as a kind of "hint" or as a "hope" by the teacher (who may be the student), that these probs may yield needed insights. STUDY Probs can be used in 2 <sup>extreme</sup> ways: 1) T. teacher knows what concs are needed & knows the study problems contain them. 2) T. teacher doesn't know what concs are needed, but suspects the study probs "will have useful concs in them." [Various Mixtures of these 2 extremes]

[SN] Would it be poss. to do useful TSO/TM development (at a beginning) using small CJS problems (almost exclusively). So it would take < 10<sup>4</sup> for a soln. (may be < 2<sup>4</sup> for a soln!)? T. Q is: Could I investigate/demonstrate all of the <sup>important</sup> ideas using small CJS? Using, say a 1MHz machine & machine code, these small cjs could be w 10<sup>3</sup> or 10<sup>4</sup> bits. - which is not so small! For the SABB TSO examples, I think each trial was "very large" & I expect that these problems should have been solved much faster using good heuristics - designed to facilitate "scaling".

433 x 1.25 = 5 +  $\frac{100}{3} \times \frac{80}{3}$   
 $\frac{100 \times 80}{3 \times 3} = 42$   
 = 592

[SN] APL has a v.g. set of "Functions". - So that combinations of them tend to be "interesting" to Mathians! Could I use a subset of them as "Primitives" for learning certain areas of MATH? [ ]

8.23.00 Bule

197

.01196.40 So: Go Para 163.01 ff: See how all of this fits into the Learning Aiem of 176.21 ff

8.23.00 B. G.

.01: 196.40  
.02

**SN**

An aspect of f. TSO that I hadn't recently much considered.

It is f. Soln. of INV probs.: e.g. Proofs of Alg. Programs.

My Rts about building up good abs from simpler sub abs stem mostly, perhaps from considering problems of this kind. I would use certain soln. techs again many times in diffrt problems. A particular soln tech again would acquire a hy conditional pc for problem in which it was appropriate.

This seems much diffrt from ordinary induction on an unnumbered seq which is what 176.21ff is oriented toward — i.e. probs of 194, 29, 32

.10

arise in  $\rightarrow$  They may not arise as INV problems, coroll.

In a continuation of f. SAAR TSO — I could start w. simple induction of defns & simple Alg. notation. The solution of (lower or higher order eqns., could be <sup>formulated</sup> regarded as induction problems, INV probs or OZ probs.

An imp't favorable feature of induction, is that its mainly what an infant (Machine or human) does in the early part of its life.

Now, one may also view the Infant TM as Schmidhuber: that its trying to maximize its mean Guro — i.e. that it uses induction as a <sup>main</sup> tool toward this goal.

Perhaps the main thrust of f. present work is to get TM "started" then, using MCT, add various kinds of problems to its Repertoire.

One very early idea I had about TM<sub>2</sub>; that it would not be of much value until TM had accumulated enuf experience to successfully work on OZ problems of that kind. This idea can be stated: i.e. we can't expect TM to do anything very clever, until it has had (as part of CORBUS) <sup>adequate</sup> experience in the domain of a certain "Cleverness"

I think what I want now, is to set it up so I can <sup>give</sup> any kinds of problems to TM, so it would have ideas on how to solve them.

Induction in unnumbered seqs seems like a good place to start, but it seems to have characteristics of 194, 29, 32 — which are somewhat idiosyncratic!

Now, I could just do the induction now, to start off. It will certainly be an imp't mode of operation. It may be inadequate as a "full TM", but I can add other modes, later. I do want to know if there are some essential differences of f. Pure Induction mode

T. Pure Ind mode can learn how to work INV & OZ problems — it can even learn to work probs that are not logically INV or OZ probs. So it should acquire the cons of .02-.10 when after it has tried to work INV problems.!

.01: 198.40: [SN] In induction probs: When (2+1. beginning), I "give" TM a heuristic,  
.02 be sure to put it in the form that it would have if TM discovered it itself!

.03 e.g. Say it's learning  $1+7=8$ ;  $3+2=5$ ... then  $5+3=?$   
? is very probably a Number. The operation " $5+3=?$ " has to have a number as output. Thus - 2+1. final funct must be add, sub, mul, div. (or whatever 1. set of operations w no. output is 2+ part func). The inputs to the funct must be num. so  $5 \div 3$ ; 4 possl inputs, 4 possl functs, so 16 trials.

.08 How we get all this into form in which TM could have discovered it, is unclear!

.09 Assume an adequate corpus for ~~the~~ these discoveries.

In .03-.07 Much of the "Reasoning" of the Heuristics used, seem ~~deductive~~ "deductive" I will have to put all deductive in inductive form!

Re: .01-.02 & .08-.09: putting the heuristics into TM in a proper form is very ~~difficult~~ complex.

.13 An approach: TM looks at the "problem": " $5+3=?$ ". It has an "association" w. the symbol ? - that it has always been a "number". This "simple" induction implies that for "various features" of the problem, TM has "associations".

Each "feature" will then have its own "x" property like "set". In this case, the "feature" is "?" & its property is "Number".

.13 ff is a very common type of induction - perhaps the commonest (i.e. Baum Seq.).

.19 The next step, to realize that the final funct. in a function set must have numbers in its range, seems more diff. Each function that TM has been given, or discovers, has a domain (input) & range (output) - COMPLETELY

In general, TM may not know the range is domain of a fun. So, each funct has several properties; Range & Domain are two: Symmetries (if say) on inputs is output. Numeric functs (domain) can have anti sym.

arg.  $x-y = -(y-x)$ ; division is a kind of anti symmetry  $x \div y = (y \div x)^{-1}$  (except for zeros)

[ this "reasoning" is beginning to sound like Lanet's "AM"! ]

On second thought, .19 ff is getting "Too detailed" (no longer "English")

.24 [ But I do want to (conventionally) find a way to express all heuristics as part of induction - as a probabilistic narrowing down of the "Search Space"

One big reason for .23 is that it will make the program much simpler <sup>easier to write/debug.</sup>

I do not want to program a special section for heuristics - I want to have only a simple induction algorithm.

So all I have to do is get a general (rule system) planned. The heuristics should not modify it in any way! Hvr, to test the <sup>learning</sup> system - make some tests can a quick use to info of several impl. types of heuristics. (perhaps including "Quick Abort")

5 x 2/3 1/3

Laws of Logic: Laws of Algebra:

TM should be able to do both of these rather easily, since these laws are useful in induction - i.e. finding regularities in tasks.

[ So why did it have to much trouble w. Rules in SAARB? ]

Perhaps the laws of alg. & solving eqns is only implicitly important

our induction has some finite C.B. Otherwise, all films of all eqns are defined by the equation  $i = 1$  or  $pc = 1$ . So  $C.B. < \infty$  is very better than the laws of Algebra etc to become useful in induction.

Re: .06 ! Even if arithmetic does have cc, if it's known cc is not the cc of simple reasoning, it would usually be cheaper to do arithmetic (eg. to the laws would not be discovered!

Even w. small (non-0) cc of arith, if TM learned to solve eqns, the laws of Alg. would probably be useful. - In fact, it may be true, that to learn to solve eqns, TM would have to derive the equivalent of "the laws of Alg."

If TM uses Logic for solving problems, cc would always be an imp. factor in finding the solns. (A what about "QuickAbout")

So: try to find problems for TM, in which some laws of Alg. are used.

OR: Just try to get it to learn to solve all kinds of Algebraic Problems:

This is probably "equiv" to trying "Laws of Alg." (!??)

ABCdefghij

It is equiv.  $\leftrightarrow$  TM ends up w. the same paths for various all cases (i.e. ends up w. same cc for all discoveries, as a TM that "knows" the Laws of Alg.

198.01 -  
on previous pages

How, w. large enough size of eqns, TM should be able to discover any describable conc. So how do I derive "Laws of Alg." as a conc?

It would seem that the "laws of alg." should be discoverable from a softer large bunch of "Arithmetic Experiments" by TM. - (if it did "Experiments" of this sort.

Another possy: that if part of TM's "kinds of tasks" was included discover Mathematical Conjectures (i.e. perhaps occasional proof) w. suitable hears to help decide if a conjecture was "interesting / useful",

that it would do better in regular lang. of chem, physics, language etc.

That ~~is~~ Inter-Domain Learning (192.14-27) is

can be very imp. ex. - [28-31] could be an imp. example.

I had originally thought that Math alone could be learned, but perhaps it should be learned as having 2 aspects ① Math as something to learn:

solving problems, proving thms. ② Math as an ART form (Making Conjectures, Deriving & proving Provs, Making Defns of "potentially interesting" ideas, etc.

The direction of MATH ART could be partly (or wholly) driven by TM's examination of its content (i.e. history) of Math. - What has happened

The interest of Mathematics is what, in your long run, has been most useful in Science — By TM's INDUCTION on that info.

Going Back to "Laws of Alg". After TM has done a lot in numbers using  $+$   $-$   $\times$   $\div$ , it might ask "Are there some relations of interest betw. the no.s & those functions?"

Try to find problems in which certain laws of alg. ~~would be~~ are useful ~~when~~ in finding solns. Probably, instead of "Laws of Alg" it would find many specific rules: That is "Laws of Alg" would be a way to compress, to express, in a simpler form,

those rules. The value of "simpler form" is that the laws are more likely to be ~~useful~~ ~~to~~ new laws of interest.

The "structures" of the laws could be used for "induction by analogy",

which is a very powerful, "creative" mechanism.

So, in search, I did get some things like the laws of Alg, by teaching TM how to work linear Eqns. — It will be possible to go from Rule to .08-13: Hrr, even if  $t$  allowed  $cc$  would be large, I suspect that the ~~size~~ front. existing data, would be too small to allow the "Laws of Alg" to be induced — Too few & unclear! we could start w. every large no. of rules (large  $cc$ ) so the "Laws of Alg" could afford some compression.

The large  $cc$  needed could be prohibitive! We could just "wire in" the solns. to the search. In fact, it probably did take a lot of search time in the Math community. — But the Math community also had other heuristics / @ Per Goals (like saving time in ~~searching~~)

$+$ ,  $-$ ,  $\times$ ,  $\div$  operations)

So Laws of Alg are discoverable (or) by

- 1) need to speed up  $\times$   $-$   $\div$
- 2) use in solving eqns.
- 3) A compressed format of rules of Alg.
- 4) An orientation toward discovering "simple" rules relating

Real numbers ~~etc~~: Rules relating integers give an entire new area of Math (for many yrs. a Basic Arith Form) — Then later found useful in reducing  $cc$  of certain calculations — ~~etc~~ in problems relating to ~~etc~~. Also in solving Diophantine Eqns.

Re:  $+$   $-$   $\times$   $\div$  : May see more w.  $\phi$  as unity (relation of  $+$  to  $-$ )  
 $\times$   $\div$  : " " " " (as unity. (relation of  $\times$  to  $\div$ )

$$x + 3 = ? + 3$$

$$x + 3 = ? + ? \quad (? = x - ?)$$

→ What I want now, is a (somewhat) general / way Alg. that I can easily program.

This should be general enough so I can apply it to several domains.

Then I want to try it, first theoretically, then practically, on several TSP's from somewhat different domains

Also, I want to see if it can detect (in theory) a kind (w. available cc) Various (impr. heavy) hours.

Superficially, it would seem that a "Laws of Alg." would be like "the laws of Physics" but over different domains, — But maybe (apparently) not!

After ~~some~~ <sup>being given</sup> ~~examples~~ <sup>examples</sup> of a many ages of ~~some~~ <sup>some</sup> ~~solve~~ <sup>solve</sup>, TM may be able to find ~~the~~ <sup>numerical</sup> values for ~~x~~ <sup>x</sup> ~~solve~~ <sup>solve</sup> ~~the~~ <sup>the</sup> ~~value~~ <sup>value</sup> if its value is substituted ~~problem~~ <sup>problem</sup>: What would "motivate" such a discovery?

We might force it what  $x^2 + 3x + 2 = 0$  means as an "eq. to be solved", e.g. give examples of eqs paired w. their solns, & see if TM can find the relation (Symbolic Regression).

well, in looking for reg's into data, TM might notice that in f problems, solve  $f(x)$ ;  $\exists z$  s.t.  $f(z) = 0$  was always true. This is a logic. reg'arity, but it's not immediately clear to TM, that it's useful in pred'n! — Unless TM knew about approx, say it could think of solving  $f(x)$  as a problem of finding  $x \Rightarrow |f(x)|$  was min.

Perhaps it would be a good idea to list a bunch of problem types to see how it if TM could learn to work them. By looking at several types, it may get ideas about how to solve them all!

(SIN) from  $x+x=2x$ ,  $x+x+x=3x$ ,  $2x+x=3x$ , etc., could TM induce  $2x+bx = (2+b)x$ ? or, more relevantly,  ~~$2x+bx = 7$~~   $2x+3x = 7$ ; could it induce  $x = ? \div (2+3)$ ? could it induce "causality" i.e.  $x+x+x \dots x = nx$ .

well, we could have TM learn what  $\exists$  solve  $f(x)=0$  meant as "finding a definition". Learning how to solve  $f(x)=0$  is a quite different problem.

Now knowing the meaning of  $f(x)=0$  would seem to imply compression in e.g. corpus.  $\{ f(x)=0, \exists \}$  How TM would deal w. this compression is unclear. It may, indeed, be unable to deal w. it, if the only kind of compression it knows, would have to be one or more instances of the expression " $f(x)$ " that would be poss. solns.

is interestingly hard

.01.20290 → Do I have a clear idea about induction, so I can try that  
linear → Quad → cubic (or any)?

.03 That  $a = b$  implies  $b = a$ ! There are 2 inductive aspects  
This idea: (1) How can it be used to compress a corpus (i.e. what corpus? & what other regys ("facts") would TM have a "know")  
(2) From what corpus & what "primaries" could T.M. learn .03?  
w.o. this info, I'd have to insert .03 into TM in especial way.

.08 → It would seem that if .03 were at all useful in predn., that there would have to exist a corpus that is .03 can help compress, - & we could  
∴ "in predn.", use this corpus to discover .03.

.11 To repeat the idea of .08: if .03 is useful in any particular inductive  
problem, then a large set of problems of that type could be used  
as a corpus to "learn" .03.

So .08/.11 mean that any trick that helps in induction can be  
"learnable" w. a corpus of proper kind.

.16 O.k. Then given problem  $1 = X \text{ imp } X = ?$   
.17 It would seem that .03 would help solve all problems that we'd  
.18 have a corpus like .16 for TM to learn .03. However, we'd like  
TM to be able to learn .03 just by observing numbers and their  
.20 relation to each other & to  $+$ ,  $-$ ,  $\times$ ,  $:$ .

Why .18-.20 is disturbing: # 5 (like to think that TM could learn  
just about everything about R.W. from studying books & perhaps just the  
internet. Hvr. .17-.18 suggests that we'd have to have a  
specialized corpus to learn certain things!

.25 On the other hand, if any idea is useful in predn., then that  
"idea" can be learned w. a suitable (i.e. commonly occurring) corpus.  
So .25 can be regarded as an idea about corps useful in predn.

Now, how to "buy out" .25? Find some things I want TM to learn  
in which the laws of Alg. are useful.

.32 [SN] on "Quick About" hour: By speeding up search, it enables us to get  
hyper PC (in Lench) for a given CC. Just how TM is supposed to recognize  
this is unclear at present

.35 I guess to buy that disturbs me about "Ingr Loves of Alg" - that at first  
glance, it seemed like it should be easy for TM to learn such a thing:  
What is not clear is just when & when it is not "easy" to write a tpe for  
a particular lang. task.

01:20:40 In the case of "Laws of Alg" (or any other lang), we have to ask: what is the criterion for TM having learned this concept? How can we test TM's "knowledge/understanding" of it?

Clearly, it is not legal to ask TM "what are the colors of Algebra?"  
 TM does not really speak that lang. The only legal tests are inductive problems.

06 What inductive inductive can it make? What new inductions can it learn rapidly?

(This corresponds closely to a <sup>Human</sup> Teacher Monitoring a Human Student! Try to figure out if a student has "acquired" a certain hour, or what part of student's work is "containing" a problem)

Consider "equals": If TM knows about "relations" then "=" is a special relation on 2 things. It is idempotent & ab transitive.  
 I could ~~test~~ have TM learn details of relations: Then ask if "=" was a relation, ask if it was idempotent, sym, transitive.

So: A present poss view: That TM can discover any conc. Relations useful for ~~tasks~~ tasks it has been given (if ss is a conc. algebraic).

But discovery of "Laws of Alg." is probably not essential for TM to be able to work most Algo problems. When TM studies other kinds of Algebra in which  $a \cdot b \neq b \cdot a$  &  $+$  assoc law may not hold, etc. — Then, it may be more likely that TM will try to compress the set of rules it learned in solving algebra problems — to give it "Laws of Alg."

19 (3 ways to do this: "Laws of Alg" 182.27)

The (203.35-40, 204.01-19) is a reasonable way to look at "Laws of Alg" (also note 203.25). I still don't feel entirely comfortable about it. Quasi. The overviews of 205.35-40 still remains!

24:187.17 Look at my initial treatment of TSQL (of 181.5) on 187.01 ff. In a realistic situation, TM would be just starting up & would have no hours that it could have discovered itself. Nevertheless, I could just grant a TSQL from "TSQL" & see how it least increases (w.o. use of hours int. TSQL).

T. point of the foray would be to see how to solve to different problems in f. TSQL, interact (or are indep) in the solving of a new problem.

30 In particular, I'm interested in how Heuristic info is acquired & applied. At present, I see no particular difficulty in 30: TM just has to acquire the hour (which is a regular inductive problem) & apply its results to new (post hour & original) problems.

Well, in 187.13 ff,  $(3.7 + 4.1 = 7.8 \dots)$  was normally try ~~to~~ inductive functions under ~~reality~~ <sup>input</sup> on the expression.  $3.7 + 4.1 = ?$  (also, participate in the process? is we start with a set of facts that we have: & we continue by making more complex functions on the input expression,  $3.7 + 4.1 = |$  The final function (usually in use) map to nos. (This ~~is~~ is a heuristic discovery that narrows down the f.D. for the final function)  
 The inputs to the <sup>(identity)</sup> unary function are 3.7 or 4.1. 205.01

.01: 204.40: (We can wire in f. fact that the numerical operators identify, + - x: only have numerical inputs so this limits our choices.

This learning 3.74.1 = 7.8, but this new operator will not work with "3.1 = ?" (f. earlier problem (and on 187.08 R) So, it now has 2 operators: one for <sup>plus/like</sup> 3.7 = ? the other for plus (like 4.2 + 7.1 = ?) So each is good  $\frac{1}{2}$  time, so they are both useful, <sup>10 to</sup> 2/3 compression is obtained. → 16

.07  
.08 TM's motivation to continue searching for a better code: Unclear! I did write about this recently, hr. (177.02) The idea was that we needed "serious theory revision", when f. system's error rate for f. new data was much worse than what we had before (or for whatever reason — worse than what was expected). Even hr., this is not very

Vague answer! I'm mainly thinking of Motivation for Theory Revision in Physics.

.16: .07 Then (for reasons, like (or better than) (.08 - 14)) we look for a way to get better prodn. A common way is to look at the subcorpus in which "add" was f. v. s. operator v. s. subcorpus in which "identity" was f. v. s. operator.

3 = [?] v. s. 7 + 2 = [?]. We can distinguish them in (several) ways: One way:

.20 ① 3 symbols v. s. 5 symbols: (hr can TM "count" at this point: ?).

.21 ② 2 nos. v. s. 1 no.: <sup>presence</sup> presence of "+" v. s. presence of "=".

[2nd way, 6.5 same kind of problem arises when -, x, ÷ are used.]

The Heuristic of .17-.18: How could it have been discovered?

What hypothetical corpus could give rise to it? What operators could be combined to discover that regularity? Seems like a very sophisticated heuristic!

NO → One way: Heuristic (Even w.o. the heuristic .17-.18) TM notices during execution of Cands, ...? ... Nothing to notice! on n=?, we try ~~add~~ add(n,n): On ~~m+n=?~~ m+n=? we try ~~ident(m)~~ ident(m) = ident(m).

A (perhaps) reasonable way to get heuristic .17-.18: It is a way to

~~original~~ <sup>original</sup> xpm 4/ induction problem into 2 word induction problem ("OR" x pm)

So we end up w. a "Time Series" w. elements n = ? → "idea"

m+n=? → "add." We need 2 Op that has "idea"; add is ok.

I have to investigate the primitive Op functions. How can they (w. Op func) generate b. needed discrimination?

Compare [m+n=?  
n=?] 2 subcorp: How to discriminate: the "+" sign

is the simplest way. (No size <sup>mito</sup> also quite simple).

What I really need to do: Examine OPS is how to use them in induction; How to use them to do b. comp

In general, ops have same inputs as ops. Numbers, Booleans, character/string. <sup>Basic "select case" inst</sup>  
→ I may want output to select from a set of functions, rather than be just True/False

Mainly, I'm trying about an op as making a choice among ops. An ops are a subset of ops

In the present case, I want an "ob" that can recognize difference between

"n=?" is "n+m=?" and use it to execute proper "OP".

- 08
- 09 Presumably, I have an ob that can look at an element; give 1 if a number, 0 if a non-number (see 25)
- Some other poss. (ob) of interest: The usual "If a <= b" T/F.

This test is "Does such a relation hold among 6 inputs"

A "relation" can be regarded as a kind of "class" of numbers "inputs"

— Here, all elements of a relation have 6 same, so "relations" are not the most general type of set.

14 One kind of ob gives: If (a) then (b) else (c)

a is an ob; b & c are ops. so, if uses a to choose between b & c.

Here, what I want is a diff. from if then else. These are used usually to control flow of execution: to do diff. things in a functional lang.

So, 14 ends up being an op.

The problem I'm working on, is to augment the normal set of funcs used in ordinary Algebra with presumably by adding to ops.

Here, other people in GA probably have been using an adequate set of operators. Koze has (usually) been using LISP.

Returning to Nos Mouton! Say S is the set of non-numerical objects

that have appeared in the corpus Puz for. So S = (=, ?, +) only 3 kinds.

- 26 Issue w. each is a "ob" that can tell if it occurs at a point in the corpus, by having a T/F output (Boolean). (see 09)

28 I could drop Puz problem for a while, & assume that somehow, somehow f. lang. was able to distinguish between "n=?" & "n+m=?"

30 There is a Q about the form of input: The input is a set of strings of symbols & numbers. If a string is 20 symbols long, I have assumed that the input must accommodate 20 inputs, simultaneously. Even a long equations will be hard to accommodate! A poss. way is sequential input of symbols. An equiv method; T. inputs of 6 functions have addresses for their args, so Puz can get them from any point in an arbitrarily long input string. — Here, best to work on this Q when I xlt. from "English" into "code" (2/10/02)

Perhaps model Puz language after the way I write programs, say "Basic".

Also, if my notion of what I do (in English) is simpler, I should be able to put it in more exact form — i.e. a formal lang.

OK: Well "n=?" v.s. "n+m=?" "in English"

.02 So I had two ~~3~~ approaches on 205.20 - .21 "in English" ① 3 v.s. 5 "symbols"

.03 ② 1 v.s. 2 "nos." ③ presence v.s. absence of "+".

These involve ① counting symbols ② counting number ③ counting non-nos,

④ "country" "+"'s. ⑤ Threshold for no. of counts. ⑥ use of <, ≤, <, ≤, =

.06 For "if" part of statement.

(SN) Unlucky, having 3 parallel codes doesn't help in normal Lsrch —  
we just use the 3 into one w. best Lsrch. But note: 3 ll codes has ~ 3 times as much  
CE, solved out up w. ~ same Lsrch of soln! → (How may be something wrong w.

This arguments, hvr. — it has been my impress. that  $\frac{PC}{CE}$  would be appreciably

better as a cost criterion for Lsrch than is ~~the~~ normal Lsrch ~~is~~ —

So "check this out" ! (C) 8-21:30 TM Gen: 1.01 - 15.90 is on this problem.

In .02, I'm keeping discuss "Vague" in English: "Continue in English".

I may not be as good as I once was in xltng from English into Math, but — too bad!

Anyway, in .02-.06, ① & ② have to do w. "Size of expressa: [

Prin Priz is a very fundamental idea — related to PC (i.e. "H/c. complexity").

— So the TM could have miss "Built-in".

Another "Built-in" skill; in .03 — recogn of "+": This is a "novel"

Symbol because it doesn't occur in "n=?" so this, too, is a legit

way to recognize differences betw. strings.

(SN) A worry about ENGLISH decn of top. 2 soln. and Priz;

That a thing that seems simple in "English" may not be! The main  
example is "Deriv of Laws of Alg".

Back to TSP: A possib sequence of problem types:

1) Learn to evaluate alg. expressa. (not in Polish) — Perhaps by Polish as ll top —

so  $3 + 5 = ?$   $3 \times 5 = ?$

$3 \times (8+9) = ?$   $(7 \div (3+9)) + 2$

• See if TM can "Get to General Idea" at any point in tag, —  
which means it can do evals. of alg by depth:

Next soln. of algus ~~x=2~~;  $x=2$ ?

"Solve ~~x=2~~ ; solve(x, x=1) = ?" each. of the function "solve".

$x + 1 = 3$  ;  $3 \times x + 3 = 1$  ;  $x + x = 3$  ;  $x + 3x + 7 = 2$ .

(discussing that  $x + x = 2 \times x$ )

→ Perhaps ~~perhaps~~ my v. early Rec Sol ARB stuff on TSP.

→ Hvr., note that one of the Great Breakthrus assoc w. MCT, was  
that TSP's should be easy to write! That any needed conc. should be  
feasible by examples, hints, "telling" or "writing"

So, just my doing an "English" TSP for Algebra! — continue  
what I've done, including other heuristics. These heuristics are usually — 209.01

Varieties of knowledge TM should be able to have:

- 1) ~~Cond.~~ P.D. : Input: desc of I/O prob: Output: Pd on desc of <sup>poss. solns.</sup>
- 2) " " Input: OZ problem desc: output: P.D. on ~~that~~  
Open Techniques (OT's): Pc = Prob that that OT would give best  
 G for that problem in available.
- 3) Languages: Pd's over sets of finite objects (possibly organized objects)
- 4) Given a "Narrow" (3 sources of assoc. info) of a T.S. & ~~is~~  
 a subsequence of it: It has a P.D. on contents of that T.S.

T. lang. are 6 kinds of info that I've been mainly concerned w.

~~5~~ Knowledge of  $\pi$ ,  $\sqrt{2}$  etc: essentially i. ability to calculate them  
to any precision a/o k. memory of a fair no. of digits of Rem. (6 covers this)

6) Knowledge of how to do various types of math problems like  
Solve eqns, compute  $\pi$ ,  $\sqrt{2}$ ,  $\sin 35^\circ$ ; multiply, invert matrices.

(This includes 5); integrate, differentiate symbolically

7) Ability to reason logically: Given postulates, to be able to  
prov. Programs, ~~conjecture~~ conjecture theorems; Give a bunch of  
data, to be able to deduce info relevant to a particular problem.

The "laws of A"  
 Logic  
 Inhib. laws of  
 Algebra "can  
 be found educationally  
 to meet  
 Equivalency  
 predictive power  
 Can be found industry

8) To be able to plan & carry out a research program  
(Like "find cure for cancer" or "design better CPU hardware"  
or "find a better theory for physics".)

Req: .13 (6): These can be taught to TM inductively.

Req: .16 (7): " " " " " " " : An imp. Q is:

can TM learn to apply this reasoning to its own problems?

Req: .19 (8) I've worked on this problem some: Don't remember

if I solved it or not!

One poss. Big Ditty: I start off starting w. a "simple" T.S. @ from  
Algebra only. But it is likely that to discover or even use ~~the~~ k. needed  
heuristics, many more "messed up" knowledge will have to be had by TM.

$ln \equiv n!$

$\frac{ln}{ln} = \frac{ln}{ln} = 1$

.01: 207.40. not absly neccy at this pt., but put them in, because C want to know ~~if~~ but C know how to do this! : Also note 208.32

In particular, note 208.16 is (208.16R) ←

One apparently imppt. idea is - T.M. has to learn to "reason logically" - many hours involve logical reasoning. Since both logic & Algebra will ~~involve~~ both have to some kind of "logic  $\leq \geq$ ", ~~the answer~~ TM will have about the same confidence in its prodns. in either area. We can perhaps make some kind of Formalism for TM that is appt. to  $\leq \geq \infty$  - It is hoped that "Truths" obtained w.  $\leq \geq \infty$  will not conflict - since we would then have to know ratio of scores of different  $\infty$ 's!

(Difference betwn 2  $\infty$ 's might be imp. e.g.  $\frac{\infty_1 - \infty_2}{\infty_1} (= 1 - \frac{\infty_2}{\infty_1})$ )

The imp. idea here: That TM has to learn to "reason logically."

That there is a real distance betwn. TM learning Algebra (Math) & learning <sup>logical</sup> logic (aspect of Math) is key to use learn this Mathematical Logic in obtaining Probabilities.

**SN** Many hours will have to be spent by OSL. We could wait for 1 of "SSZ" to 2, but this would be wasteful of SSZ's. Also, it is essential that TM have good facilities for OSL doing OSL.

.19

So what I have to do, is write a TSQ in English; then ~~write~~ figure out to ~~it~~ needed (or "good" behavior) hours in English. Then figure out what sort of training logic ~~can~~ also help, but TM needs be part can discover/use ~~each~~ heuristic.

Perhaps try to find where I've already done much of it.

Perhaps Reread Original Proposal for Sol 89. It even had estimates of Time Scale of C.

But I ~~should~~ shouldn't be "Too Careful" in constraining TSQ! T. techniques supposed to work w. not-so-perfect TSQ's.

So in writing t. TSQ is "Analyzing" in English. I can use various amounts of "Heuristic Guidance" To start off, I just want to get a feeling for just what (i.e. how much) has to be done. Ideally in "steady state," it should be poss. to train TM using not much more than a TSQ that has been designed "IN English". - That if it doesn't acquire ~~some~~ a certain core. We accept the cc, I will analyse what occurred, ~~is~~ just ~~to~~ give a "hint" or give it (or teacher) what I think ~~is~~ is a relevant heuristic.

.34

I think latest TSQ analysis: 237.01 - 17; → 207.24  
205.07 - .90 206.28 - .90, 207.01 - .90; 209.01 (A)

$\frac{24421}{205.08} = 119$

D.H.G.!:  $205.08 = 14$

Main points: start w. ~~the~~ ~~maximum~~ 3 = ?

From 3 + 7 = ? ~~maximum~~ 3 = ? is solid early because score of

only a few <sup>numbers</sup> ~~numbers~~ that give nos. as output. That TM should notice that

"?" has always been a number, is right - ~~there is a hint~~ This seems to



Doing  $3 * (4 - 5) = ?$  would seem to be quite difficult at this point.  
 TM may recognize it w. MULT ) ; - in SUBC ) , but this is rather vague.  
 Trying  $\text{mul}(3, \text{sub}(4, 5))$  is a reasonable possy.

Similarly, it would learn  $(4 + 5) * 7 = ?$  and  $3 + (4 + 8) = ?$   
 ect:  $4 \text{ contigous } 4 * (8 + 3) ; (8 + 3) * 4$  to be hard.

Somewhere along this path, it should begin to do some "hyerorder" things by not trying that  $R$  over symmetric, simultaneously in its "rules" for various sub-expressions. Such hyerorder rules are 1 pc of corpus.

Also, when new kinds of problems are given, they ~~cannot~~ ~~learn~~ solve the new problem immediately or help speed up needed search.

What I'd like, is that at some point TM should discover what "parents" "really mean" induce a general rule for evaluating any exp. expression in infix notation.

O.K. so that would be an interesting TSO:

Another TSO: learn  $3 = ? ; 2 + 3 = ? ; 2 - 3 = ?$   
 $\text{solve}(x, x + 1 = 3) = ? ; \text{Solve}(x, x + 3) = ? ; \text{Solve}(x, x + 3) = -3, \text{ if } x \text{ is } 0$   
 $\text{Solve}(x, x + 3) = ? ; \text{ } (x \text{ is } \text{literal}; + ? \text{ is } - \text{ on } R \text{ case, } x + 3 = 0$

If may be way to get TM to learn mult & div first (?).

After TM learns to Evaluate any Alg. expressions, try teaching it solving linear eqns. - some "non-linear eqns. - many of this isn't quite clear. well, eqns involve some exp. Manipulation is neccy, but final eqn. is "linear" to be solved.

.24 → Perhaps I want to get TM to point where its using +, logic a/o work it out, to help find models for new problems.

.27 Long Range Q! Just how much work will it be to get TM to point where usually one can teach it w.o. getting into details about how TM is going to learn it! i.e. w to teaching a person?

This Q may depend on Domain: i.e. one might be able to do it in some domains, but need more training before it can be done in other domains

Probably Sub-goal .24 is a large step toward Sub-goal .27

Anyway, to get .24, I may not need a very large TSO: Even in simple problems, if one wants to work them w. very small CJS, one must use much "logical reasoning" = "Mathematical Analysis"

An imp. Q is how to get this Mathematical/Logical reasoning to arrive automatically, w. any special prms. on my part. → 216.01

The defn. of Adequacy of an English Soln of a TSQ. .05-.10

1/20  
Shaded  
o/n pad  
padding.  
(more pad to  
go.)

.01:211.40 : A possibl. Example of "Much Reasoning" is in the Substitution Heuristic used in soln. of Linear Quadratic ~~Equation~~ <sup>cube</sup> eqns. Also the "Planner" heuristic not breaks probs into "or", "and" naks.

This devises sub-goals.

.05 → **SN** [ have been a bit worried, recently, about mapping from English descr of t. TSQ & its soln. ] to a program (SW, HW). This shouldn't be too hard. [ If t. English soln to t. problem is Legitimate then there <sup>must exist</sup> ~~is~~ <sup>practical</sup> ~~is~~ <sup>probably</sup> search method (perhaps LS tech) to implement it. So return to t. spec & write t. TSQ's! ]

see 219.19

.10 → So .05 really defines t. Adequacy of an English Soln. of a TSQ.

Ok. So lets go back to t. TSQ of 209.34A: How "Complete" is it? — What needs to be added/changed to get us to satisfy .05-.10?

So start w.  $3 = ?$ ; T.M. has a bunch of functions available: at least idea ( $x \rightarrow y$ ), add, sub, mul, div. The input consist of 3 "things", 3, =, ? a "thing" is something that can be an input to a function. At this point, = & ? are not "things" because there are no functions that can use them as inputs.

For <sup>each</sup> t. specific "things" (other than nos.) that have appeared in the corpus we can define a function that recognizes it: Has "T" as output if input is that, "N" otherwise. This SW/HW idea gives some way to estimate PC of various functions (usually primitive functs at first).

We also have a function that <sup>recognizes</sup> ~~recognizes~~ Numbers; { It is the "no" of the "or" of all other recognition functions. } I may want a function that is T if some its assoc symbol occurred anywhere in the input string. If it does we can look at each position to see if it there.

Well, Ok. say we have all of these O/F functions: for the  $3 = ?$  problem, they could be tried at first level, but they would give "T or R" out - never a no.

Even better, I'll want a means for TM to recognize that a funct w. numerical output is needed — a Priority ↓ t. amount of search needed by a sizable factor. So TM "Notices" that output is always a No., then concludes that only funcs w. numerical output can be tried at first level.

Just how do we <sup>realize</sup> ~~realize~~ t. resultant PC of .30 → .31? What Mechanisms can I use? (I want to desc. t. Mechanism "in English" w. going into HW/SW details). → 218.01 spec

Perhaps cancel ship this "detail" at this point, but make list of those "reasons". When I have several, see if I can work out one a technique that deals w. several (or all) of them.

1	2
2	4
3	6
8	8
10	10

Second  
Sub b  
on final  
Ad!  
Microshanty  
script.

216.134 spec  
01: 216.40 : One ~~Approach~~ Approach: One has to produce "number".  
 probly, we find it has 2 (maybe been a "number").

That + - \* / have always had numeric outputs — we can give TM a pseudo corpus that tells it this — since ~~it~~ it is a "number", it wouldn't have much ~~SSZ~~ of this sort.

07 The discovery of t. "working backwards heuristic". This can be obtained 2 ways: ① purely empirically, TM notices that f. Macro function must have a terminal function that has numerical output, it <sup>requires that</sup> it ~~must~~ have a numerical output. TM would have to have acquired a needed concs ( "Vocabulary" ) before this could be "noticed".

11 ② Because needing a number for "sin" always has had numerical output" have large vary large SSZ, TM would consider using Logic (SSZ 200) on these statements. [Also, proper "vocab" needed before this can be done] <sup>"adequate"</sup> <sup>"concs"</sup>

14 The methods of 07 & 11 need partly t. some concs (Vocabulary) & probly. some different concs.

The maybe, 14 is it so true! T. main difference betw. <sup>deduction</sup> logic & induction is that in induction, one traces out all poss. paths — even those w. low pc. In <sup>deductive</sup> logic, most paths are of zero pc., so one doesn't bother tracing them out. In <sup>deduction</sup> approximation we will not trace out very low pc paths, so we can approach "Logic".

SN Say we are "telling" TM t. laws of logic & / or laws of Algebra. If this info is on "Advice Channel", it can be regarded as a "Hint" — in t. sense of reducing cost of searches for TM.

So: Ok.: We have given TM enuf info so that its find that "?" is "usually" numeric, but "+, -, \*, /" all are "usually" numerically numeric output. TM always constructs new concs using old concs & useful sub ~~traces~~ traces. In making these traces, it could "respect" any info that it may have on I/O of t. various operators.

28 Normally, f. Maps are constructed "Backwards" (R. L. in & output <sup>func</sup> operators first). ← ?

well we can construct them this way: Start by doing all poss. funcs w. derived output "Type", connected to all poss. legal input types.

Next, to add ~~new~~ our new function to t. "kinds", replace each input to t. function w. all poss. functions, & have t. input to that func, for all poss. inputs.

To insert (map kind), replace all input lines by all poss. funcs.

28 It seems to get a different result from the method of function generation that I used on (120.25 - 131.18), which builds up functions starting w. input lines. This method is not so good, if one a certain "Type" for output:

On the other hand, it may be that 28 is not correct — that it doesn't get all of t. functions w. given output type.

.01: 218.40



$F_1$  is the output function.

$F_2$  is the poss. additional forest to  $F_1$ .

$F_3$  is another poss. additional function to  $(F_1, F_2)$ .

Actually, this analysis need be done for usually no more than 3 or 4 functions, because the pc's <sup>become</sup> so low, due to 6. very ~~large~~ large no. of possys.

So draw this fore while (Note 143.20: Discussion of Symmetries Symmetries)

in forests, can ↓ no. of possys by ≥ 10x!)

The Present Problem: To understand how ① Hours are discovered

by TM: what form 6. discovery takes. ② How are these discoveries implemented in ↓ ~~some~~ cc/3 for L such? [i.e. How do we use these ~~discovered~~ "discovered hours"?

.12

I'd like hours to be in some "standard form" to facilitate their applic. 7.17

.13

**[SN]** In General "Types" of input/output of forests could much reduce no. of poss. combin. The formulae of 130.25 ff didn't consider this 143.20 discusses Symmetries; possibly ~~another~~ 2 ~ methods could boost for "TYPES": I'm thinking of using mainly 3 types Number, Boolean, ~~String~~ String

.17: .12 → Try to put this Q into as exact forms poss. : Exactly what is f. Main Problem Now?

.19 216.10

One <sup>Big</sup> Problem: (linked to 216.05, 10) 1 How are regys (x concs), compresses found? When do they are found, how are they ord. for prodn. How do these new found regys modify subsequent searches for regys (= compressa)!

.23

"Soln" to .19: "I've read all of f. regy found thus far" Try all poss. codings of f. Corpus in order of pc. When ~~some~~ store all significantly useful codings. (i.e. ignore all compressa not obtained)

A poss. Approx. to .23: We are considering only codings that are operators. So we have 2 conditional pd, betw. input & output. We start w. a set of <sup>primitive</sup> primitive forests (of perhaps = crip). We code <sup>cand.</sup> cand. operators as functions desc'd by trees. [I have to work out the details of the coding of these trees — I will try modify of "Z(41)". Hopefully, these trees can be desc'd in 2 pc order very to "4 off-man teach usque" (130.19; 142.01)

143.05 ff, 144.01 d.3 crosses • PSG's (phrase str. Grammars) as models for tree search. — derived vs. non-derived languages.

So, anyway, we list these cands in a pc order using a Huffman trick. Each function has a pc assigned to it, so we can do this "Huffman coding". Any significantly short code ~~in~~ for the corpus, becomes a newly defined operator (= function).

After defn of this new operator (we ~~are~~ any defining several of them in "l1 codes"), we have for each such new defined function, (20.01)

.01; 219, 40 - 2 code for v. corpus: This is a "2 part code". Part 1 is the "parameters" that consists of the primitives, followed by <sup>functions</sup> all of the definitions of functions (that terminates w. v. data of the last Macrofunc). This is followed by the domain of the corpus in terms of that last Macro Function: This last is in the style of 214), in which v. pc of any element will depend on how many times it's been used into code plus far. [ I haven't yet figured out how to do this in the ~~finite string induction~~ <sup>US Induction</sup> <sup>v.s. TS induction</sup> <sup>time series</sup> <sup>US induction v.s.</sup>

Del

Think of CFG's. - How the various pc's for choices <sup>strings</sup> get updated w. each use of them. I do want to write this up in some detail! This process was v. My not understanding the process, was a cause of much confusion about pc's of functions & "sub-functions" in both the coding of v. corpus & v. coding of new functions: sub-functions,

Finite lang  
US induction  
TS = 11

~~if I really work well only during hours~~ (i sometimes better going to bed?) Spend much of day properly problems so they are in form that's most easily worked on in Morning (I preferred)

Still, Much confusion in my mind about difference betw. Stochastic operators (function) & CFG. Well, one by Di.Cruce! CFG is a stoch. operator for a constant (invariant) 14 pt!

.18 One Try: Say we've coded v. corpus (a MTM corpus) using a string of definitions culled in a certain Macrofunc, Fo. We get a new bunch of f(x) pairs that don't seem to fit well. What do we do? : Well,

.20 ~~we try our operators in PC order~~ This would mean starting w. f. primitives & using each of the Macro Funcs: that worked in part of v. past TSQ. Actually, none of them works, & they all give a zero pc to v. corpus - so didn't go compare them. Next in order of PC, might be taking Fo & s/o other "Recent" Macro ops & <sup>MUTATING</sup> ~~try~~ them, by instantiating & substituting.

~~different funcs for sub operators~~ (substrings traces) within Fo and other recent Macrofuncs. ~~essentially identical to OSA~~

.27 Actually, MTM problems are always INV probs. - So maybe try Lynch. In this case, TM has to "recognize" the new kind of problem (recognition involves combining concs., just like any other problem.)

"Recognition" is a kind of "Categorization" which is an imp. kind of knowledge that must be acquired.

.27-.32 is a common approach to v. problem of .18-.20. We Try to find a minimal code telling how v. "new input" differs from all of v. old inputs. (One such way is the passage of time :) Actually, time may not be that "A.I.T"! The new (untractable) input may be identical to an input in the more distant past - but "Times change" - so TM has to adapt. One way would be by finding a new soln. for v. recent data, & give wts. to v. ~~old~~ old & new soln. - So we also not

"MCT: How to do every thing Right Every time." Title for ToM.

This changes it from a MTM to a NMTM problem!

0.08:220.40 100% sure of 6. new soln. T. referee wts with bias should bias more strongly toward t. "recent" soln., as time passes.

While 220.27-32 is, indeed, a common approach to this problem,

I do feel it is somewhat A.H. & I'd like a more General approach.

This is in line w. my writing a very simple <sup>common</sup> form for ALL RTM's problem types: "Modes".

It may be that my considering only MTM in 220.18-20 is where the trouble is. In general, TM is supposed to have this Very General Cond. P.D. that contains, stores, all of its "knowledge". <sup>including the entire "knowledge"</sup>

The structure Macro funct. sought in 220.18-20 doesn't contain enough info to be very useful for heuristics. <sup>Heuristics are usually "NMTM distributions" - i.e. pc's are not close to 0 or 1</sup>

Her., t. MTM d.f. of 220.18-20 could be (is) a part of the more complete P.D. of 10.

I think the P.D. of 10 is my simple, unified model for TM (imp.). It is t. P.D. that TM2 spends its cc "Updating".

But how does ~~my~~ my approach sol 89 fit into 10? Sol 89 was making new cond. concs by combining older, useful concs that were found to be useful. How does S89 fit into MCT?

This seems to be the right Q! In fact, whenever I get into trouble, I should always ask: "What does MCT have to say about this?" - or/ <sup>More specifically</sup> what does MCT have to say about: SAARB TSG's?

So perhaps SAARB-like try. & see what MCT says about it ... how it should really be done. T. General idea is that t. P.D. helps solve problems, & after each problem is solved (or even just "worked on"), t. P.D. is modified, to "contain" this new info.

So for t. ANL problem, we start w. our primitive functions, & means of combining them. T. functs themselves have PC's, as do ~~the~~ operators that combine them. This gives rise to a P.D. for all functions. They are searched in w. Cost order to try to find one (or several) that <sup>do ANL as far as we t. corpus goes.</sup> "Error Search".

How do we then Modify P.D.? Well, we add new <sup>to deal w. t. new examples that "Don't fit" t. old Macrofunctions.</sup> functs to t. set of primitives: but what pc's do they get?

Also note: in 28 we used an unconditional P.D. In 33 we <sup>need</sup> a conditional pd. One of the things t. cond. P.D. considers, is "what to do when we have to revise a theory". Given a "Theory Revision Situation" - we use a P.D. on techniques to deal w. it.

110

28

33

37

31 On to UNIVERSALITY of a PRIM. RECC. FUNCT GENERATOR.

01! 222.40: While 222.37 is close (or just what) we want to do, we may want to "Elementarize" (break into <sup>Tentative</sup> AND or OR sub problems, (that may or may not solve the main problem). { Remember that in breaking a task into sub tasks (AND/OR not) part of one's time is spent trying to (prove) various of the tasks are imposs.! }

**T** could be p.d. of 222.33 is the MCT P.D. It characterizes the entire corpus thru par, (as well as the techniques we've used to try to solve probs (which is new part of the corpus). Hvr., in this problem ~~the~~ discussion, I may not want to consider the entire corpus... but this is unclear just now.

Another point: Storing the cond trials as part of the corpus, would seem, at first glance, to be pointless, since the trials contain zero info: The trials are completely desc'd by the "stated TM" i.e. "Lsrch algm":  
- Hvr., the prog. assumes  $C \neq \infty$ . For finite  $C$ , it may be worth while to store certain info in the Lsrch (other than final results).  
An extreme (No 2 bit word) case would be storing very many of the short codes of the corpus, ~~with~~ the less short ones being good candidates for later "Theory revision". **[T. Revision Problem!]**

So T. Big Q is "How is the Big (MCT) P.D. (updated/Revised) error  $\alpha$  (successful) Lsrch? How will TM's subsequent behavior be modified? (More General Q).

Consider the early T.S. Q.  $3 \geq 2$ ? ;  $3 \geq 4$ ? : We could start w. a simple P.D. over a (potentially universal) set of funcs/functional. (Possibly a universal or Prim. Rec. Universal Alg.)

**NS** It is not clear what a universal Prim. Rec. Alg is: Perhaps if  $A(\alpha, X)$  is a Prim. Rec. algm,  $A(\alpha$  is the desc of a P. Alg,  $X$  is its argument), Then if  $U(\alpha_0, X)$  is the same func, implemented on Universal Machine,  $U$ ; Then for all  $\alpha_0, \alpha_A$  ~~the~~  $|\alpha_0| - |\alpha_A|$  is bounded by a constant that is a function of  $A$  i.e.  $U$  only. This would be the case if  $A$  were a Universal Alg.

Or, say  $A^1$  i.e.  $A^2$  are 2 algms that can generate all Prim Rec. funcs, Can  $A^1$  dominate "majorize" all generators of Prim. Rec. funcs i.e. not be universal Universal (Turing) Universal Function

31  $\Rightarrow$  Since the Prim Rec. funcs are effectively enumerable,  $A(N, X)$  could be Prim. Rec. Universal ( $N$  is index / number of func. desired), i.e. could desc. only Prim Rec. funcs. I suspect that one couldn't get significantly small  $N$  i.e. one!

1:36 Its not clear that my Prim. Rec. Machine is Universal in the sense of 31: but drop this for now

220: (22) consider the set of successful trials: 1) for  $3 \geq ?$  find the number in the input set? to the no. (Equality function) 2) for  $3 \geq 4$ ? 3 solns: ~~the~~  $\text{sum}(b, a) \geq \text{sum}(a, b)$  find 2 nos.  $a, b$ ;  $a \geq b$  " ? "  $\leftarrow \text{sum}(b, a) \geq \text{sum}(a, b)$ . } some PC for this 2 solns.  
1:57  $\text{sum}(b, a) \geq \text{sum}(a, b)$  else ?  $\leftarrow$  (2 only no. in input)  $\Rightarrow$  (224.0)

01: 223.40 [Unclear as to whether I want to include considerations of "?" being to be a number  
 = 1. Anal funct into Macroduct having numeric output. ("TYPE" info). The "Type" info  
 could be an invariable a counterpart of all symbols. ~~so~~ so each item has 2 sub params:  
 Type & Value. ]

05 Or I could let all symbols be same type, & let TM figure out about  
 "Types"

The .05 would making looking for "+" diff! TM, say remembers all symbols  
 that have occurred, so it can decide if they occur again. (i.e. so if "=" can be  
 x'ed into a Boolean funct. — By using "Types", I ↓ the no. of Params Tremendously!  
 This is because: no. of Numbers, → enormous! A way around this is to use only one  
 sample per example, & use 32 bit/integer. Even so, I'd want to give new randomness.  
 for each new example type.

Apr #3  
 #4

But I was mainly interested in running a ~~new~~ not-very clever TSC  
 Since my technicians supposed to work w. all

16 Speaking in general terms: After a <sup>new</sup> subcorpus has been worked on & ~~is~~ a soln.  
 for it obtained: How & by P.D. updated? (First), & params of old corpus exchanged.

17 dat BPD serend new corpus added to (B.P.D.) w. assoc. params.

19 Next TM<sub>2</sub> can work on ~~the~~ entire P.D., TSC to look for better regyl. Possibly a complex  
 recording, or  
 coding of code.  
 20 Can I use a sort of arby B.P.D. & see how the new sub TSC  
 21 expands & changes it?

22 My impress: I'm a TM working on MTM probs, there are 2 kinds? Noted Below!  
 of sub-PD's: One for Math probs — in which real orph is other PD's  
 used to guide heuristic search on Math probs & perhaps other  
 25 PD's used for NMIM-type problems.

To start .16-19 + (.19-24)R, maybe O.K. I'm not sure it  
 addresses .22-25

[SN] I had considered a usual Max of 3 or 4 functions to be combined!  
 but this limit could be much exceeded if I had a particular method of  
 combining functions that was often used. (This is a "Meta Programming" idea.)  
 One example is "loops", a combination of at least 3 functions:

- ① Counting function
- ② Main function
- ③ threshold of termination function (Boolean)
- ④ Initialization. (Unclear how ④ is a "function" — it could be an input)

36 Haven't checked on Peter's form. It may be that ① can always be  $j = j + 1$  &  
 initial value can always be 1. So 1. loop functional has input n & function ②  
 Essentially, what we do is to do function ② and add another argt. to it, "n".  
 If ② has  $n$  args, we need to define function in

$$\vec{x}_0 = \vec{z}_0 \text{ (initializ.)}$$

(2): Essentially,  $\vec{x}_{i+1} = \vec{f}(\vec{x}_i)$  repeat n times.

.02  
usually  
ext 224  
CUCMA.

A big Q is 224.36: do I need an arby "counting func" w. an arby form of "stop" threshold? — This would be useful in finding out say, when an approx. procedure should stop. — But do we need Pcs for Prim Rec. Funct? — See (recons) "Introdu. to Math Meth".

.02 with actually 2 central Q: 1. Q is: to what extent is 224.16-19 "adequate"?

Re: 224.16-19: Consider various possl. "Solns" to TM's problems.

Can each discovered Recpy be put into 224.16A form?

Can what TM found from f. Soln. (f. Solving process) be put into 224.16 form?

In general: 2 parts: ① Soln of problem ② Info from f. Soln. process.

An extreme example: say f. problem is  $\sqrt{2} = ?$  One persol soln is 1.414...

Another other part is how this soln was obtained: 1.414... with a stored as

a soln to  $\sqrt{2} = ?$ , since this problem may occur again. Whether or not it is stored depends on cc of storage & cc of computation. Expected time before info will be needed.

### INGENERAL in 224.16: This can be done in many ways,

.18 each w. its "own" of completeness". In one way, <sup>t. B.P.D.</sup> ~~the~~ ~~prim~~ consisted of a set of functions, each with its own pc, & a set of combining rules (functions) each with its own pc. ~~The~~ ~~MAIN~~ ~~idea~~ <sup>in 224.17</sup> (first) f. pc of Pcs

.22 func & functions are ~~revised~~ In 224.18 (second) New Funct (& perhaps <sup>NEW</sup> functions) are added, each with its own ~~initial~~ pc. The "funct" will be Macro Funct used in soln steps: <sup>Funcs. represented by</sup> ~~subnets~~ ~~Pcs~~ ~~are~~ ~~used~~ ~~frequently~~

.25 (These "subnets" — I haven't found TSO in which they are useful & Pcs is a source of "increase") Re: New functionals: I don't know if Pcs is necessary, or if so, how they would be discovered.

.28 In (third) 224.19, the revision of t. enters B.P.D. Code: This also needs much work: It may involve discovery of "New functionals" <sup>1</sup> (.22), <sup>1</sup> (.25).

Anyhow .18-.28 is only one way to construct & update a B.P.D. How a well defined, how efficient, how complete it is, is unclear at present.

.18-.28 is an "Eng" dcm of <sup>2</sup> ~~the~~ ~~func.~~ ~~system.~~ I could go into more detail, or Generalize it more. — Make it Yagum: More Englishish!

A MAIN Q: Can all the induction methods I can think of, be fitted into this (.18-.28) Model?

AN APPROACH: Work some (Noman-w.30) <sup>problems</sup> ~~problems~~ & see if I can fit the tech reqs into (.18-.28).

**[SN]** Consider folg. Problem: How would TM have ① Motivation ② Ability to work it: Given  $f(x)$  from  $a$  to  $b$  is monotone ↑, to find  $\int_a^b f(x) dx$ :

Discover Simpson's rule: Bounding  $\int$  betw. upper & lower limits.

③ Could TM have motivation & skill to discover higher order versions of this algon when  $f'(x), f''(x)$  were monotone on interval? ~~then~~

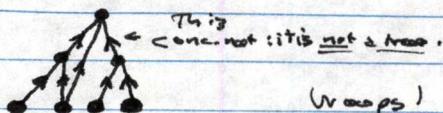
Ans: Find order of approx to use v.s. no. of pts evaluated  $\int \in \epsilon$  was then.

Would TM have to have a kind of "AM" like "motivation" to work on such problems? For  $f$ : initial problem, to. Problem definition might be "find  $\int_a^b f(x) dx$  within  $\pm .001$  & prove this is correct. (or make it very likely that it is correct).

Perhaps study "History of Math" to get ideas of <sup>order of</sup> sequences of concepts.

A posssy, is that  $f$ : function nets I've been considering, ~~are~~ are not always able to ~~solve~~ desc. all solns. to problems. If not, then concs are more general than functions, &  $\int$  can make desc. of problem solns as "conc nets" (as in Sol 89). (The updating of  $f$ : params, will be  $Kos$  w. function trees)

Whoops! There's a big difference betw. a function (which must be a tree) & a conc, which must be a "net" of concs, but a conc net is somewhat more general than a tree! — Tho all function <sup>trees</sup> are conc nets, all conc nets are not trees.



.22  
.23

Whoops! A function net need not be a tree either! (.22-.23) Could just as well be a function net!

So it looks like conc nets & function nets are isomorphic.

Nieder need be "TREES"

The idea is that any idea ( $\equiv$  conc) is formed by combining other (earlier) concs. (This is an English statement / desc. of  $f$ : process)

If  $f$ : concs have simple unconditional pc's, it's easy to update those pc's: They are independent & are obtained exactly as in Z(4) — so pc's are no. offines each conc. has been used in ~~the~~ solns to problems that have been accepted.

In  $f$ : more general case, they are not "indip" but are conditional pc's:

— T. conditions can be truly complete. I guess updating indep. conc. pc's ~~is~~ may be simple (viz Z(4)) ... but updating cond. pc's seems much more diff.

On second thought, updating (function/conc) nets may not be so trivially covered by Z(4) techniques!

01: 226.90. Consider Function & Conc. Separately.

First, Functions: To Construct a function: Start at top (terminal)

Function: Using a corpus of successful Macro Functions: Each Funct has a pc of being chosen at "top funct"; — but we will, at first, want to pool this info, because, at first, SSZ's are small. So, say each functor connects to k inputs, has a certain pc (initially, say, they are all the same). After 1. first Funct is chosen,

Its inputs have to be chosen, a way, too have to share d.f. over all of the functions <sup>(Macro-Funct)</sup> <sub>(inputs)</sub>

So, given any Macro-funct, as well as the assoc pc's of the funct's <sup>(the pc's)</sup> <sub>(inputs)</sub>, we can assign a pc to its construction of that M-Funct. ( $\equiv$  Macro-funct).

These probability assignments can be done exactly like in an advanced version of Z14f, with ~~long~~ "long" definitions.

Def

Def

.15

.17

.20

The pre-corpus, consisting of the M-inputs ( $\equiv$  inputs to Macro-funct) followed by the primitive functs. We then define our first funct. It can be one of the m-inputs, or one of the primitives: If it is a primitive, it is followed by its inputs, which must be m-inputs.

The next function can have as inputs, any previous function output, or any m-input. (Loop / Recursion) to itself. The pc. of each choice made  $\equiv$

$\equiv$  (no of possible identical choices) / (no. of possible legal choices)

So, if an input was  $F_3$  a  $F_3$  occurred  $N_1$  times in previous code, & there were  $N_2$  legal choices that could have been made,

its pc is  $N_1/N_2$ : This is same as normal Z14f coding. (also  $\equiv$  "Laplace's Rule")

.15-.20 Tells how to code/generate pc of any M-funct.

This pc will be indep of the pc's of any M-Functs that this m-funct does not "refer to" (This does not "refer to" in this sense of that M-funct — There can be parallel decns of this M-funct, that use entirely different M-functs in their decns).

The isomorphism of concs & functs can be used to assign pc's to concs in a formally identical way to M-funct assignment of (.13-.20)

In a Conc. net, each node in time is a "combination rule" w/

Several inputs: r- inputs are "lower order concs."

.30

.32

In funct. nets: Conditional pc's can be obtained empirically by case counting,

but I suspect that this will not give much info usually, since SSZ's are

too small: probably could pc's will drop from "reasoning", analogy, act.  $\rightarrow$  (228.0)

Re: (.13-.20) (T. method of): That gave to mathematical value of pc.

To actually get it, each Funct would have assoc. w. it, a  $N_1$  &  $N_2$  value (.17-.20)

So we could rapidly compute (& update) its pc.

(.13-.20) suggests a formula for functs & concs. Since funct.

analysis is simpler than concs., Do function problems first. — But the analysis

will apply exactly to same to conc nets. One big remaining problem is

(conditional pc's) (.30)

**.07 Present Branch of Activity: Put this on STACK**

.01: 227.40: Re: Analogy (227.32) This is common structural properties of concs. Usually 2 conc will have several possi. derivs. Only using certain of these derivs, will "structural similarity" w. another conc. be recognized. So holding "parallel codes" can be useful in this way. Also, if we suspect that 2 concs may be analogous, we could examine ~~the~~ a (for active codings of both of them.

.07 **So: Maybe do this: do Alg. Imp. using only 227.13-20 (if possible) to simple cond. pc's of 227.30) See how far I can go w.o. needing more complex concs, <sup>than "functions"</sup> or more carefully constructed cond. pc's.**

.10 Some Q's: will 227.13-20 work for only MPM funcs, or will it also work for NMPM funcs (stochastic operators)? Note that B.P.D. is a stoch operator. <sup>229.18 BEF</sup>

.10 is an interesting Q! → Because it deals w. a confusion that I may have had betw. the pc of a function (which can be deterministic or stochastic) & the ~~the~~ params. to deriv. the cond. PC of a Stoch. Operator. → See 227.19 to at least

I usually consider 2 kinds of probabilistic operators/derivations:  
1) T.S. probn. (regression) (symbols &/o numbers)  
2) F.S. probn. (languages) (called "Symbolic Regression" by Koza) <sup>stochastic</sup>  
229.30 for discn: I think some of these were complete soln. to the ~~problem~~ problem!

.16 Give Examples of stoch operators I may be able to discover using models like 227.13-20. Well, there is, for T.S. probn, ZCF, w. Wolff's form (of ~~reversing~~ <sup>breaking thru</sup> every once in a while). Note that this is a coding method, & doesn't ~~not~~ directly give a prediction operator.

.17 The T.S. probn method I have of defining all past fixes of a corpus, & giving a wtd sum of their probn., is closer to a stoch. operator.

It would seem that the method of P ZCF could be applied w.o. much modifi, to a corpus of unordered finite strings (a "language") - (Also I have all these ideas on PSD discy)

Every BIG Q in all of the large. To what extent will it be able to deal w. the "Scaling Problem": The ↑ in no. & variety of available concs; the necessity of having more (cond. pc's) for the concs to narrow their pc's down to the application in which they are to be (presently) used.

So: How to make a T.S.Q "Acceptable": I have to know how each new needed conc, is derived from older, useful, concs. Also, I have to have cond. pc's for these sub-concs, to show why they were likely to be tried as components in the (present, relevant) ~~situation~~ <sup>situation</sup> 187.33 ff

.36 I think an idea of a "ob-op" <sup>operator</sup> ~~operator~~ was not forgotten cond. pc's: One way (not the most general) to get them is by building up a set of "ob" concs that build on one another hierarchically, to be "categories". These "categories" are then "correlated" w. the of operators

Aug 3<sup>rd</sup> (k cof → 2936 136  
Lofc 3860 179  
Puzzles 3854  
of Photography  
These operators)

.01 So we can know under what cond<sup>s</sup> (its more likely) that we should try these operators.  
In general, the rate of growth of the "OB" vocabulary, (conc set) must be at least as rapid as the growth of the "OP" conc. set. — These rates can be "served" by TM<sub>2</sub> toward approx equality. One signal that there are "too many OPS per OB" is that the <sup>cc</sup> of search for acceptable ops is too high. — (This there could be other causes or this last diffy!).

Re: 228.07-17: This problem needs clarith. I don't have a clear picture of how discovery of stock ops is done: how "categorization" (concl. pcs for search) fits in, etc.

I may want to do a good review of: A more detailed descn of just how I expect this Prelim TM to work.

Probably best: outline how non-stock ops found, first: Random (w. a few kinds of stock ops: (228.16-17)

On to coding of a seq. of MTM problems: (solns. are functions)  
The TSA is A, B, C, D, (A is a set of examples of a function.  
Given A, the (operator) soln is FA.  
"A, B" " " " " FA FB where FA is a descn of operator in terms of prim. functs.

"Similar sub-trees" in many cases — coded by <sup>similar</sup> ~~operator~~ string

FB is a descn of two parameter in terms of prim. ops at FA. FB solves (A, B)

.22 **NB** Even w. only 2 functions, FA & FB can have common sub-functions  
.23 (≡ sub-trees) that will ↑ pc of t. coding.

.25 Given A, B, C, FA FB FC; FC is a descn. of an operator in terms of prim ops ≡ FA & FB. Also, the remark of .22-.23 holds even more strongly for the code FA FB FC than for FA FB. (More likely had of (above-threshold-frequency sub-trees) in a larger corpus).

.29 When common sub-trees are found, they may be added to t. function list (w. proper assoc. pc's) for t. construction of new trial functions.

{.22-.23; .25-.29} seems to clarify a lot of my confusion and unease about this lect in my SAARB TSA.

I suspect that the no. of ~~examples~~ new example types in the SAARB TSAs was far too small for t. effect of .22, .23 & .25-.29 to be observable. observable!

Also Note: It is poss. to "not need" the ability to detect sub-trees, of .22-.29 if one puts examples in t. TSA's that use these sub-trees as solns. (No! In present system, this would not work; Even if I gave you a problem which a particular sub-tree was a soln. (say t. sub-tree was fo). Then fo would never be a M-funct. — We would (230.01

of 229.40 have to have an Ob recognize when  $F_0$  was relevant, & have  $Prig(\mathcal{O}b, F_0)$  object, & found (added on) to ~~the~~  $M$ -function. — Or have a general reformulation (total code revision) to fit  $F_0$  onto  $F$   $M$ -function. But in general,  $F_0$  could never (by itself), be an  $M$ -function (unless it was a  $F$  soln. to the first ~~largest~~ set of probs. in the  $TSQ$ ).

In fact: I had residues of teaching TM definitions (in Algebra) as always an important part of the  $TSQ$ . The  $Prig$  could, indeed, simplify TM's learning of simple cons: I think the mechanism of finding "common traces" [Or much ~~more~~ more diff: OSL of such cons!] would be easy. ~~to~~ better TM could use those cons in solving new problems.

T. Main TROUBLE w. OSL, is that it requires either an enormous amount of searching (for functions), or some kind of INTRO-RETRIEVAL — ("associative" memory).

One approach to the OSL problem would be to look at cases of subtraces that I'd want TM to find, & try to find ways to ~~do~~ <sup>either</sup> ~~do~~ such ~~by~~ <sup>creative such</sup> ~~by~~ ~~some~~ ~~hardware~~ ~~method~~ to ~~cheapen~~ ~~associative~~ ~~such~~ — or whatever

Case Based Learning is OSL, but I think it models the conscious aspects of the process only. There are probably many strong, idiosyncratic, (individualistic) techniques of categorization, association, but are not "conscious" — perhaps many kinds of "Analogy" (= Structural Similarity).

One kind of OSL that may be common: Say I give TM examples of <sup>"named"</sup> ~~a~~ ~~named~~ cons. to learn ("Definition lang"). The ~~result~~ ~~of~~ ~~the~~ ~~learning~~ ~~is~~ ~~that~~ ~~the~~ ~~TM~~ ~~has~~ ~~learned~~ ~~the~~ ~~cons~~ ~~that~~ ~~are~~ ~~learned~~ ~~in~~ ~~its~~ ~~own~~ ~~way~~, occupy a special ~~position~~ ~~in~~ ~~the~~ ~~resultant~~ ~~M-function~~. When new problems arrive, TM looks at those positions as being good cons. for OSL.

(a mild Gen. of 22)  
An alternative approach to OSL: That the  $M$ -functions are normally "perturbed" to some extent, so we do have  $OBS$  &  $OPS$  & correlations between future — So TM could do a search over all ops that had a highly correlated Ob in the OSL spec. (i.e. "which track (ops) have been useful in the past"?)

An elementary  $TSQ$  that could be very revealing! :  $M$ TM  $TSQ$ , small amount of simple (long Gen ANL). Then we teach it a data: Then we give it a problem in which that data would help solve it. This is OSL, & I am concerned w. the mechanics of how TM would deal w. it. I think the problem is easier than looking for common sub-traces — because there are many many sub-traces to look at — in this Case Based lang, OSL, we only search EXAMINE a much smaller part of the corpus for relevant cons (I think!) (231.01)

.01: 230.40 In general, Long definitions involve creating an OB. (func. w. Boolean Output).  
Normally, just long a definition is not very useful in itself. It can become a useful OB,  
only after it has been correlated w. corresponding OPS. (or corresponding op.)

**SN** I have been considering only MTM problems that were "instantiations" —  
as opposed to problems involving a sequence of operations: usually obs  
followed by ops: The obs told "what to do"; the ops "did them".  
Or, we can think of a "ob. of" combination as a single OP, & just have  
a sequence of ops. # # # # #

Re: Long "Definitions" & OSL: If an OB has ever been useful,  
it is a Cond. for OSL. Hvr, certain "Utilities" are more useful than others.  
Useful in a taught "Definition" will have a higher probab. of being a Cond. for OSL.  
Hvr, in general, when a problem is presented to TM, all of the obs that  
TM has (and, are applied to it to understand it (the problem) in as many  
possible ways as poss. Altho the no. of OBs that TM has will ↑ (perhaps  
linearly) w. time; i. (amount of time) needed to find a match, will probably  
↑ much more slowly.

**.19** In the theory of OB recognition as simple sub-string  
recognition! That an OB is represented by a string or set of strings.  
To recognize a subset of a set of strings in a longer string, is a  
well defined problem. The Cond. strings can be in lexical order.  
So recognition is like my "soln" of the DNA sequencing problem,  
(use of B trees); Other relevant methods: Zako Coding,  
Hash coding (see Knuth's Volume 3 on this last — or perhaps he  
has tools to deal with problems directly related to the problem of **.19**)  
Maybe ask Simon! Ask Alex.

Zako Coding  
Hash Coding  
See Knuth for

**.19** occurs in Zako in reversing the corpus.  
Since .19 appears to be an impl., often occurring operation: perhaps  
Special N.W. can be used. For Decryption such string matching N.W.  
is available — but I don't remember the N.W. is always reversed w.r.t.  
"Moore's law": A large amount of Parallelism can be used, &  
of course, any very large computer will be helpful (if feasible).  
Hvr, Obs can be Boolean combas. like AND, OR, NOT.  
Skill, recognition of the components of the Boolean Expression, can be done  
via **.19**.

Also, there are hierarchical means for recognizing OBs. — so  
2 parts of a ob is recognized, so a large set of conds are  
now narrow "super conds" — which narrow down the problem —  
narrowing down

01: 23/10: Another technique for Ob recognition is that used in LZ coding.

(very fast & very "cheap" very little RAM needed!)

— Now, in contrast to LZ, I would also store info on how many times each substring occurred.

So! 1. OSL problem may not be so "computationally intractable"

↑ ~~more~~ <sup>more</sup> ~~than~~ <sup>than</sup> a bit simplified! In many cases, an OB is

far more complex than just ~~some~~ <sup>certain</sup> sub-string matching. I.e. to recognize that a ~~substring~~ <sup>certain</sup> substring is an equation, or that it's a linear ODE,

etc. is certainly more complex than string matching! A more realistic Model would be Pyndomianism — in which each OB looks (call) for things that are "a case of it". A Q would be 1. cc involved in this.

Also, whether one might not be able to save cc by doing sequential testing for categorizing.

Do a bunch of Examples of Definitions (and perhaps

~~other~~ other forms of concs. that have to be found by OSL. Go further to long of 1. conc. is ~~1. conc.~~ <sup>later</sup> applic. of 1. conc.

Normally, we give TM a new chunk of corpus (≡ "sub-corpus"). Sep it learns to match probs of 1. corpus; ~~then~~ <sup>even w.o. recognizing 1. new sub-corpus,</sup> this problem solving will much pc of coding. But next step is to "recognize" 1. new section of corpus. This is an "Ob Job". — ~~probably~~ <sup>presumably</sup> made much easier if somewhat to many concs have been (and as "definitions".

→ How to use Neg concs: We just have to categorize 1. input into 1 of 2 categories. TM assigns pc's to each category: 1. conc is max value of  $\sum P_i$ ;  $P_i$  being 1. probly assigned to "Rite" category.

O.k. so: Defn. long ~~with~~ <sup>with</sup> problem is given:

α, examples; Def. "Say this is format for learning that example is a case of α. ~~then~~ TM is then given queries of form ? , examples; Def.

→ or perhaps Def, α, examples, ~~then~~ <sup>then</sup> "then Query is "Def, α, examples; ?".

Say TM finds Ob<sub>α</sub> that gives rise to answers for the [examples] sub-corpus.

We also have to tie the Ob<sub>α</sub> to "α" and "Def": Assoc. w. α is Def are Boolean operators that recognize them, B<sub>α</sub>, & B<sub>Def</sub>; so 1.

final operator is Ob<sub>α</sub> ~~and~~ <sup>And</sup> B<sub>α</sub> And B<sub>Def</sub>. (I've omitted some details, here).

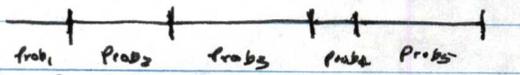
Say Op<sub>M</sub> is 1. previous M-function — so we want 1. new M-function to be Ob<sub>α</sub> ~~and~~ <sup>if</sup> B<sub>α</sub> and B<sub>Def</sub>; also Op<sub>M</sub>.

In general, 1. format 1. M-function (at first) will be ~~2. 1. 2. 3. 4. 5. 6. 7. 8. 9. 10. 11. 12. 13. 14. 15. 16. 17. 18. 19. 20. 21. 22. 23. 24. 25. 26. 27. 28. 29. 30. 31. 32. 33. 34. 35. 36. 37. 38. 39. 40. 41. 42. 43. 44. 45. 46. 47. 48. 49. 50. 51. 52. 53. 54. 55. 56. 57. 58. 59. 60. 61. 62. 63. 64. 65. 66. 67. 68. 69. 70. 71. 72. 73. 74. 75. 76. 77. 78. 79. 80. 81. 82. 83. 84. 85. 86. 87. 88. 89. 90. 91. 92. 93. 94. 95. 96. 97. 98. 99. 100.~~ <sup>2. 1. 2. 3. 4. 5. 6. 7. 8. 9. 10. 11. 12. 13. 14. 15. 16. 17. 18. 19. 20. 21. 22. 23. 24. 25. 26. 27. 28. 29. 30. 31. 32. 33. 34. 35. 36. 37. 38. 39. 40. 41. 42. 43. 44. 45. 46. 47. 48. 49. 50. 51. 52. 53. 54. 55. 56. 57. 58. 59. 60. 61. 62. 63. 64. 65. 66. 67. 68. 69. 70. 71. 72. 73. 74. 75. 76. 77. 78. 79. 80. 81. 82. 83. 84. 85. 86. 87. 88. 89. 90. 91. 92. 93. 94. 95. 96. 97. 98. 99. 100.</sup>

- 1 If ob<sub>1</sub> Ran Op<sub>1</sub>
- 2 If ob<sub>2</sub> " Op<sub>2</sub>
- ⋮
- n If ob<sub>n</sub> Ran Op<sub>n</sub>.

See 235.16 for the construction 234.01

.01: 232.40: T Form of Soln. of ~~tasks~~ 232.37-40 is a.k.a. for a certain type of Corpus: One that consists of a sequence of "separate, clearly defined, problem types."

.02  I think that each of these "problem edges" gives TM<sub>2</sub> some info about when to spend much time on a "single problem", rather than the entire past corpus is expected future corpus.

This form of Corpus is quite "restricted" but none, & less, impt., difficult problems can be put into this sequence. A big Q is: Can I put the Understanding of English text into this formalism?

.08 Superficially, Obj: can be a device that counts the no. of probs that have occurred this far. — but I can outlaw this by making TM regard the problems as "unordered". — by giving TM no functions that could detect this order. On the other hand, I may want TM to be able to detect "Recency": So if I teach it a date, then in the near future of that date, it will expect problems using it. (This is a rather broad "hint" — perhaps an "inverted one.")

I probably see anyway so that TM will ~~not~~ cannot do .08: — but I'd like to know just what <sup>other</sup> restrictions on TM's capabilities this would imply!

Actually ~~if TM did .08, it would be unable to solve new problems!~~ In fact, the soln. format ~~of 232.37-40~~ 232.37-40 is also very limiting! If I give it a new problem that is not <sup>of the same type as</sup> ~~any of its training problems~~, it will not know what to do! — Yet, after

.22  $\rightarrow$  it has solved a seq. of diff't problems, it should in some sense, be very smart!  $\leftarrow$

.24 Well, look at it this way: Say TM has worked to T&Q up to a certain point. We then give it a problem: "string?". How should it best get a P.D. for "string"? Well, presumably it tries to get short codes for "string", —  $\alpha$  being various poss. continuings of "string".

.28 Actually the situation at <sup>.28</sup> isn't so different from the situation when TM is given to first problem examples of a new problem set.

In .27-28 TM has to get a psm. to produce  $\alpha^T \beta$  (where  $\beta$  will be eventually replaced by "?" in the query aspect of the lang.) ...

.33 Well; 2 comments: (1) If a person were given a totally new problem under these circumstances, he wouldn't know what to do.

.34 ~~TM~~ T&Q given to TM was really of the form  $[Q_i, A_i]$  — but it was broken in to distinguish the <sup>subsets</sup>  $[Q_{ij}, A_{ij}]$  "j" is the name of our subset.

Consider the T&Q: Solve linear eqns, Solve quad eqns, Solve cubic eqns. We can consider this seq. as 3 subsets or 1 long seq. (235.0)

9.13.00  
Joyce  
783 8785

105 : 234.40 i.e. we can use the info about the 3 divisions or not. In the latter case, we write regard them all as "equations" to solve.

Also, even when [redacted] TM clearly uses the structure (234.02L) and the recognition Ob, 232.37-40, we can regard TM as solving 1 category of problem, with 232.37-40 being an analysis of the problem that tells TM what to do. — Hrr, I guess "232.37-40" is a poor analysis of the problem: it doesn't tell how to extrapolate itself into new domains: It is rather A.H. (Given Pro it has a lot of "learning in it" 234.22).

110 : 234.34 230.33-34 may be a nice idea! — But unless TM has been specifically taught to generalize input analysis, it will not be able to do it — it shouldn't be expected to be able to do it!

So, one Q is: 234.02L is a desirable structure for long: is it done get into unit (234.22) even w. the soln. format 232.37-40:

Can we somehow use that form to get more useful long?

116 Allen Serious Criticism of 232.37-40 soln: T. search for OP's: i. such that Ob are separate & not related: Normally, I'd like to input to create a cond. p.d. for the search of OP's: This should be cc of such tremendously! It's a really broad area for creation of hours! So: while 232.37-40 write work for a relatively small corpus, it would not have enough hours in it to scale up to a large corpus.

As the corpus grows, the no. of concs available grows, — we may narrow down of the search that would be obtained by "looking at the problem". — (236.16)

24 To the extent that 237.37-40 doesn't "top line" on MCT, it's deficient

26 Ideally, TM should use info on past (correct/relations) before Ob's assoc. to OP's, to help in each new search for an OP.

27 One way to do 24-26: After TM has (using 234.02L & 232.37) done a reasonably large corpus of example probs., TM should try to find useful (predictive) (probabilistic) relations, betw. the OP's & their corresponding obs. They "scales"

29 O.K. — Since the corpus is small when one just uses (232.37, 234.02L) Later, one really needs the relations of 27-27 to the least of such.

Unfortly, for a infant TM, the relations of the sort needed in 27-29, may be too difficult. — It may be wiser to put this in a A.H.

Another way to deal w. this: Use the strict 232.37, 234.02L ~~TSQ~~ form, until TM has acquired a set "hints" to do induction required in 27-29. — Hrr, unless one has very great IPC (number of bits/sec) it may not be practical to do this, because before TM is smart enough to

do 27-29, it will run into "scaling problems" — I could do it.

partly BH thing of 33 to help — to avoid need of super-hy IPC. Equiv. to A.H., would be different degrees of BROADNESS of HINTS.

236.01

.01: 235.40 : So, OK. Say I have this set of ~~data~~ [problems, ob-op solns.]  
 .02 Def corpus ~~of~~ solns. of  $f$ . "Simplified TSO" (of 232.37-40, 234.02L)  
 .03 For this set of pairs (of  $\cdot OIR$ ) I try to find a primitive operator (as  
 in 235.27-29) to  $\downarrow$  f. p.c. of that set of pairs. I could do it  
 in an operator form of solving  $[Q_i, A_i]$  in which I assume no info  
 .06 in  $f$ .  $[Q_i]$  set.

So .03 ff sounds fine: Note f. stuff on by **IRC** is "Hints"

at 235.33.40  
 T. original problem set (TSO) "STSQ" was a  $\sum [Q_i, A_i]$  form,  
 w. "clumps"  $[Q_i, A_i]$  ("j's a clump name"). So we ended up w.  
 .11  $\sum [Q_i, O_i]$  & we want to extrapolate this so it will work w.  $Q_{n+1}$   
 T. problem of all is just like any other  $\sum [Q_i, A_i]$  prob, except that  
 up until now, I've been doing MTM prob & this one is NMTM (primitive). **OB**  
 In .11, I ~~should~~ be able to use  $O_i$  w.o. to associated "recognizer" for  
 the "j" group.

.16 hours This gen. ("M<sub>2</sub>-like") method is also useful for success probably  
 into f. Lstch, to deal w. "Scaling" - it deals w. 235.16-23  
 What I'm doing in .02 is a "receding" of f. soln of  $\cdot OIR$ .

STSQ of .02 does give a legit. code for it's corpus: Th. code is one  
 .20 single final M-Funct, along w. f. recognizer  $O_{b0}$  of 232.37-40.  
 Hvr, this code can be much compressed! **.01** is one way to do it.

The corpus + the code of .20, ~~allows~~ can create the data string of  $\cdot OIR$ .  
 From  $\cdot OIR$ , any stack operator that can set's code rd of solns. from  
 problems as input, could  $\uparrow$  f. p.c. of the M-Funct of .20. One way this works:

Say we ~~are~~ are able to  $\uparrow$  the p.c. of one of the prob. solns. pairs of  $\cdot OIR$ :  
 then the p.c. of f. final M-Funct is also  $\uparrow$ , since the p.c. of f. final M-Funct depends  
 on ~~and~~ the p.c. of each previous M-Funct. If all of f. component M-Functs  
 have their p.c.  $\uparrow$ , the final M-Funct has its p.c.  $\uparrow$  ~~even more~~ (perhaps  
 necessary final M-Funct is  $\approx \sum$  of each of all component M-Functs.

How the Stack operator  $\uparrow$  p.c. of component M-Functs: It looks at  
 the problems & makes a kind of rd. on possible solns. This rd. can be  
 very direct, or it can work by making narrower rd's for the functions  
 that ~~are~~ components of solns. (These "conditions" can be on the  
 to partly-constructed ~~stack~~ function for solns.) - in either case, the  
 .35 p.c. of solns. would  $\uparrow$ .

Next, I want to go into more detail on f. "entire system":  
 .37 First, we have this set of pairs of  $[Q_{ij}, A_{ij}]$ . "j" is named subset of  $Q, A$ 's of  
 common "soln". At first pass we do  $[Q_{i1}, A_{i1}]$  first: we do an Lstch  
 .39 over primitive funcs to find  $\exists f_i \Rightarrow f_i(Q_{i1}) \approx A_{i1}$ . (Since this is at first 237.01

.01: 236.40 : a MTM to  $Q$ , "2" "3" = " in 236.39)

↑ When we solve ~~Problem 1~~, we go to problem 2. We solve it by Lsearch, using primitives +  $F_1$ , to obtain  $F_2$ . For  $t$ . entire corpus  $\{Q_{ij}, A_{ij}\} j=1,2$

.04  $F_1$  works about  $\frac{1}{2}$  times,  $F_2$  works about  $\frac{1}{2}$  times. It is, over 2 stochastic Operator: which we try to improve, by finding operator ~~we~~ can look at or  $Q_{ij}$  is total  $j=1$  or  $2$ , so it can't all be  $F_1$  or  $F_2$  is applicable.

.07 We then do  $\{Q_{ij}, A_{ij}\}$  for  $j=3$  and incorporate it into a Grand Funct ( $\equiv M$ -Funct) as in .04. ... we can't have ~~it~~ w. hierarchical values of  $j$ , unless cc of solns is too big: They are too big, because we have too many functions to construct our new trial function

.12 from — a these functs will have about same pt.

.13 Nexts we have to go into phase (236.01 - 206): We want to find

.14 of alternatives in the code for the operator that does  $\{Q_{ij}, A_{ij}\}$

.15 [SN] Perhaps before we go to .13: In the soln. process of 236.37-237.12 I had been thinking of just using functions that were primitive or were  $F_j$  type of Routs, or Obj type that identified  $j$  of  $\{Q_{ij}\}$ . I think I will need more: I will need simple OSL. Also, OSL (a MSL (Multiple step ~~something~~ lang)) is ~~something~~ learning from subnote ( $\equiv$  sub functions) .....

[SN] TM could easily have means/criteria for "Soln to eq"  $\text{Soln}(X, X+7) = -7$ ,  $T$ : How would it go about solving "Soln(X, X+7) = ?, T"? IN FACT, any INU problem can be put to TM in this form, in the best way to solve it is Lsearch (if TM has proper heuristics!)

[SN] Perhaps make "Graph of  $M_j/P_j$  in TM work, so I know where to go, & what needs be done.....

I think the critical work now is .15 - .18 & Plan .13 - .14

.28 In 236.37-237.12 we can have just one "i" value ( $\equiv 1$ , say) for all  $j$  This will work if we use long random nos. for examples. - This funct will probably not work in non-numerical domains (it probably wouldn't work in "Number Theory" either!) 236.37-237.12 is a kind of Gross Generalization of the Task. It is of some interest in that it appears able to do some (very - perhaps at a somewhat level) (.13 - .14) & (.15 - .18) are improvements (.15 - .18) is conceptually simple, but the details of implementation - could be very difficult to get it to work w. reason acceptable cc.

.36 (.13 - .14) = (236.01-06) : Using the ideas of (.28 - .30) (i=1 only), we have pairs of  $\{Q_j, O_j\}$  pairs ( $O_j = M$ funct $_j$ ), & we want to find a good linear stochastic operator  $F(Q_j) \approx M$ funct $_j$

.39  $O_j \Rightarrow \prod_j P(M$ funct $_j | Q_j)$  is max (Mult by pct of  $P_i$ ) 238.01 is max

2/0 (Non-Conventional) TM could do analysis of Wholestore Medicine) (it may be first success is almost always no good good data to conclude much - best TM could read a lot!

Bulg

.01 : 237.40 : Actually, we should save much cc by doing 237.36-.39  
 After every "j" problem is solved; since it should make soln. of G.  
 next "j+1" problem easier (See 236.16-.35 for discussion of why i how)  
 Using the  $i=1$  only idea of 237.28-.30, we can think of TM's  
 work as "linear regression" in f. way:  
 In linear prog; we use info upto  $j=n$  to produce a p.d. for  $x_{n+1}$ .  
 After ~~some~~ we are given t. true  $x_{n+1}$ , we use this to get r. p.d. for  $x_{n+2}$ , etc.  
 In TM we use In all cases, r. p.d. for  $x_j$  is based on knowledge of  
 of t. true  $x_j$  values for  $i=1|j-1$ .

.10  $\alpha$  In TM, similarly - knowing the Mfunc's for  $i=1|j$  and  
 the  $Q_i$ 's for  $i=1|j$ ; we get a d.f. for Mfunc $_{j+1}$ . We use this  
 d.f. over Mfunc $_{j+1}$  to do an search to find v. "actual" Mfunc $_{j+1}$ .  
 we then do  $j \leftarrow j+1$  loop to  $\alpha$  (.10)

.13 .10-.13 is very interesting! Somehow we are able to get this  
 d.f. for Mfunc $_{j+1}$ , but in cooperation with our previous knowledge  
 of  $\{Q_i, Mfunc_i\}$  for  $i=1|j$  !!

.17  $\alpha$  It would seem that after finding for  $M_{j+1}$ , finding  $M_{j+2}$   
 there is no need to find a way to find  $j$ 's as a function of  $Q_j$ .  
 i.e. finding an ob that identifies  $j$  from  $Q_j$ . We don't  
 need this in .10-.13!

.20 Well, what happens after we find  $M_{j+1}$ , and we are then given a  
 problem  $Q_5$  ( $j > 5$  is  $Q_5$  is one of the previous (y dear) problems).  
 Then, presumably, TM has to pair  $(Q_5, M_{j+1})$  available so it, so it  
 will give  $P(M_{j+1} | Q_5)$  a very high pc.

.25  $\Rightarrow$  My impression is that  $M_{j+1}$  doesn't need to include ~~any~~  
 info on how to work problems  $Q_i$  for  $i < j$ !  $M_{j+1}$  need solve  $Q_j$  only (N.B. 32-34)

.29  $\alpha$  Quite different procedure of TM than 236.37-237.12! It looks  
 less  $\epsilon$ l, more readable, but I'm not sure its better!  $\alpha$  One fear is that my  
 "Stochastic operator" Model of a cond. d.f., is flawed - but  
 it may assume that there is no info in the  $\{Q_i\}$  set.

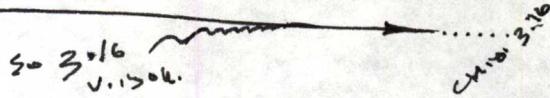
.31 Actually, in .25, the f. d. of  $M_{j+1}$  finds  $i$  as a function of  $Q_i$ ; need not  
 be very SMART (can't nor need it to be useful info) - All it has to do is find out  
 how  $Q_i$  is different from all  $Q_j$  for  $i < j$  (!) - So perhaps  
 (.10-.13) seems much better, more direct than (236.37-237.12)

[Hvr. N.B. 236.37-237.12 was merely a practical exam. of TM: A kind of  
 "Study problem". In .10-.13 getting a d.f. for  $M_{j+1}$  from within  $\{Q_i, M_{j+1}\}$   
 $i=1|j$  is not so easy! - But it may be ~~undoubtedly~~ ~~calculated~~  
 always eventually, ~~noisy~~. [.295-.31]  $\Rightarrow$   $i$  is a poss. worry.

9:17-00 Bulb

3.60 (9.4) = 3.16

239



22 Ω at 3 volts  
 $\frac{3}{22} = \frac{1}{7} = 140 \mu\text{A}$

600 mamps  
 → 4 hrs.

01: 238.40: I'm really not sure how compl. @ of 238.295-.31 is. (on into in [Q<sub>2</sub>] set)  
 Perhaps drop it for a while & see if I can continue w/o. answering it.

02: Say we have this [Q<sub>i</sub>; MF<sub>i</sub>] z: 1/n! use it to obtain ~~MF<sub>i</sub>~~ P(MF<sub>i+1</sub> | Q<sub>i+1</sub>)  
 I think I'll have to see how I would work such a problem, to get some feel for how I'd write do it.

06: A Perhaps Relevant Idea: for a given/sequential corpus, "a", we can have a "Ideal Summarizing Machine, M", so that Random inputs to M, give ~~random~~ outputs w. pc's ≡ pc's of poss. continu. of "a". M is a complete summary of all replies in "a".

09: Normally, "Summary Machines" are approximations of this ideal (Summarizing Machine; → 242.07)  
 An interesting Q is: if we ~~then~~ concat. string "a" to "a", how does the Summarizing machine M, get modified? Well, it's not very long, we simply put lots of random inputs into M, until they produce a, a continuation of a. These continuations of a will have to pc of continuations of a<sup>2</sup>.

There is a corresponding "Summary Machine" assoc. w. the "Product (unorder) set of strings" I don't immediately remember how this works! See Text 20199:  
 "T. Computer Journal": "Two kinds of Prob. induction" → 241.01-242.05

Anyway an approx (summary machine) for a b. forward chain of strings! would be a stochastic. It would have certain for  $\beta$  S G's, (stochastic) also 242.07

Each such lang is defined by a set of production rules & prob. choice probabls. T. prob. rules correspond to NT's (which correspond to sub-languages or sub-grammars)

21: When we add new data to a lang: we usually modify the Grammar by (1) changing the prob. probabls (2) Modify the Grammar by adding new NT's & assoc. prob. choice pc's.

23: (3) Markov's loss likely: Deleting certain NT's ≡ adding operators. (Harder to do). In any case, we end up w. a new Summarizing Machine (≡ P.D.)

02 is the problem of updating a "Summarizing Mach.", Hvr, it's diff. from normal updating of a stoch. Gramm, because it's a conditional P.D. Prob. files to be updated. OK, but the same difficulties (21-23) hold — we want to change pc's (if any), add new NT's or functions & perhaps revise the structure of the MF. ∴

More specifically: When a new Q<sub>i</sub> or P<sub>i</sub> is given, we ~~do~~ into decide how operator a/o try to combine the new P<sub>i</sub> into the old one in a compressive way; a/o revise the entire system in a compressive way.

A GOOD APPROACH: Watch how I work a specific problem of this sort: Express my soln. in the formal language ("conc"), then perhaps gen.

35: Hvr: My impressn is that Demonstration of the (kind of behavior I'm interested in) can only occur w. a fairly smart F.H., w. C is, a rather long TSC. T. reqs required are rather complex & irreducible (via) a small corpus. Only by A.H. insertion could the needed conc. be variable in a small corpus.

240.01

Examples  
 $Q_i^1$  is symbolic part  
 $Q_i^2$  is numeric part

.01: 239.40 | 239.35 is another example of a kind of TM behavior that cannot occur unless TM has reached a certain "sophistication."

.03 Specifically, the behavior "looked for" in 239.35: After a fair no. of  $\vec{Q}_i, A_i$  pairs in which  $Q_i$  is of form  $Q_i^1, Q_i^2$ , and TM is able to learn problems  $W$  in prob  $Q_i^1, \vec{Q}_i^2$ : how  $Q_i^1$  is an input that it has tried on:  $\vec{Q}_i^2$  is part of input that is new.  $\rightarrow$  it is able to get proper  $A_i$ .  $\rightarrow$  TM is given an  $\vec{Q}_i$  in which both  $Q_i^1$  &  $Q_i^2$  are entirely new to it, if it is able to get a "reasonable" pd. for  $A_{i+1}$ .

.08 [9.21.00] Looking at 241.01-.05: In particular, 241.20-40 and [proof of adequacy 242.01-05], it is clear that the  $[Q, A_i]$  T.S.Q. is adequate, i.e. that making stochastic functions  $P(A|Q)$  using ALP should be adequate. — That the only reason it didn't seem to work, was that  $P(A|Q)$  functional forms I was considering, were too limited — not a "universal" — or not able to express the needed regularity, (i.e. "universality is usually unreach") (238.10-13) & (240.01-20.05) seem to tell how to do T.S.Q.'s!

I had 3 kinds of induction that I wanted to demonstrate in T.S.Q.'s:  
1) Simple acquisition of concs states & rules (MFuncts) as in the search T.S.Q.'s  
2) Finding subtasks/sub ~~tasks~~ (not necessarily groups) & using them for naive induction.  
2.5) doing 2 for both OSL & MSC <sup>Multiple</sup>  
3) A more elaborate kind! say (.03-.08) ( $\approx$  239.35-40) This involves NMTM  $\neq$  truly probabilistic problem (.03-.08) seems to be a v.p. example

.22  $\rightarrow$  Look at (.03-.08) say  $\vec{Q}_i = S_i, N_i$   $N_i$  is numeric (random) part.  $S_i$  is symbolic part.  
Say  $F_i$  is a functional soln. to  $\vec{Q}_i$ ; so  $F_i(N_i) = A_i$ .  
After solving several problems, we have this set of pairs:  
■  $[S_i, F_i]$   $i=1/n$ . My earlier, simpler ideas ~~was~~ attend  $F_{i+1}$  to give a pd. for  $F_{i+1}$  based only on the known set  $[F_i]$   $i=1/n$ .  
Now I want this pd. for  $F_{i+1}$  to include all of  $i$  into in  $[S_i, F_i]$ .  
Ideally, this can be done by a (set of) function(s) that map  $S_i \rightarrow F_i$  ( $i=1/n$ ).

.29  $\rightarrow$  The map is from a kind of string, to a function.  
Superficially .29 would seem to apply only to ANL, but in reality, it could cover solns of any kinds of equations, — so, in reality, TM should be able to learn essentially diff task via this type.

.35 Book mark (where I was): Trying to do simple T.S.Q.  $\Rightarrow$  trying to devise simplest poss. Learning machine that would work in any T.S.Q.'s.  $\rightarrow$  243.09 244.37  
T. recent (241.01-242.05) still makes it clear that a pure  $[Q_i, A_i]$  T.S.Q. would be always "solvable".

The idea of (.22-.29) of my book type T.S.Q. as a special kind of  $Q, A$  T.S.Q. is var. / 11/29  
243.01

0.01 CONDITIONAL PROBABILITY:

2 forms of Data: ~~XXXXXXXXXX~~

Convergence from 242.01

On Conditional (complexity) Prob. It should be poss. to devise a form like STS for Conditional probability! This would seem to be closely related to MCT.

Anyway, say some corpus has been generated by some cond. Pd:

$P(y|x)$ . T. Corpus itself is  $[x_1, y_1]$ . If we assume that  $(x_1, y_1)$  pairs in the corpus are ordered, then this is an example of Bag production ( $\equiv$  unordered set of finite objects)

Actually, we'd need  $P(x)$  as well as  $P(y|x)$  to generate the corpus. Will the error bound in ~~XXXXXXXXXX~~  $E(PM(y,x) - P(y,x))^2$  be indep. of  $x$  d.f.?:

$P(y) = P(y|x) \cdot P(x)$  If  $P(y|x) \& P(x)$  are finitely describable then  $P(y)$  is also "finitely describable".

How, then, is also an approx. of  $P(y|x)$  that is indep. of  $P(x)$  - that does not use info. in the  $x$  d.f. It tries to find a  $P^R(y|x) \Rightarrow$

$E(P^R(y_i|x_i) - P(y_i|x_i))^2$  is min?

More exactly, it tries to find a  $P^R$  s.t. w/ short derivs  $\Rightarrow$

$\prod_i P^R(y_i|x_i) = \max$  or, more ~~exactly~~  $2^{-|R|} \cdot \prod_i P^R(y_i|x_i) = \max.$

.16 is the form that doesn't much use  $P(x)$  info. (?)

Finding a  $P(x,y)$  assoc. w. the corpus  $[x_1, y_1]$  is an (approximate)

different way (better way?) to get the approx. to  $P(y|x)$

Q: does  $P(x,y)$  imply a  $P(x|y)$ ? (Yes!)

Note that  $P(x,y)$  <sup>(S. vac. implies)</sup> both  $P(x)$  &  $P(y)$ .

.21 9.2.1.00 We are dealing w. 2 different Goals for our model! In one, we want  $P^R(y|x) \Rightarrow$   $2^{-|R|} \cdot \prod_i P^R(y_i|x_i) = \max$

in .17-18 "  $\Rightarrow 2^{-|R|} \prod_i P(x_i) P^R(y_i|x_i) = \max. \Rightarrow$

So, taking logs in both cases, the first one gives us to set  $x_i$ .

The second one gives us to set  $y_i$  or  $\prod_i P(x_i) \cdot 2^{-|R|} \prod_i P^R(y_i|x_i) = \max$

It differs only by the factor  $\prod_i P(x_i)$  from .16

So in .17-18 we have the same ends as .16, except that the model must also give a good Pd. for  $[P(x_i)]$ . When the  $[x_i]$  are from my TSO,

then  $P(x_i)$  d.f. is somewhat "A.H." & is related in a weird way to

$P(y_i|x_i)$ , so I may not want a TM to try to model  $P(x_i)$  - particularly at a cost of a less good  $P(y_i|x_i)$

So: for the present, use .16: It also has the advantage that  $P(y|x)$ , (which is what I really want) is obtained in a direct way: in .17-18,  $P(y|x)$

is obtained from ~~XXXXXXXXXX~~  $P(x,y)$ , the joint distrib., and involves division by  $P(x)$ .  $P(y|x) = P(x,y) / P(x)$ :  $P(x)$  is obtained from  $P(x,y)$  by ~~integration~~ or summation

$P(x) = \int P(x,y) dy$  (or  $\sum$  over  $\leq$  form)

There are ~~also~~ imp. side-effects in which .17-18 is better than .16 - in which

$[x_1, y_1]$  corpus is from R.W. entirely & not modulated by my "Heavy (A.H.) Hand"! (242.01)

.01: 241.10: The convergence theorem for  $P(x,y)$  (or  $P(x) \cdot P(y|x)$ ) is about the same as that for Bag of strings. Expect the "Bag of strings" convergence theorem follows the 252 corollary of .01, when  $x = \text{constant}$  or  $x = \text{A null}$ . Probably best look at present proof of Bag of strings convergence theorem (in MCT files) to devise proper proof for .01. (15)

.07: 239.09 "Summarizing Machines" that are recursively complete, need never backtrack.  
 The only reason we ever backtrack is that our 'summarizing' is imperfect.

On convergence of  $E \sum_i (\ln \frac{S_i}{S_i'})^2 \equiv E \sum_i (\ln \frac{S_i}{S_i'})^2$ :  
 Also, for S78T3 and for Bag of strings:  
 we do have constraint that  $\frac{P_i}{P_i'} > c$  and the convexity of  $\ln$ .  
 — that limits excursion of  $S_i$  from  $S_i'$ .

.15: .05\* On 241.01-.40: In the case of 241.16: what is the default, (A.H.) dcrn?  
 We need this to tell if we are making progress & how much progress.  
 Also, how does QA system work, when there is a body of data to use for reference (e.g. an Encyclopaedia)?  
 MCT would seem to hold to key)

In much of my thinking in 241.01-.40: I had been thinking in terms of "MTM", in which ~~there was~~ there was one formula that successfully did all predictions, & that best formula was far behind. For a small corpus, perhaps this is not true... But in such a case, a more "soft" probabilistic dcrn would have higher PC. — This is true in MTM w. small corpus. There are 2 aspects of "Corpus Size". One is to normalize paths: easy to get it to be effective (over by using long random nos). Second is to symbolize paths: No easy way to 152.  
 If  $Q_i \rightarrow A_i$  is 1 to 1 then there is a simple code for the corpus.  
 If  $Q_i \rightarrow A_i$  is 1 to many, there will be a code from there will be many codes - ~~some~~ of which does to corpus exactly.

The normal way to think about this is eq. 241.16. Each path there is a probability over. For each  $Q_i$ , there is a p.d. of poss.  $A_i$ 's. In a MTM corpus, of much length, these p.d.'s are very narrow. — Almost all wh on one  $A_i$ , but all other  $A_i$ 's have non-zero wt. since they have poss. codes.

.36 So, if this happens in a NMTM corpus, say  $A_0$  has many  $\geq$  "possi."  $Q_0$ 's:  $Q_{10}$  &  $Q_{20}$ . Then it may seem of = p.c. that both will have codes of about same length, for that  $Q_{10}$  input. Essentially we

.39 have a ~~set~~ set of machines w. 2 inputs. One input is  $Q_0$ , the other 243.01  
 244.01

.01: 242.40 is "random" input, or just all possl. inputs. It's this Random input

.02 whose code length we're interested in

I think [242.36 : 40; 243.00 - .08] is the right way to understand this stuff. → Actually, there are 3 inputs for machine: ① an input that defines f. machine behavior: its length is |R| of 241.16 ② The Q<sub>i</sub> input of 242.39, ③ "random" input of 244.01 : 02.

R

"Eloshely" speaking we want on R a bunch of "3" (random) codes

.08 →  $|R| + \sum_{i=1}^n |code for A_i|$  is min.

.09 ① To what extent have we solved (made progress on) 240.34 - 35? → 244.37

② Just what was the Q<sub>i</sub> + SQ I was most optimistic about? 240.03 - 08, 22 - 29

What we have is our F.S.Q [Q<sub>i</sub>, A<sub>i</sub>], we start w. a few Q<sub>i</sub>, A<sub>i</sub> pairs (i=1|n)

We find a R plan and a set of codes for the A<sub>i</sub> (= z<sub>i</sub>) w. smallest

|R| +  $\sum |z_i|$ .

Using that R, when we put in Q<sub>n+1</sub>, we get, using randomization at input, a d.f. for A<sub>n+1</sub> is we then

do trials (Larch) ~~to see what we can do with~~ until

we get A<sub>i</sub> as output. This, of course, assumes that R doesn't change. In fact, as we get more & more Q<sub>i</sub>, A<sub>i</sub> pairs, we will

want to Revise R. This has been all very theoretical thus far.

~~...~~ I want to see what these operations correspond to in a real F.S.Q.

Say we just doing MTM w. Q<sub>i</sub> = ~~...~~ S<sub>i</sub>, N<sub>i</sub> [like 240.22 - 29]

~~...~~ We end up w. a set of solns F<sub>i</sub> ⇒ F<sub>i</sub>(N<sub>i</sub>) = A<sub>i</sub>.

Consider that a [S<sub>i</sub>, F<sub>i</sub>] correspond to a x pair of original [Q<sub>i</sub>, A<sub>i</sub>] (S<sub>i</sub>).

Given pair [S<sub>i</sub>, F<sub>i</sub>] i=1|n How does one D.R. of F<sub>i</sub> from S<sub>i</sub>?

Not "Bog" in Pigeon

.25 One Gross simplification: we know primitive set functs, we then want to find

a set of functs (w. WTS), so that w. the primitives, we can use that set of functs to generate [F<sub>i</sub>] w. min p. [we haven't yet included [S<sub>i</sub>] into]

Includes OSL

.28 These new sub-functs will be sub-codes of the [F<sub>i</sub>] i=1|n. functs.

Next, we look at the inputs [S<sub>i</sub>] — try to find generator Plan from a set of primitives, i find larger abs that so that it comes out [S<sub>i</sub> small] total d.cen. } Similar to 25-28 on P<sub>i</sub>.

.32 Next, we try to find parts of the [S<sub>i</sub>] that correlate w. their corresponding F<sub>i</sub> as parts of c. correlation P<sub>i</sub>. We do all of

.33 We do all of .25 - .32 so as to minimize (0.08)

So .25 - .33 is a rather gross dem of the kind of activities one wants to minimize.

It is a very "elemental" way to do it: to break down parts into sub-parts & correlate them.

There are certainly more "global" ways to minimize .08!

.25 - .33 are some simple induction methods. To find the way to find more methods, Do run Plan & TSQ & see just what

.39 techniques I use.

.01: In 243.25-33: Make sure I understand just how each operation  $\uparrow$  PC  
( $\equiv \downarrow$  243.08).

N.B. The ANL TSG I did in most detail in Saarb was somewhat non-ideal, in that it simply tried for a start overall psm. in 243.08: Perhaps look at that psm in some detail - find out just how it did this.

.06 I think the way it would work was  $\downarrow$  we started out w.  $\{F_n\}$  start w. primitive function set.  
So, found  $F_1$  by Lsuch: ~~using~~ Adding  $F_1$  to  $\{F_n\}$  function set, we find  $F_2 \rightarrow$  it works for both  $S_1, S_2$ .  $\therefore \alpha$  Adding  $F_n$  to  $\{F_n\}$  function set we use Lsuch to find  $F_{n+1} \rightarrow \{F_{n+1}(S_i) \rightarrow A_i (i=1|n+1)\}$   
Then  $n \leftarrow n+1$  is loop so  $\alpha$

.06-10 suggest an improvement to itself,  $P_{25}$  might make it better than 243.25-39: We do .06-10 as stated, but the functions we use to generate trials are ~~more~~ <sup>much</sup> more general (than those used in .06-10)

A more Global (but still bit el.) approach to .06-10: [A hunting for

.15  $F_{n+1}$ ; We are interested in "modular"  $F_n$ , because  $F_n$  is already a short code. Similarly  $\{F_i\} (i=1|n)$  are all short codes. Also, say common sub-graphs (sub-graphs) in  $\{F_i\} (i=1|n)$  would be useful in  $\uparrow$  PC of all of  $F_i (i=1|n+1)$  [I think I may have dropped .15-.18 not so long ago!]

.18 Anyway .15-.18 is a justification for using  $\{F_i\} (i=1|n)$  as parts of Psm functions to construct trials for  $F_{n+1}$ , it tells us (I think) what PC's to assoc w. Psm: In particular, it enables us to quantify OSL - which is quite imp. in this problem (I think).

.22 It may be poss. to augment  $\{F_i\}$  to  $\{F_i\}$  of .15-.22 by Psm of 243.25-33: looking for good sub functions (overlaps)

.25 in both  $\{F_i\}$  &  $\{Q_i\}$  &  $\{F_i\}$  sets and corrects better than: Any such overlaps ~~which are~~ found would  $\uparrow$  PC of  $F_{n+1}$  in .15-.22. (The  $F_i$  &  $Q_i$  in .15-22 <sup>things</sup> ~~mean~~ somewhat different than the  $S_i$  &  $F_i$  in 243.25-32.)

.28 So: .15-.28 is essentially the method used in ANL in Saarb, w. (I hope) a better understanding of the theory (theory = 243.08 and 241/16 and 241/01-242.05 <242.01-.05 is of particular import) Also .19-.22 gives theoretical basis for PC's of component functions in ~~the~~ Lsuch trials for  $F_{n+1}$

Also, because of MCT, I have a greater variety of data types I can put in to corpus - which makes TSG writing easier ~~than~~ than at SAARB)

T. large stuff is all for QATM. It ~~may~~ may be that a general way I do to TSG into Psm .15-.28 can also be used for OZ problems.

.37 Also Note (Book <sup>Mark</sup> ~~Mark~~) sub-codes of 240.24-35: How General (is it) (very) technique of .15-.28? Would it be able to work reasonable TSG's and deal w. the Scaling Problem? T. "correlations" of .25 may help a lot.

The Analysis methods of 244.23-28 may not all apply so directly to the QA problems! While [Q:] sets & [S:] sets can be identified & "understood" (nominally coded) The Princs corresponding to the [F:] sets of 243.25-33 are not as clear!

05 Hvr: 244.15-24 should be regarded as a guide in lang TSCQ's! That I will write to 250: decide on what topics a TM needs to learn, what kinds of topics it needs to know about, & see if I can fit it into the schema of 244.15-24! This schema may need

09 "Augmentation"! → .15  
One main Q was: How far could I get w. a given schema for lang? Presumably, at some pt. of complexity, a schema would become "Universally Extensible" so w. suitable TSCQ, it would learn any needed Mod. fn. of its schema

15' 09 → **SN** Another ("Very English") approach to TM: write TSCQ: write down all the heuristics, tricks, cones, that I seem to need to "run" the TSCQ. Then try to convert (more ideas) formal ideas in MCT.

244.15-28 would be a good first approach to such a model. (E.05-09)

In .15 ff: After I write TSCQ in "solns" in English, make up a compact lang. that expresses easily, for hours, cones, func's, etc, used in solns.

**SN** A common "Meta Heuristic": when a problem is solved, or when something unexpected occurs: Try to see how this new (conc) fits into or past → to the PC. Can it be more advanced than the expected future? — so, what kinds of probs would it be useful for? This puts "hooks" & "cond. pc's" on the new conc., so we know when to try it in future.

Ok. So go back to those TSCQ's! 181.5, 182 have some stuff, but I think that were extensive (using) of Princs to put into TSCQ's.

190.24; 167.25-34; 173.10-16  
190.34

173.06-08 gives a big set of TSCQ's  
— Also poss. future Extensions

If I get stuck: review ~160 ff (or 157 ff), lots of good ideas!  
→ Q: How did I get stuck in 160 ff? — what were diff's?

Perhaps go thru history since 160: look at each of diff's text and how each was solved.

As I see it: Ti way it's done: I start w. a stochastic language that is universal & w/

① it can express anything ② It's expressions are at most, a constant "layer" (or PC & by > a constant factor) from any other stoch lang. [ cond ② implies cond ① ]

< Wops! in 37-38 stochastic lang → stochastic Operator >

Bulf.

01: ~~245.40~~ 245.40: Next: ~~summary~~ using the stochastic lang, w/ input  $Q_0$  — we pick ~~245.40~~ random codes (L such) until  $A_0$  comes out.

We then make a "summarizing machine" to do  $Q_1, A_1$  f. some way.

245.37 ff is a bit "too general". More narrowly,

— I'm thinking of a stochastic function-language. (Reg Prim-rec funct lang — not quite Turing Universal) — can't express Ackerman funct)

07 Anyway I use this lang to get  $A_0$  from input  $Q_0$ , using L such.

Next, I modify f. lang so that  $Q_0 \rightarrow A_0$  is more likely, but it keeps.

(By "Universal" (Prim. recursive universal) Then I repeat w.  $Q_1 \rightarrow A_1$ .

ABC

10 In 07, if we get all codes for  $Q_0 \rightarrow A_0$ , we have a "complete summarizing machine" & we should be able to "recreate our random input" using  $Q_1$  as input, & eventually get  $A_1$  as output.

(SN) N.B. our "Universal" machine probably has to be able to make "Definitions" (at least!).

15 In 10, After "input #2" creates  $A_0$ , Input #2 is connected to input #1 (Input #1 "dialing to current Operator").

Woops! 15 wouldn't work (I think)! After creating  $A_0$ , with the correct code on input #1, I don't think the system would be more likely to give  $A_0$  as output (w. input  $Q_0$ ).

20  $\rightarrow$  I have to work out the "Summarizing Machines" for stack operators.  $\rightarrow$  (25)

Perhaps in 15, ~~After~~ <sup>Before</sup> creating  $A_0$ , the machine put its "state" on the stack.

After creating  $A_0$ , it goes back to stack state but for new input, it remembers how  $A_0$  was created, & it's ~~more~~ more likely to try it w. whatever new ( $Q_2$ ) input is.

25: (26) Look at "2 kind of Turing Prob. (McLachlan)" for summarizing machine for Bags. I did have a summarizing Mach for Bags but it used a less convenient Model:

A better summarizing Machine for Bags:

28 We list all stochastic operators  $S_i (X \rightarrow Y)$  in a prop order ( $\rightarrow$  is order,  $P(S_i)$  is <sup>assoc.</sup> PC).

Pr. summarizing machine ~~is~~ is a pair to: Chose a  $S_i$  w/ <sup>my</sup> probab

or  $P(S_i) \cdot \prod_{j=1}^n S_j (Q_j, A_j)$  & use it as evaluator  $S_i (Q_{n+1}, A_{n+1})$  (All poss)

33 } On practical Reg message "store the  $S_i$ 's w. the host

" $P(S_i) \cdot \prod S_i (Q_j, A_j)$ " The fewer we store, the more "Backbracks" we have to do.

34 The next problem is how to do 28 ~~33~~  $\rightarrow$  34 in a practical way

— Heuristic Methods to ↓ cc.

eq. 33 induces a pd  $P'(i)$  on all stochastic operators,  $S_i (Q_i, A_i)$

When a new  $Q_{n+1}$  (or  $Q_{n+1}, A_{n+1}$ ) comes in, we'd like to try them

$\frac{P'(i)}{cc(i)}$  orders, but it's not so easy to do, if we just have, say 1000

01246.40  $S_i$ 's w. by  $P'(i)$  If we had all  $S_i$ 's in  $P'(i)$  order then this would be true & we'd get a v.g. pd for  $Q_{n-1} \rightarrow A_{n-1}$ . ~~What I want~~ What I want is a way to approximate  $P'(i)$  in a way that gives a useful, smoothable distribution of  $i$ , for Lschr.

05 One way might be to look at  $\vec{S}_n$ , which is the 10 best  $S_i$ 's that I've found, for  $[Q_i, A_i] \ i=1/n$ . (So: 10/n  $S_i$ 's.) a "pass a grammar thru them."

08 Or possibly "pass Grammar thru" the 1000 best  $S_i$ 's for the current value of  $n$ .

**[SN]** in Sol 89 (Israel): §5 "How updating is done": We use Lschr to solve several problems. We have a set of solns to pass a grammar thru them.

It is then then guess is a pd. to use Lschr to solve the next problem. When described this way, the Lschr is not "conditional", so its P.D. is indep of the nature of the problem. In .05-.08 we do a similar "pass a grammar thru", but we have a conditional probability dist.,  $S_i(Q, A)$ . [Note:  $S_i(Q, A)$  is usually not a joint pd. over  $Q$  &  $A$ ; it's a pd. on  $A$ , as a function of  $Q$ .]

So the P.D. on  $S_i$  is supposed to be "Problem-Independent."

09 One Q is: Just how do I express a cond. pd.? Can I express it like those "function/concept" nets? Well, a pd. is a type of function, but it's a very special kind of function - so we'd want to restrict the representation method so it would generate (almost) only pd.-type functions (compd on  $[0,1]$ )

One sure method is to simply use an approx of ALP: to get  $P(Q, A)$ , we have many functions that map from  $Q$  to  $A$ , if we put in  $Q$  & then the prob of  $A$  is  $\propto$  to no. of funcs that have  $A$  as output. We may want to ~~weight~~ these  $\uparrow$  funcs, for greater variability.

It would be neat, hvr, if we could just put in  $Q$  &  $A$  & get a pd. or, put in  $Q$  & get a list of  $n$  most likely  $A$ 's w. their associated pc's.

We can get a P.D. on ordinary funcs, by considering the net that represents their generation. (Each ~~single~~ choice in the net (each edge) will have a certain pc.)

Perhaps a better way: Consider the set of (non-probabilistic) functions  $[F_i]$

033 that generate  $Q_j \rightarrow A_j \ (j=1/n)$ . Say  $P_i$  is the ~~strip~~ strip of  $F_i$ , the ~~is~~ ~~subset~~ subset. Then we pass a grammar thru the  $P_i$ -wtd. set of functions  $F_i$ . The funcs are represented by nets and we can look for common sub-nets in the set of funcs. There is a finite set of such funcs, so we may be able to generate the  $P_i \leftarrow \frac{P_i}{\sum P_i}$ .

Hvr, ~~it's not clear~~ the meaning of "passing a grammar thru" set of funcs is not clear, because ~~SSZ~~ ~~is~~ ~~a~~ ~~not~~ ~~clear~~, and ~~SSZ~~ ~~has~~ ~~to~~ ~~be~~ ~~clear~~ ~~later~~ : 248.01

.01: 247. To We can have a "corpus" whose codewords want to minimize. This enables us to tell if a code element (a "regularity") is legit. in derbng. to corpus"

.03 In the present case, we know to group <sup>stoch</sup> grammar & for xi set  $F_i$ . It is xi. 2 prind of  $[F_i]$  with zero wt. for all func that which ~~cannot~~ <sup>cannot</sup> 200% compatible w  $\sum Q_j, A_j, j=1/n$ . We want to approximate a vector of D.F. from  $P_i$ 's

.05 ~~we~~ with sample,  $\sum F_i$ . IS  $P_i$ 's a "surface reconstruction" problem?

Probably not: I think I've been here **[.03-.06]** before: I may have ~~not~~ solved it. It may have been in **SGA** in which I wanted to approximate

$G(x)$ , given  $[G(x_i)] i=1/m$  — an interp'n. function. [re. stat of pairs  $[x_i, G(x_i)]$ ]

I normalized  $G$ , so that  $G(x_i) \leftarrow \frac{G(x_i)}{\sum_j G(x_j)}$

Then I wanted to pass a grammar over the pairs  $G(x_i)$ 's — which were like a P.D.

Lots of trouble!

There is an ~~assn.~~ <sup>A.H.</sup> that assigns  $P_i$  to  $F_i$  for  $i=1/n$  & zero to all other func's.

.14 Perhaps try to a short der'n of the set of pairs  $(P_i, F_i) i=1/n$ .

or  $(F_i, P_i)$  in the sense that we want an operator in which we input

$F_i$  & get  $P_i$  (or close to  $P_i$ ) for  $i=1/n$ . We want the operator to have

.17 a univ. d con.



.18 ~~Die I ever find a way to deal w. ~~the~~ to pc of "correcting"~~

$P_i$  when  $F_i \rightarrow P_i$  wasn't exactly right? Well, one way is to have

$F_i \rightarrow P_i$  be a pd rather than a deterministic function. We could

have a deterministic funct, then a Gauss D.F. w. common  $\sigma^2$  for

$i=1/n$ . This seems Not BAD!

So (.14-.17) & (.18-.22) may solve the problem!

It looks like a non-linear regression problem ("How many <sup>params</sup> conts to use?")

Well, this "n.l. regression problem" may not be so easy! In fact I did try to

model  $G_i$  as a function of  $\vec{x}_i$  in my recent work on (GA/GP). — But I didn't

think of it as a n.l. regression problem!

~~It~~ Still, it looks like a rather hard problem! n.l. regression or not!

One trouble: I do know the grammar that obtained the  $P_i$  from  $F_i$ . (in 247.53)

$P_i$  is the comp of  $F_i$  & it is usually easy to find — in that  $F_i$ 's are generated by some (known)

stochastic grammar &  $P_i$  is the pc assigned to  $F_i$  by that (known) grammar.

.33 So the question is: is there a cheaper way to der'b. the set  $[F_i, P_i]$ ?

Well, we may add more info — say on **negative cases** — in which case ~~that~~ **GOOD!**

OK. old grammar that generated  $[F_i]$  would give ~~the~~ wrong pc's to the ~~func's~~ **GOOD!**

but should be given near zero pc. I will probably have a lot of  $F_i$ 's

that I know (empirically) do not fit.

Hrr, see 252.29 for discussion!

The poor Derby for positive cases only is easy; its pc = 1; its just the

a generic grammar (pc=1) generating the  $P_i$ 's from the  $F_i$ 's — total pc = 1.

22 x 16 3/4 → 27.65" dia ←

→ 22 x 16 1/2 → 27 1/2" pretty narrow ← 3,4,5

If we list the  $[F_i]$  that satisfy constraints,  $F_n$  will be a complete desc. of a set of  $F_i$ 's that excludes all other  $R_i$ . It's for PC

.03

is  $\prod_{i=1}^n P_i$  This is a A.H. desc. of a ~~set~~ set of possible  $i$  all known negative cases.

So .03 is PC of  $P_i$  default (analogous to "random") case. Any shorter desc. is of (some) interest. — desc. of smaller PC are usually not of interest unless we have a way to add up a lot of them. **ABCDE**

But perhaps all we really want is a way to get functions that are "close" to  $F_n$ . — or to  $\sum [F_i] i=1/n$ . Actually  $F_n$  is the only function that satisfies all of the constraints — only it <sup>must</sup> of  $\sum [F_i] i=1/n$ . We use i. rest of  $F_i$  to "expand to sample" in a "soft", approximate way.

Not!

On second thought,  $P_n$  is a PC of  $F_n$ , &  $F_n$  is not to do a complete desc. of  $\sum [Q_i, A_i] i=1/n$  : ~~pos. no. of~~ positive cases!

I want to desc.  $[F_i, P_i] i=1/n$  plus  $[F_j, \phi]$  for  $F_j$  that I've tested that ~~didn't~~ did not work.

I guess  $F_i$  ( $i < n$ ) are all imp. also, because they are all attempts to find  $F_n$  (i.e.  $F$  that works w. all  $Q_i$  in an optimum way.) ... But I've forgotten about the probabilistic nature of  $F$  mapping  $Q \rightarrow A$ .

But still  $F_n$  is "Uniformly Better" than  $F_{n-1}$ . Should I try to find a program that just gives  $F_n$  by PC, & very low PC for all other  $F_i$  that I have tested that fail for one (or more)  $Q, A$ ? I could <sup>often</sup> just have one pos. instance of  $F_n$  (possibly <sup>small size</sup> ~~mean of~~ "oversearch")

Re: use of data of  $F_i$ ; ( $i < n$ )! These can be considered to be "approx. of  $F_n$ ": Each has a PC of "correction" to bring it to  $F_n$  accuracy. Usually, I imagine, this PC of correction is quite small so these

~~can~~  $F_i$  write not be worth considering (?). — Maybe not so small! In the first place,  $F_i$  have approx  $\gg$  that of  $F_n$ . "Correcting"  $F_{n-1}$  could involve just recognizing  $Q_n$  & then ~~providing~~ giving  $A_n$  or a suitable function  $Q_n \rightarrow A_n$  (perhaps) — Total PC could be not much worse than that of  $F_n$ .

.30

See 249.33-40; 252.01-28 for ending and a kind of resolution of this problem

~~Another kind of problem~~

CRITICAL

.33 247.19-249.30 is an attempt to solve a very simple problem: How to develop a good stochastic function / operator that maps  $Q_i \rightarrow A_i$  ~~set~~  $[Q_i, A_i] i=1/n$ .

.35 There is a standard ALP soln. to this problem: Say  $[F_j]$  is a set of funcs. of type  $[P_i] \Rightarrow$

.36  ~~$\forall i, j \forall i, j F_j(Q_i) = A_i$~~   $\forall i, j F_j(Q_i) = A_i$ . Then  $\sum_j P_j F_j(Q_{n+1})$  is a wtd. d.f. over poss. "values" of  $A_{n+1}$ . — i.e. a d.f. for  $A_{n+1}$ .

.37 So just what is 247.33 ff. trying to do?? Well consider .33-.37: It was only how a few  $F_j$ 's map to  $[Q_i, A_i] i=1/n$ , then we will only have (at most) a few  $[252.01$

# Meta Problem of TM (34)

- .01: 249.40: I want to do a good review of ~160-249: T. present idea ~~is~~ is to
- .02 write a TSQ. i. write out detailed hours for humans: Then develop method
- .03 of hrs. along with this 160-249 discusses various problems: solved forms:  
I should be familiar w. Rose (probs/solns) while I'm doing .02-.03.  
It should be poss. to do .02 w.o. (.03). I would list all needed hours, then look into Q of how each hour could have been dev'd. — which hours (if any!) were needed for each ~~hr~~ hour dictionary, ect... down to
- .08 write a Basic set of hours on a primitive set of functs/functionals.

Some imp. probs/ideas in TSQ design:

- 1) The idea of local v.s. Global (symbols/nos/vars): So if I ask TM:   
If  $x+3=7$  what's  $x$ ? It must realize that  $x$  is  $x+3$  etc are to be used in this problem only, but that "Most" other cases (unless explicitly told to be "local") are Global & apply to All problems
- 2) Is  $[Q, A]$  format an adequate/good format for an initial tsp? — for all TSQ's? (conceivable all problems could be "usefully" put into this form. — e.g. If it's a TS, bag hrs, inv, OZ, problem, we could have Q w. an additional component that tells which of  $f$  & it is so,  $\textcircled{1}$  (TS, begin of TS):  $A$  would be next element in Time Series  
 $\textcircled{2}$  (Bag hrs):  $A$  into bag: Part of  $A$ :  $A$  is  $A$  ~~needed~~  $A$   $A$  or rest of  $A$  1.  
 $\textcircled{3}$  (INV, Functn,  $F, FX=y; y$  is given):  $A$  is to find  $X$ . 12  
 $\textcircled{4}$  (OZ,  $G(\cdot)$ ;  $CC: A$  to find  $X \Rightarrow G(X)$  is Max in  $CC$ ):  $A$

→ Note, hrs, Most INV probs are solved by converting them to OZ probs

→ TM could learn a lot by watching an O.T. at work: The O.T. would find a sequence of  $X$ 's in attempts to Max  $M(X)$ : TM would try to find a p.d. that characterizes  $X$ 's  $G$  distribution. TM would not have to know  $M(X)$  in order to do this, but TM could regard this as a kind of Cond'l p.d. w.  $M(X)$  being part of "Condition" ( $\approx$  Question). 5

By watching many O.T. for many kinds of OZ problems, TM might get a good idea as to how to estimate  $G(X)$  very fast & thereby do OZ probs very well. 130

Note that part of the OZ problem is  $f. CC$  of  $z$  ( $z$  is  $z$ ): This would have to be appreciated by TM! 1  
40  
20 out

34 Work on "Meta Problem" of How I should work on Designing TM! Taking into account my ↓ power of memory. Sounds like "unsolvable" OZ problems where  $G(X)$ .  $F$  (Time of soln) is to be maximized.  $R(t)$  is my failing Memory!

- 38 1) Some variables: What was bottleneck after Sol 89? — Why did I not finish TM @ Sarb? Reasons: (1) T. TSQ's were very hard to write (2) These solns  $\rightarrow$  (251.20)
- 3) I have made several imp. discoveries since Sarb: (251.01)

(b)

"WON"

Very imp. problem  
("Bottleneck")  
How much progress on problem of interaction of tasks? in AND or OR mode?

01: 250.40: 3) (cont.) They are: (a) Sort of gain of (what to work on next) for complete AND/OR net.  
.02 (b) MGT proofs, understanding (c) Understanding of TM's Gov.

→ The main Subject is Understanding English text.

→ A BIG Q is: How much ~~int~~ do I have to introduce ( $\approx$  A.H.) into TM (by TSO's usage) before it can learn much from less carefully designed text? How will this threshold depend on IPC of Machine Used? How well can we do w.  $10^{10}$  ops/sec?

$10^{11}, 10^{12} \dots 10^{15}$  ops/sec? Or, more exactly, how well can we do w.  $10^n$  ops?  $\equiv$  CJS

For a given T.S.Q. I will have to put in fewer steps (less "sinning") if I allow large CJS. ~~say~~  $> 10^{10}$  or  $10^n$  steps

If I have smaller CJS, I'll need more examples. So the Q is: What is (no. examples)<sup>N</sup> x (no. CJS of examples)<sup>C</sup> = total ops needed for T.S.Q.:

$N \times C$ : Can we minimize  $N \times C$  (for a T.S.Q. that goes to "understanding text")

by varying C (then N is a function of C:  $N(C)$ ) — so min  $C \cdot N(C)$  by varying C.

$C \cdot N(C)$  could be small for small C, but we would then have a TM that had no experience (i.e. hours) for problems w. large CJS.

Large CJS's use common hours but are not practical for small CJS: — exp. large initial overhead.

So, in general, we may want to use as large a CJS as we can afford; its  $N(C) \cdot C$ . (Restrict total cc of ~~the~~ T.S.Q.)

$\approx$  Total cc of Corpus

.20: 250.36: (a) Only used (ones that were) solutions of previous problems. (b) There was no use of sub notes (sub functions) of previous solns. : I recently (since ~160) wrote about this — why it occurred. I think it is intimately involved w.

how 'big', how complex the T.S.Q. is, & the exact nature of the induction system used: What is form of ~~inducting~~ (say is, acc. Ind. T.S.Q.'s ideas of ...)

? what did I have in mind?

(c) T. soln. method didn't "scale" well —  $\Rightarrow$  T.S.Q. continued, too many functions in "Storage": (see 253.12 on no "scaling"; see 253.02 for dem of SAARB scaling)

[SN] In "insisting hours" we do this so that TM could have had to learn by observing and ~~also~~  $\sim$  cases in the past. What SSZ should be used? It may depend on just what the hours is: but try OSL: just one rescript. post.

Bulg

Olympic fund  
US

**STRI**  
or SZRI  
0.35  
0.39

String to Real  
Arithm. Induction

.01: 249.40: poss. values of  $A_{n+1}$ : If we are looking for a particular known  $A_{n+1}$ , then we may well be unable to find it in this small set of poss.  $A_{n+1}$ 's.

— so we would really completely "lose" on this search.

247.33 ff tries to deal w. this by extrapolating to set of functions,  $[F_j]$  of 249.35-36, by "Passing a stack grammar" thru  $[F_j]$ . The spirit of this is that of  $\geq 141$  — (Passing a stack grammar thru a set of strings).

A major diffy is that of  $SSZ$ . We only have a few "strings" (w. wts,  $p_j$ ) to pass our grammar thru, & I don't have a clear idea as to how to do this. . . .

It may, indeed, be a not viable way to solve this problem.

.10 I had the idea of extrapolating to set of pairs,  $[F_j, P_j]$ , w. ( $P_j = \phi$  for  $F_j$  trials that did not pass thru  $[Q_i, A_i]$  in  $(n)$ ). 247.33 — 249.30 tries to deal w. this problem.

Note that because of a large no. of negative cases, the  $SSZ$  for this problem of 10-11 is quite large.

A somewhat different approach to 247.19 "How to express a cond. p.d.": Stochastic Grammars (like in  $\geq 141$ ) over p.d.'s: Ray over on conditional p.d.'s: If the Grammar were a function of  $Q_i$ , and  $A_i$  were giving a P.D. by that Grammar, we'd have what we wanted! However, it's not clear as to how to do this — the deterministic (or even probabilistic) mapping from  $Q_i$  to Grammar's.

In General, it may well be that I will get a better "feel" for what kinds of cond. P.D.'s I want, when I try to express my "English" total (including hours) solutions to T3Q's in the form of cond. P.D.'s.

At the present time, my ideas on this would have to be too general.

.26 So this is a good method to go to the point  $250.01 - .08 \approx 163.16$   
in which I write a T3Q in English & write down the hours in English, then try to devise a language & induction rules to acquire the T3Q  
v.i.e. solve hours in (26) "early work"

.28 10B. The idea of 249.33 of including neg. cases, may not help much! A v.g. fit could be obtained by deriving the  $[F_j, C_j]$  set exactly & giving  $C_j = \phi$  to all other cases: (particularly if there are only a few  $C_j > \phi$ ). However, still it is poss. that we may get a grammar that gives approximate values of  $[C_j]$  that has a whole proper PC.

.35 Any way: Consider the problem of "convergence"  $[F_j, G_j]$  to be "naturally solved" 2 simple cases  $F_j$  is solved fact,  $G_j$  are known zones for neg. cases.

(2)  $F_j$  are functions or strings derivable objects in  $[G-P]$  &  $G_j$  are their known forces. Much work on this

.38 DEP Call it a String to Real Induction "STRI" STRI.

N.B. Stochastic loops is one kind of STRI problem that is some "partial" solved. functional form

9:30:00 Bulg.

Partnershi low: "Work expands to fill time"  
To get work done fast, allocate less time to it!  
E.g. TM, → 555.01

01:252.90 That a STRI problem soln. can have. Hvr T. hours of Grammar discovery have not proved to be very useful in solving STRI!

02 (SN) I wanted to use a STRI soln. for SGA! My "soln" of Koza's "3+2" input Maxer problem was simply broken over a simple function space; Man add to f/ functions, any new func found that <sup>set of</sup> ~~was~~ were much closer to f. Goal. — This seems close to what I did in SAARB TSC's. This suggests a "Back Door" soln. to STRI problem!

— So if I have  $F_1 \ni F_2 \ni F_3$  w. by  $C_i$  values, I just add them to the "function pool" w. wts, perhaps a ~~few~~  $C_i$  values. The functional combinations can be as ~~many~~ <sup>as</sup>  $2^N$  or  $3^N$ , because of rapid comb <sup>ational</sup> explosion (w/o. heuristics). We also have rapid  $\Delta$  since as no. of functions to be used  $\uparrow$  in combinations  $\uparrow$

02: One trouble w. this  $\Delta$ : By itself, it does not scale to larger parts —  $\Delta$ . no. of funcs available grows (exponential) w. no. of parts solved — so it eventually becomes impractical — unless one devises heuristics to narrow down "which funcs to try".

One aspect of this "Scaling" problem

06 Some Common Mappings from strings to reals: ① strings represent equations or systems that have evaluable parameters. Example of ① would be a string representing an electrical ckt:  $\dots$  is an  $\omega$ ; the real (or complex no.) is the impedance at that frequency, or  $\dots$  the string describes a neural net's  $i$ th input; the real (or complex) output is the  $i$ th output. The representation of SPICE ckt's by Koza is a good case in point. — The "output" is the ~~fitness~~ "fitness function" of that ckt.

A common way to discover the string  $\rightarrow$  real relation is to experiment w. the numerical params in the "string".

A string can represent a physical system (say a QM) — the "real" can be some computed property of the system (Energy, velocity, ...)  
② then, the "real" will setup. ops & the "numbers" will furnish "parameters";  
③ occasionally numbers (integers, etc) can help setup ops, but this is usually a bit of a specification of a continuous param or the nos. are ~~randomly~~ <sup>randomly</sup> descriptors that are assigned "symbolic" meanings in a rather A.H. way.

— So they have to be found via ~~large~~ <sup>large</sup> ~~SSZs~~ <sup>SSZs</sup>.  
This is true in Koza's systems: "Reals" & "symbols" are ~~found~~ <sup>found</sup> in different ways, in GP.

In assigning PC to strings (stock lang.) the strings usually have no nos in them. This is ALP's way of bringing "Quantity" from "Quality". It is a very special kind of functional relation. What it does is related to "counting" — no. of times a certain feature occurs. We can get a pc - like number by suitable norm'n. — or by multiplying  $\Delta$  such norm'd nos together.

Considered this way, it seems clear, that usually, STRI

depends very much on Info Ques TM has about what "symbolic part means",  
I had decided that I couldn't really work on this STR problem until  
I had a less "abstract" idea of what to expect in the <sup>relationships</sup> functional  
relationships.

Well; now I have a somewhat better idea of what to expect!

AA is one simple example of STR. (253.16)

Another type would be recognizing certain "substrings" or "structures",  
Country Ques is having the functs. of f. ~~various~~ various "roots". ~~that~~  
is done in "Standardized Individual" Passy a Grammar Para a set of strings  
is one way to get a number ( $\equiv pc$ ) for each string.

Also: "Spec" is an extreme case! Looks at Symbolic (etc. dera) &  
has (exam values) & calculates its path in ~~time~~ time! ~~is~~

( $\equiv$  seq. of numbers) or ~~is~~ any other param of resulting system.

Or to invert "Spec" Given param to design (Symbolic) char  
param (nos) (this is what Kozzi's filter design program did).

The dom of functions in terms of primitives involve mainly Symbolic  
(<sup>not</sup> Graph) ~~nodes~~ + primitive + 1, 2,  $\pi$ ,  $e$ ,  $\gamma$  ~~etc.~~ & some small  
integers as "params". e.g.  $\sin x = \frac{e^{ix} - e^{-ix}}{2i}$  (divided by 2 because ~~because~~  
2 functs in numerator ... (from "Country" operation).)

.01 Admin: Parkinson's law: "Work Expands to fill Time":  
Early in TM rsch, I felt that TM could easily take rest of my life: It looks like I've been arranging it to do so!

A (Poss) way out: Make outline of what needs to be done on TM:  
(A sort of ~~PERT~~ PERT (?) diagram), w. indications of interaction,  
AND/OR not of tasks:

Describe each task clearly & tell how much of it I've done, & how much more time I ~~need~~ <sup>expect</sup> I need to "finish" it. (different 's' of "finish" may be poss!.)

For most tasks, have given names "Names" along w. clear definitions of them.

→ Also Arrange Journals so I know <sup>where</sup> stuff is; Also so I can refer to  
= page <sup>or</sup> set of pp.

Stuff since Searb; since S89; since S86. are of most import.  
Work on S89 was probly very imp: (Also mention S86).

• Main Subgoal is "Good enuf" Understanding of English, to begin to read  
& understand English text, so that % of understanding ↑ w. time.

.17 • Subgoal before that: Understanding of Algebra or some part of Math.  
Enuf to work probs of some diffy.

• Sort of Sub-goal: To be able to do NMTM induction problems —  
"Soft" induction in f. areas of Math's eventually in other domains.

.21 • Devise TSQ for Algebra of .17

.22 • Devise Lang. strategy for .17. & for general  $[Q_i, A_i]$  problem → <sup>is general of</sup> (25) t. STRE problem  
• PSG discovery: Probably very useful for various kinds of grammar models...  
(Grammatical induction.)

.25 • STRE problem: Given  $[X_i, Y_i]$  to induce  $P(r | \vec{x})$  to recode.  
<sup>strategy, Recd, induction</sup>  
This is important in learning of 's & understanding, 's, 's, GA. do to induce  $P(r, \vec{x})$ .  
This is a special case of 22R  $[Q_i, A_i]$  induction

tailored

Superficially, it would seem that  $Q_i A_i$  lang would be a rather general coin.

to .22 & .25 — both imply problem aids.

.31 I think I felt that I was doing so well in finding > both .22 "in abstract"

.32 that a better way to deal w. it was to write a TSQ for Alg 21 along w. "solving"  
in English, w. all hours I could think of. — Now express this "solv" as a log. strategy (no. 22)

While the log. lang method would be somewhat tailored to that TSQ, I hoped I  
could generalize & transfer in a useful way.

Then I would continue TSQ & solve probs "completely" in English  
if exp. info / transfer probs for lang. was adequate — or whether new tailored  
lang. techniques had to be added.

m/m/m // = LITD ABCD

.01: 255.40! So there are 2 issues:

- 1) Work on 255.22 ~ [Q<sub>i</sub>, A<sub>i</sub>] (ing problem directly, abstractly, in rather general case. [Q, A can be all or partly symbolic; numeric
- 2) Do 255.31-.40 — which seems very promising.

In 255.22 I had to update problem: i.e. say I had a good induction model or d.t.

.07 for [Q<sub>i</sub>, A<sub>i</sub>] s.o./u; How do I update my model when ~~it~~

.08 Q<sub>n+1</sub>, A<sub>n+1</sub> comes in? I did do work on this if it soln. was a "Complete Summary machine" <sup>then</sup> ~~then~~ was no diff: If fi summary was incomplete, then Backtracking is warranted/necessary.

.11 Another tack would be: If P(Q, A) works on Q<sub>n</sub>, A<sub>n</sub>,

.12 what is a prop for fi functional form, P — some can (such as fi for a fit) → see 267.29-

Can ~~(.07-.10)~~ & (.11-.12) be unified? — It would seem that they should be!

.35 for poss. relevant remarks! maybe soln!

Re: .07-.10 & Summary Machines: T. stuff about "Backtracking" is correct if "summarized" by only including fi. Short/codes of fi corpus. — in P<sub>fi</sub> case, "Backtracking" retrieves some lower codes for fi corpus, P<sub>fi</sub> are now relevant. BUT there are ways to "summarize" ≠ .15:

— Just what are they? Consider an approximate code plus a correction code.

Is P<sub>fi</sub> a case? Also what is done in "Theory Revision" in physics?

.20 In physics — (say introduction of Relativistic phenomena) we first decide that we are working in a new area (by velocities/accelerations), so we label it as such, so we can distinguish it from the old area ("old corpus"). We then make models for the "new area" specifically. When we get these models, we then try to put a "grand theory" that unifies the old & new models for the old & new corpus —

.25 A "Grand Reformulation" that ~~unifies the old & new models~~ overall code length (this is ≈ 257.34-.40)

.26 This would amount to finding a good model for (Q<sub>n+1</sub>, A<sub>n+1</sub>) (or a sequence

.27 of [Q<sub>i</sub>, A<sub>i</sub>] = (n+1)/n) and a way to identify [Q<sub>i</sub>] = n+1/n.

.28 — Then attempts to unify the new model into the old.

.26-.28 is easily applied to learning "3+7" then "5\*9".

.30 There is the problem of deciding TMs deciding how big M should be on .26-.27. This means — deciding how much of the corpus should be covered by the new model. Well, we just let the model be small M, then we see how large an M we can take & still have the new model fit!

T. long assumes the corpus is very nice & built into being new concepts sequentially: say the new corpus was 3+7; 5\*8; 4+2, 4+7, 3\*7 ...

Here, "3" & "7" are just 3 & 7, they are not (any) random nos. —

.33 this means we cannot simply code 3+7, then 5\*8, because the model is too big to handle a fixed any code compression viz 1/ or 2/ or 3/ or 4/ or 5/ or 6/ or 7/ or 8/ or 9/ or 10/ or 11/ or 12/ or 13/ or 14/ or 15/ or 16/ or 17/ or 18/ or 19/ or 20/ or 21/ or 22/ or 23/ or 24/ or 25/ or 26/ or 27/ or 28/ or 29/ or 30/ or 31/ or 32/ or 33/ or 34/ or 35/ or 36/ or 37/ or 38/ or 39/ or 40/ or 41/ or 42/ or 43/ or 44/ or 45/ or 46/ or 47/ or 48/ or 49/ or 50/ or 51/ or 52/ or 53/ or 54/ or 55/ or 56/ or 57/ or 58/ or 59/ or 60/ or 61/ or 62/ or 63/ or 64/ or 65/ or 66/ or 67/ or 68/ or 69/ or 70/ or 71/ or 72/ or 73/ or 74/ or 75/ or 76/ or 77/ or 78/ or 79/ or 80/ or 81/ or 82/ or 83/ or 84/ or 85/ or 86/ or 87/ or 88/ or 89/ or 90/ or 91/ or 92/ or 93/ or 94/ or 95/ or 96/ or 97/ or 98/ or 99/ or 100/ or 101/ or 102/ or 103/ or 104/ or 105/ or 106/ or 107/ or 108/ or 109/ or 110/ or 111/ or 112/ or 113/ or 114/ or 115/ or 116/ or 117/ or 118/ or 119/ or 120/ or 121/ or 122/ or 123/ or 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374/ or 375/ or 376/ or 377/ or 378/ or 379/ or 380/ or 381/ or 382/ or 383/ or 384/ or 385/ or 386/ or 387/ or 388/ or 389/ or 390/ or 391/ or 392/ or 393/ or 394/ or 395/ or 396/ or 397/ or 398/ or 399/ or 400/ or 401/ or 402/ or 403/ or 404/ or 405/ or 406/ or 407/ or 408/ or 409/ or 410/ or 411/ or 412/ or 413/ or 414/ or 415/ or 416/ or 417/ or 418/ or 419/ or 420/ or 421/ or 422/ or 423/ or 424/ or 425/ or 426/ or 427/ or 428/ or 429/ or 430/ or 431/ or 432/ or 433/ or 434/ or 435/ or 436/ or 437/ or 438/ or 439/ or 440/ or 441/ or 442/ or 443/ or 444/ or 445/ or 446/ or 447/ or 448/ or 449/ or 450/ or 451/ or 452/ or 453/ or 454/ or 455/ or 456/ or 457/ or 458/ or 459/ or 460/ or 461/ or 462/ or 463/ or 464/ or 465/ or 466/ or 467/ or 468/ or 469/ or 470/ or 471/ or 472/ or 473/ or 474/ or 475/ or 476/ or 477/ or 478/ or 479/ or 480/ or 481/ or 482/ or 483/ or 484/ or 485/ or 486/ or 487/ or 488/ or 489/ or 490/ or 491/ or 492/ or 493/ or 494/ or 495/ or 496/ or 497/ or 498/ or 499/ or 500/ or 501/ or 502/ or 503/ or 504/ or 505/ or 506/ or 507/ or 508/ or 509/ or 510/ or 511/ or 512/ or 513/ or 514/ or 515/ or 516/ or 517/ or 518/ or 519/ or 520/ or 521/ or 522/ or 523/ or 524/ or 525/ or 526/ or 527/ or 528/ or 529/ or 530/ or 531/ or 532/ or 533/ or 534/ or 535/ or 536/ or 537/ or 538/ or 539/ or 540/ or 541/ or 542/ or 543/ or 544/ or 545/ or 546/ or 547/ or 548/ or 549/ or 550/ or 551/ or 552/ or 553/ or 554/ or 555/ or 556/ or 557/ or 558/ or 559/ or 560/ or 561/ or 562/ or 563/ or 564/ or 565/ or 566/ or 567/ or 568/ or 569/ or 570/ or 571/ or 572/ or 573/ or 574/ or 575/ or 576/ or 577/ or 578/ or 579/ or 580/ or 581/ or 582/ or 583/ or 584/ or 585/ or 586/ or 587/ or 588/ or 589/ or 590/ or 591/ or 592/ or 593/ or 594/ or 595/ or 596/ or 597/ or 598/ or 599/ or 600/ or 601/ or 602/ or 603/ or 604/ or 605/ or 606/ or 607/ or 608/ or 609/ or 610/ or 611/ or 612/ or 613/ or 614/ or 615/ or 616/ or 617/ or 618/ or 619/ or 620/ or 621/ or 622/ or 623/ or 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749/ or 750/ or 751/ or 752/ or 753/ or 754/ or 755/ or 756/ or 757/ or 758/ or 759/ or 760/ or 761/ or 762/ or 763/ or 764/ or 765/ or 766/ or 767/ or 768/ or 769/ or 770/ or 771/ or 772/ or 773/ or 774/ or 775/ or 776/ or 777/ or 778/ or 779/ or 780/ or 781/ or 782/ or 783/ or 784/ or 785/ or 786/ or 787/ or 788/ or 789/ or 790/ or 791/ or 792/ or 793/ or 794/ or 795/ or 796/ or 797/ or 798/ or 799/ or 800/ or 801/ or 802/ or 803/ or 804/ or 805/ or 806/ or 807/ or 808/ or 809/ or 810/ or 811/ or 812/ or 813/ or 814/ or 815/ or 816/ or 817/ or 818/ or 819/ or 820/ or 821/ or 822/ or 823/ or 824/ or 825/ or 826/ or 827/ or 828/ or 829/ or 830/ or 831/ or 832/ or 833/ or 834/ or 835/ or 836/ or 837/ or 838/ or 839/ or 840/ or 841/ or 842/ or 843/ or 844/ or 845/ or 846/ or 847/ or 848/ or 849/ or 850/ or 851/ or 852/ or 853/ or 854/ or 855/ or 856/ or 857/ or 858/ or 859/ or 860/ or 861/ or 862/ or 863/ or 864/ or 865/ or 866/ or 867/ or 868/ or 869/ or 870/ or 871/ or 872/ or 873/ or 874/ or 875/ or 876/ or 877/ or 878/ or 879/ or 880/ or 881/ or 882/ or 883/ or 884/ or 885/ or 886/ or 887/ or 888/ or 889/ or 890/ or 891/ or 892/ or 893/ or 894/ or 895/ or 896/ or 897/ or 898/ or 899/ or 900/ or 901/ or 902/ or 903/ or 904/ or 905/ or 906/ or 907/ or 908/ or 909/ or 910/ or 911/ or 912/ or 913/ or 914/ or 915/ or 916/ or 917/ or 918/ or 919/ or 920/ or 921/ or 922/ or 923/ or 924/ or 925/ or 926/ or 927/ or 928/ or 929/ or 930/ or 931/ or 932/ or 933/ or 934/ or 935/ or 936/ or 937/ or 938/ or 939/ or 940/ or 941/ or 942/ or 943/ or 944/ or 945/ or 946/ or 947/ or 948/ or 949/ or 950/ or 951/ or 952/ or 953/ or 954/ or 955/ or 956/ or 957/ or 958/ or 959/ or 960/ or 961/ or 962/ or 963/ or 964/ or 965/ or 966/ or 967/ or 968/ or 969/ or 970/ or 971/ or 972/ or 973/ or 974/ or 975/ or 976/ or 977/ or 978/ or 979/ or 980/ or 981/ or 982/ or 983/ or 984/ or 985/ or 986/ or 987/ or 988/ or 989/ or 990/ or 991/ or 992/ or 993/ or 994/ or 995/ or 996/ or 997/ or 998/ or 999/ or 1000/

"BAD"

.01: 256.40 Well, P is 256.38 may well be an example of a "BAD" ("imperfect" "corrupted") TSQ. "I wrote this report" "Perfect TSQ is t. cost of corruption" — on this problem. I had the idea that it could vary in an  $\infty$  cc of search, it sometimes makes it prohibitively large.

My more recent ideas, hrr, were that we shouldn't depend on 2 TSQ being near "perfect". Maybe for instant TM, we may use perfect TSQ's — but later on, I expect TM to be able to deal w. very imperfectly constructed TSQ's!

.09 One way would A.H. deal w. 256.38 (2) with a somewhat more general disty of this kind): TM finds an operator that works 3+7, then looks for other Q.A.'s in which this operator works, then tries to find a way to identify the Q.A.'s in which that operator works.

.12 Actually (.09-.12) is not so A.H. It amounts to a way of "paraphrasing" the corpus in a useful way!

(N.B.) the problem of det 256.38 is its "to (n)" (.09-.12) is an example of an unworded "Bach" corpus — Harder for TM to learn, but much less likely to be "imperfect": That it can be a realistic corpus for TM, is very good, in the sense that TM has some idea as to what its "future" problems will be. This enables it to deal w. what would ordinarily be done by TM2 — i.e. to have a feeling for what "chords" are "interesting", in the sense that they are likely to be relevant to "advanced" parts of the "Bach" corpus. — I also vaguely remember this "Bach" corpus somewhat enabling TM to deal w. cc

minimization is a fairly non- $\infty$  way. — I'm not sure just how this was supposed to work! — I would strongly

under the writing of TSQ's a lot easier! — 258.06

Note, hrr, that my initial goal is to get info into TM! — That the "sequentially" of the corpus can contain imph. info, is I start by giving TM distinct "Free Free". Later, I can weed TM from this by giving TM the documents of the corpus in larger & larger "chunks", until I am adding chunks that center into that TM will not be able to deal w. at the time. So he will learn to recognize these corpus areas &

.33 realize that he is not yet able to deal w. the chunk "Textbook" — 258.06

.34 So this is a standard, simple, method of theory revision used

in physics. Old model doesn't work on  $Q_{n+1}$ ,  $A_n$ . Find new (usually narrower)

model that will work on  $Q_{n+1}$ ,  $A_{n+1}$ ; find way to recognize  $Q_{n+1}$  as different from

.28  $Q_n$  ( $i \leq n+1$ ):  $(\text{Unity}) M, M' \rightarrow M$ , which is a shorthand of code for

$M, M'$ . — (note some aux. problems! 258.15-17).

.39  $\rightarrow$  Note one non-obvious way to do (.34-.40)  $\rightarrow$  271.34-40  $\rightarrow$  258.05

TM most

.01: 257.40 While 257.34 is "not bad" it is not optimum. It is e!. TM most natural way would, when Q<sub>int</sub>, A<sub>int</sub> remain, do a direct search for a good model for [Q, A, ?]  $\approx$  /  $\approx$  /  $\approx$  directly. For this to be even mildly interesting, we must have a reasonable description of search space of  $A \in f(Q)$  functions  $\approx$  (256.11)

.06 257.33 257.26 A Commonly Occurring "Batch corpus" of this kind, would be the problem of getting TM's to <sup>(understand)</sup> compress a large English text. A v.g. way for TM to work on this would be to find parts it could compress easily, then find more difficult parts, etc. I expected that TM would learn to "read & understand" English text in this general way, but it hadn't that or it as a "Batch Corpus" w. TM going back (later to try to code or recode a section that it didn't "understand" it later (or later) time around. I really want to get TM to pt. at which it can do "Batch Corpi" of this kind: <sup>removes writing temporarily</sup> **TSQ's very easy!**

One recurrent problem: TM has to decide when to quit work on a part of corpus & work on some other part - (hoping to eventually return to that part later (is wiser)). This judgement also occurs in e.g. 257.34-40!

.15 We find M' for (Q<sub>int</sub>, A<sub>int</sub>). How good a model must M' be before we go on to + "Q<sub>int</sub> recognition problem" & "M, M' 'unicosity' problem?"  
.17 we write do one M' then if it's no good also the entire part didn't work well, go back & try for a better M'. (or even a better M! super back back!)

Could I get TM to learn Algebra in "Batch Mode"? I would start out (perhaps) w. a "linear" + TSQ & switch to "Batch Mode" instructions as soon as possible. The "sequencial" TSQ has more info in it - the explicit ordering - really makes it a lot easier for TM.

Best way, start out in sequencial Mode, then see if I can get TM to work in "Batch Mode".

[One of the good pts about "Batch Mode" is that it might be easier to define TM's long term goal in terms of this batch. If the batch is of infinite size, we want TM to understand, work as many probs as poss. in a given time. This means we have to define TM's "Horizon"! Also the trade-off betw. Good compression for a small part of the corpus, vs. weaker compression for a larger part of the corpus. I think the horizon is a trade-off. .31-.32 Most Be User Selected.

One poss. Good aspect of "Batch mode" TM could be like a Grad. Student & Ask Questions of User occasionally.

Another aspect of TM's work TSQ's part I've sort of neglected is + "ADVICE CHANNEL".

.38 Another idea I've neglected: That one of the big reasons of my wanting TM to work on probs of large CJS, is that only in such problems is (259.01)

development of  
.01:258.40 t. "Overhead" of Various Search enhancement techniques feasible.

How much Time to spend on such developments is a TM<sub>2</sub> problem

- Having to do w/ "Horizon" as well as expected cc of soln.

Hvr, in early TM, I will be using TM problems that will help find or reduce CJS search enhancement techniques.

be a search enhancement methods, or will be close to those such methods - in the sense of reducing CJS of finding such methods.

.08 Still, t/ approach of 255.32-40 is very attractive, & I'll probably do it.

- Hvr, I want to have as much Theoretical Understanding as poss. Before I do it, to guide my practical creation of what I hope to be a very general Lang Elem.

.12 (TM) My functional lang. didn't use Recursion, because I felt it could be faster in execution. Hvr, it seems clear that use of recursion can vastly simplify the expression of many funcs.

Even the simplest recursion in which a function calls on itself, can make a lot of "Simplification". Least may express all recursions in 2 parts: recursive funcs in 2 parts: (1) Pre final simple value of the func for a certain (usually low) value (2) the self-referential definition parts

So I can use recursive defs of funcs, then have a compiler that translates them into loops (or some other fast, low cc, form).

So our slot can be Recursive Perm. Another "Slot" could be a low cc version of the perm. We "Mutate/modify" the recursive perm, because it is a very low by the expression of the function in decs.

OK, so now, T. main problem is my state of understanding of the Proc.

Sum of 6 Lang. problem: 257.34 is reasonable approx:

for theoretical optimum: 256.07-10 (Summary Machines) 256,11-12 (problem at a price for L spec)

.27 for "Summary Machines" I want a more general model than the one that simply takes a bunch of base codes.

for the "problems of a price" of Perm (Q,A) d.f. - Perhaps all the heavy work/need is an updating algorithm for when we add a new Perm. This may be tied up w/ the form of the Summary Machine of .27.

One diff w/ Summary machines - I had no idea of a Perm model than

.34 a set of short codes: In fact any f.d. is an approximate "Summary machine". So stochastic CRG's, linear regress w/ states or are all cases of Summary Machines.

T. method of updating, will depend on the Model (= Summary Machine approx). Most Models don't do OL. Each loop update by

modifying prodys taking new NT's by general Model of Grammar.

defining new NT's by General Model of Grammar (using loops, etc. and other old NT's...)

To run Many computers in 1 for Load ↳ worker computers.  
 One <sup>(control)</sup> ~~(king)~~ computer :=  $C_0$   $C_0$  gives search ranges to each  $C_i$  ( $i=1/n$ ).

- $C_0$  has an input register for each  $C_i$  ( $i=0$ ).
- " " " " out " " "  $C_i$ .

So  $C_0$  has  $n$ -way communication w. each  $C_i$ .

When  $C_i$  gets its range of problems, it starts working on them. If it solves one, it tells  $C_0$ .  $C_0$  (sees its inputs for statements of soln).  $C_0$  then tells all  $C_i$  that are working out. solved problem to stop, and rec. new (problem / search range).  $C_0$  also tells  $C_i$ 's that have solns. to send them to  $C_0$ ;  $C_0$  receives them & stores them.



Whenever  $C_i$  finishes a particular trial, it looks at its input from  $C_0$  to see if the problem has been solved yet.

This arrangement would involve only ordinary I/O ports.

- <sup>NVR</sup> for  $C_0$  to give  $C_i$  a new problem / search range
- but " "  $C_0$  to receive solns. from  $C_i$ , will require a serial port, (or 11 port)

[ really don't know how "port" work - how to address them, & how to communicate cables are to be set up. T. If port is ordinary 2 way.

AS <sup>I</sup> see it r.  $C_i$  machines are all <sup>ordinary</sup> machines, but  $C_0$  has  $n$  I/O ports: These are actual HW connectors, - perhaps each has 2 (2 way).

Alan felt that it could probably do what I wanted in a secure (or ~~or~~ network "server" is a bunch of computers connected to it. - So all computers would be "ordinary". Is there much overhead time for this ~~system~~ network system?

It was thinking  $C_i$  need not have a hard disk: Maybe 64k ram is floppy to start with.

.01: 259.40: Another kind of p.d. is Post used for T.S. regression. Here we update by modifi-  
or params, ↑ no. of coils, use of non-linear coils:

In both Stoh long is T.S. regression, I'd like a way of updating operations that was  
"Universal", in the sense that ALP is universal, is a loop that finds any finite  
derivable way, of size  $n$  over large  $n$ . ← (S78T3)

.06 In regression, by employing many linear & n-linear coils, one can approach  
.07 a kind of "Universality", since any funct can be approx'd this way.

Similarly, feedforward ANN's can approach any function - in  
some ways, better than .06 + .07

Tho, I think even ANN is not really "Turing Universal" in the sense of S78T3

Rissanen's work may be relevant, but I find him very hard to read

I do have a paper of his, somewhere at Generalized Regression. Paper from the ISIS conf. attached. Abstract on p. 4 of ISIS conf proceedings.  
A purely numeric form of  $[Q_i, A_i]$  is:  $Q_i$  is a numeric vector &  
 $A_i$  is a scalar or vector. This is the general/curved ML problem.

.15 Again, using many ML coils, or ANN can do the job. → (.22)

A nice way to approximate ALP is what Riss does: He lists a large (perhaps  
infinite but enumerable) set of  $P_{i,j}$ 's, & he uses a system in  $S_{64}$  (T. one I  
dubbed as "Macropolis").

So, in General Induction, we can use a weighted Mean of Prod. methods,  
wts. (a priori method; \* (pc of coils) wrt. Post Method); This should be  
applicable to all kinds of QA problems; Symbolic Numeric & mixtures.

.22: (.15) Another interesting possy: Say we have  $k$  numeric inputs and a set  
of functions of various types. We can make all functional combinations of inputs using

a function of  $k$  inputs.

.25 N.B. In .22 we also have to include constant inputs! Please see  
Continuous params in addition to  $k$  normal  $k$  inputs. This also applies to my earlier  
analysis of "functional composition" of 130.25 - 131.18

.28 Anyway, one of the ideas of Post's functional logic is that any (prim. recursive)  
funct. can be derived by a finite  $n$  composition of primitives. (Riss is much satisfied if  
definitions (as in  $\geq 14$  notation) are used.) T. notation is a pre-processed copy

string as in  $\geq 14$  & pc's are automatically assigned, as in  $\geq 14$ . → see 262.12 for recursive details

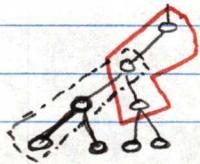
→ There is, however, the problem of listing  $f$  functions in  $\geq$  pc order  
If we allow a set of primitive functions to be both symbolic & numerical,

we can get a p.d. over all  $Q \rightarrow A$  functions  
Some such primitives: AMS & M → True also False.  
Boolean functions of  $T, F \rightarrow T, F$ ; T. various Numerical functions  $+ - \times \div$ , etc.

Various Control functions,  
Actually, a set of functions used in "Basic" would be about adequate.  
It does both strings & numbers.

.01: 261.40 : The development of 261.28-40 is fine, but its pretty much  
 4. same as A/P: except that I use a kind of extension of TRMC,  
 and I <sup>think to Z141 Method,</sup> automatically sum over many of M. codes, to get a list of various functions.

.05 In coding Function nets, is there much of a parsing problem? —  
 I think there might be: I could describe this net using a tree based  
 macro, or the ~~initial~~ macro.



So, if I have a certain set of Macro functions —  
 each w. its assoc. PC, I will have to try  
 re-parsing it, every time a macro is new needed

~~Macrofunction~~ "Macrofunction" definitions (this is Wolff's idea) → (18)

.12: It might be poss. to write <sup>recursive</sup> ~~Recursive~~ Definitions using the idea of 261.28-40.  
 T. recursive defns, that would be evoked would be of the form:

Defn. of  $F(x)$ :  $F(1) = 1$ ;  $F(x) = x * F(x-1)$ . [defined  $R(x)$  for positive integers only]

I'd have to find a way to express this in b. Z141 formalism.

First go thru formalism of 261.28-40 in some detail.

.13: .12 Actually, this Reversing could amount to an important "REFORMULATION"  
 of the <sup>theory</sup> code! One time it may occur is when a new defn is made  
 on the pc of ~~old~~ old defns that changed much — both occur w. Growing Corpus  
 While this may be a common type of Reformation, it is probably ~~not~~ not  
most General kind.

One kind of "reformation": Td1 (ing "1+2; 3\*7, 4-8, 6-3;"  
 as individual ~~cases~~ classes! Then it looks at <sup>some</sup> Pro (expresses for all of them  
 is ~~coarser~~ simpler expression that covers all cases. — T. reversing of .05  
 does not cover this. In this case perhaps "Integration" is a better term than "Reformation"

The reversing of .05 could result in an entirely different looking code  
for t-corpus!

Anyway, T. problem I've been working on, is to describe a less c/l. way of  
 doing QA induction than 257.34-40, 257.38.40 is pretty "standard" in sciences  
 I imagine. On the other hand, the Non-~~of~~ method of 261.29-40; 262.01-02 is  
 closer to A/P, but w. b. advantage of (.01-.02), As is, it is not ordinarily practical for  
 a large corpus, but it could be used for a small ad hoc corpus  
 (like Phi, Ann)

The 261.28 ff is probably usually used to evaluate a parsing of a corpus.  
 The actual functions defined, are normally found by other means (as in  
 the old Z141... for finding nouns by noting traces of occurrences.)

Bulg.

01:262.40 Another fact on P<sub>12</sub> problem, each CAG's give a p.d. on finite strings.  
 - So it's a sort of soln. to the Big induction problem. It works by assigning pc's to various  
 & rewrite rules (or Matrix Multiplication rules), Z 141 does this also.  
 for B<sub>12</sub> & grammar & k. (proper) corpus.

HVR, f. function descr'd in 261,28-40 are deterministic: Could I do a similar  
 thing & get probabilistic results? Well, as a matter of fact I do! The functions  
 are constructed probabilistically, so what 261,28-40 does, is give a p.d. on

08 Functions, These act (in //) on Q<sub>n+1</sub> to give a p.d. on A<sub>n+1</sub> (!)

09 It may well be that "Backtracking" is the only ~~non-el.~~ non-el. way to  
 get better models in a "Universal" way. [In s. fully discussion, (Q<sub>n</sub>A<sub>n</sub>) ≡ Q<sub>n</sub>A<sub>n</sub>]  
 is meant to be a large chunk of the corpus & a common ~~soln.~~ soln. (common Matrix function)]

So, say I get a soln f<sub>n</sub> for [Q<sub>n</sub>A<sub>n</sub> & |n:]. F<sub>n</sub> doesn't work on Q<sub>n+1</sub>, hvr.  
 So I back track: When F<sub>n</sub> was found as a ~~soln.~~ <sup>soln. for</sup> ~~matrix~~ matrix I also had  
 other solns that were not as good (if we did any "oversearching") - perhaps  
 many of them. In "backtracking" we try these solns on Q<sub>n+1</sub>.

If none of them work, we go back to Q<sub>n</sub> & look for solns that work for both  
 Q<sub>n</sub> & Q<sub>n+1</sub>. It was can't find any we may back track to ~~Q<sub>n-1</sub>~~ Q<sub>n-1</sub>!  
 To try to find a soln that works for Q<sub>n+1</sub>, Q<sub>n</sub> & Q<sub>n-1</sub>

HVR, Normally in inductive coding, we don't use such Non-El. Methods of Backtracking.  
 We use heuristics that narrow & search down considerably & in doing so  
 we find solns faster, but we tend to MISS certain (v.g. <sup>v.g.</sup> ~~impl.~~ <sup>impl.</sup>) solns that a Non-El  
 technique would find.

23 In General, when ~~work~~ <sup>work</sup> problems using 257,34 & other El. methods,  
 I will try to see how I can make them less el. Also in 277,34, the  
 (Unify/integrate) phase search can <sup>employ</sup> sometimes ~~the~~ <sup>the</sup> Backtracking  
 or (.09) <sup>or</sup> ~~or~~.

I want to write a review of recent ideas on Non-el. of  
 257,34. Also, perhaps expansion of the ideas of 261,28-262,103  
 plus the notes on P<sub>12</sub>'s of 263,01-.09 (A. Non-el. soln. of T. problem)

20 T. Problem This is imp. ! One of big advantages of ALP over other induction formulations  
 is that given an induction system, it suggests how to improve it. I really want a system  
 that is "usefully open-ended" I know that w. finite CB, I cannot expect to  
 23 get best possl. induction. T. Q is, given extra CC, how best to spend it.

One way to spend it is on hyp pc trials that haven't yet converged.  
 25 I think the spirit of the soln. to .20-23 is: We start out w. a general UMC  
 biased by whatever ideas we can think of. We use this UMC w. L<sub>1</sub> search to find  
 solns. to simple problems. We then bias the UMC in view of the solved problems.  
 We then continue L<sub>1</sub> search - used to biased (the still Universal) UMC.

Hvr, the trouble w. .25 (if it is indeed the trouble) is that ~~the~~ ~~the~~ 264.01

0.1: 263.40 "Summarizing Machine" used to incorporate & solve problems, is not a complete summarizing machine, so we have to use "backtracking" (like in 263.09-.23. This is rather non-ai backtracking, in my impression is that it is very expensive.

.05 I'd like, perhaps some kind of Mix of the elimination of 257.34-.40 and a Non-ai method (like maybe backtracking, but not exactly 263.09-.23.) So .05-.06 seems to be where I am now.

I want to be able to use Heuristics, yet I want to be sure the System is Universal.

It may well be that "Scientific Method" as practiced by the Sci Community, is not universal, that it depends too heavily on certain heuristics - that it does tend to "Paint itself into a corner" so much, that the art. of backtracking (≡ Recoding) that would be necessary, is quite impractical! (E.g. drop all of Modern Physics & start over!)

However, Modern Physics summarizes an enormous amount of data - so any new formulation would have to track its models closely! - This is what variations on standard Relativity & QM & "standard model" do.

Unfortunately, the Sci Community doesn't much tolerate dissent!

.18 **Another tack!**: I think one of the original ideas, was that one starts (try to TSD using a ~~complete~~ set of instructions: that the initial problems are such that the backtracking set makes for ~~easy~~ find solns rapidly. After solving a few <sup>New</sup> problems, the P.D. is modified in various ways, (new data are made & the various instructions are different PCs) - Making it easier to solve what were before, excessively difficult problems, loop to .31

Note that a full MCT TM can use practically any kind of info to improve its P.D. A very imp. source of info is the traces of its own attempts to solve problems. This is the source of many heuristics.

.31 (22) During the loop of .20-.22, the Machine/PD remains universal!

.32 All searches are always made over a universal (instr set/PD).

→ I have to Reconcile .18-.32 w. the idea of approximate "Summarizing Machines".

.18-.32 Does seem to be a very (GOOD) way to run a TM!

A kind of "Summarizing Mach" more like .18-.32, is what one does in linear regress: After each new data pt comes in, one updates all of the coeffs - Of course this induction system is not universal.

.33 261.28-.40 is a complete (Machine/P.D.) formalism. The Remark of 262.01-02 Makes this system more than just a UMC for ALP. It does induce a pd. that changes automatically as we code a corpus. - we put changes variations in PCs of various concs, & we introduce (data) new concs as we code corpus. A hour would seem to be (probably) a further biasing of the PCs - perhaps in a way that depends on previous codes.

Hrs noted; 267.01-.03

~~Star~~ Sears  
Silvertone Guitar ~ 1960  
Soll to first Guy who wanted to buy it?

or: 264-40: 264.33-40 suggests that parallel coding trials can influence on a zero!!

The way this works: We try 2 certain codes for corpus but it fails.

A MCTM could learn from this one failure (OSL) and perhaps influence the pc of a code ~ to a "failed" one!

So how does 264.33-40 relate to "Approx. Summarizing Machns.?"

(I probably want to consider various induction systems & see how they can be made Universal & how they do "summarizing") e.g. linear/n-linear, ANN, tech toys (cf. a C.D. Grammer)

Re P.D. of 261.28-40 and others that may think of. Does this suggest any amazing classes of Productive functions?

Def Sumes Consider summarizing Machns (Sumes): After a UMC has coded a ~~part~~ part of a sequential corpus, the ratio of 0's to 1's in its shortest code, could be a kind of very weak summary: But in general, this ratio will be  $\approx 1$  because of "randomness" ~~the~~ we can, however, consider non minimal, fl codes: They need not be "random":

Consider a pure Bern Sep: T. pc's of its symbols are a complete desc of all <sup>generated</sup> probs in any of its corpi. — So these pc's are a complete summary of P.D.

But, case of 261.28-40 The probs are a complete summary of the Bernoulli-like regularity in the corpus: These probs also include several "defined concs".

Conceivable E might find a way to express conditional probs. (like a proby ~~vector~~ vector of symbols that follow  $\alpha$ .)

Presumably, w. these probabilities, the prob of creating the relevant corpus, is maximized.

.23 A Big Q is: Can any conceivable P.D. on all poss. functions, be expressed by something like 261.28-40? This formalism expresses or can be <sup>modified</sup> to express, all conceivable concs. — But all P.D.'s on them?

.26 An analogous Q about P.D.'s on strings: Can all poss. P.D.'s on them be expressed by a Bern-like seq in which various ~~conc~~ concs can be defined & given probs? I would say that this is extremely unlikely! — But consider it anyway.

.29 Well in (26) <sup>not</sup> (21), say we consider only P.D.'s on strings that are derivable from summing over pc's of all infinite strings that <sup>finite</sup> they are the prefix of. So the pc of a string most be monotonous as one moves along it.

.31 Well, I suspect that whether or not 261.28-40 is "complete" in the sense of .23, — that that approach is pretty much what our "scientific Method" is — and possibly it is well as can be done by humans (??)

The Q of .26-.30 is interesting! Surely we have more "Universal" methods of assigning pc's to strings! — Probly we can apply them (analogously) to 261.28-40 Are ~~the~~ Hidden Markov Models more powerful than the Bernoulli Model? I think so! T. Bernoulli model is a HMM w. 1 state! So 261.28 could be reduced into a HMM.

CSL corr. to  $\exists$  Time  
Linear Bounded Automaton

See Hopcroft - v. 144 "Intro to Automata Theory" - 100. " p. 221  
finite  
No: CSL ~~is~~ is equiv. to a TMC w. 1 tape containing input ~~and~~ only ~~the~~ can be created & used for more tapes.  
which can approximate

.01: 265.40 well, HMM's correspond to finite State Machines!

Full Umc's! Hvr, CFL's & CSL's are more powerful.

There is some belief that CSL's are Turing Universal. See what extent

It is true. It would have to allow <sup>some</sup> ~~shortening~~ <sup>ing</sup> of strings.  
i.e. rules like  $ACBD \rightarrow AD$  otherwise, ~~it would~~ it would always be poss. to tell if a string were in the lang.

Since strings can be made to represent all funcs in a universal way, a strong <sup>probabilistic</sup> lang on strings should give us a good ensemble of ~~prob's~~ p.d.'s on functions. **GOOD!** Hvr, I don't want to (constraints on p.d.'s on strings) (265.29-31).

They are not what we want. We want a way by ~~prob~~ <sup>Discrete</sup> on finite strings - so like L. v. it's ~~Discrete~~ D.P.: Umc's that stop at end of string. T.P.D. assoc. w. a stochastic Lang., rather than sequence extrapolation

There are 2 problems here: First (the easiest) to get the "language" of 261.28.. to be actually universal! (or Prim. rec. func. "universal") - say to model Lisp or another functional lang. Second (hardest): to get f. p.d. on these functions to be universal. I have been using Bernoulli Models, F.S.M. models, CFG's, CSG's, Umc's (Per Chomsky hierarchy)

.18 Stack Machines One approach: See what kinds of models are needed to express various heuristics that I will need. [for a list of some of them see my "How to solve Problems" sheet.]

One imp't Hvr: "Express problem in a different lang." (A meta-heur is to keep one's eyes open for new "languages"). Also, the process of preparing (modeling) the problem to express it naturally nicely in the new lang. may involve (inventing/discovering) new useful concs that could be used in other ways, namely for "compression" - or to

Simply help solve the problem in a more direct way.

**OSL** seems to be outside the "code" model - outside Chomsky hierarchy.

Hvr **OSL** can be dealt w. by auxiliary Mechanisms (Presumably)

.33 A vague Model of learning that stays universal: We start w. a set of universal concs, so that by suitable composition, we can create any function (a universal just def in the UMC sense). Assume this set has initially all = empty. After we solve some problems, we have new funcs & we have modified p.d.'s of primitives, but our system is still Universal,  $\exists$  (264.33-.40) which was

.33 a Big "Accumulation Pt." in my recent Prob.

.34 As for the "Summarizing Machine" that idea may not be so good in present context. For ~~practical~~ <sup>Summarizing Machn.</sup> induction, T. Zurus machn is little more than an approx to full ALP. The model of 264.33-40 is also an approx to ALP. It is my impressn, hvr, that since 264.33... retains its universality at all times, then at all times a sufficient  $\Lambda$  of CB must solve the problem (if it is solvable!)

.01 A possibl. problem. 264.33-40, is part while it's universal, in the sense that  
 .03 it can code any function, it is not (ordinarily) universal in being able  
 to express any possibl. f.d. on all functions.

.04 However, when one begins to T.S.Q., (Q.A to Q), the system can <sup>and does</sup> do an ~~Q~~ search  
 .05 over all possibl. functions. It does so <sup>if must be over</sup> it ends up w. a simple distribution over  
 all possibl. functions, T.w.f. will be over only a few functions.  
 If the corpus is large, we will have a wt. over all functions  $F: (Q_n) \rightarrow A_n$ .  
 who will be ~~...~~

I'm confused! .04 seems to cause a bit of trouble, but but but...!  
 After the search of .04-.05 (if it oversearches a bit), it will have several functions  
 that fit  $[Q.A_n]$   $i=|n|$  exactly

Perhaps a summary of the last wk's work: (since 155.01)

- 1) Mainly work on Q.A. lang.
- 2) 256.07-10 T. updating problem for Q.A. lang! No problem if complete (CB=0)  
 .15 ALP is used! Otherwise, partial ALP is, in general, impractical, (P.O. occasionally  
 it can be used w. Backtracking as an effective updating method).

[ In .05 when I spoke of "Backtracking" I meant BLIND "Backtracking":  
 Here,  $F_n$  doesn't fit  $Q.A_n$ , so one simply goes back & finds for  $F_n$  some  
 that fit  $i$  upto  $Q.A_n$  & also upto  $Q.A_{n+1}$ . One should try to find lots of  
 them, because  $Q.A_{n+2}$  will cut down their number again - perhaps  
 to zero! (from this pt. of view, no of o.s. points & exponentially w.  $n$ , so it gets to  $\ll 1$  fast) w

There are 2. Modulus of / Backtracking. Syst. that make it more practical.

- 1) When  $F_n$  does work on  $Q.A_{n+1}$ , we don't just do <sup>Blind</sup> blind search  
~~Q.A~~ data up to  $Q.A_n$ : We do heuristic search - <sup>Being</sup> being aware that  
 solutions must fit <sup>the known</sup>  $Q.A_{n+1}$  as well. We do this, say, in physics, w  
 we know  $Q.A_{n+1}$  & we know what ~~Q.A~~ we have to have to fit up to  
 $Q.A_n$ . This latter is characterized by equations that ~~the~~ summarize  
 the data & any new trials must closely approximate these equations.

.29 2) When I did in the updating discussion of 256.07-10, I was considering  
 discrete codes, a finite number obtained by "Oversearch": In fact it  
 may be often possibl. to ~~be~~ obtain  $\infty$  codes that fit. e.g. linear regression:  
 for every part. set of coeffs, we have an  $\infty^2$   $\therefore$  a code for it.  
 corpus. The pt's ~~are~~ w. each code will depend on  $\infty^2$   $\therefore$  on how many  
 coeffs it uses. As new data comes in, we always have codes in the set  
 that will fit it.

.35 ~~...~~ .29 fit may be an answer to 256.11-12

- 3) The Common Method of updating in physics, (is possibly in T.S.Q's of Szeeb: ANK)  
 256.20 - .28 is one only dion of Reg's other dion in 256-267.

162  
267

.01:267.40

4 Batch Processing; 256.30 - 257.33; 258.06 - 260.40:

5 English TSO 255.32 - 40; 259.08 - 11; 266.18

6 On Recursion in algebra T. (any TM uses! 259.12 ff.

7 Why we want TM to work on BIG problems! 258.38

8 On "Summarizing Machines" 259.34 - 36; 266.34 - 40 <sup>← these are not v.g. refs!</sup> recursive

.06

9 T. General (so possibly Universal) model (or TM, but is also practical).

264.19 - 32; 266.28 - 33; 264.33 - 40; 261.28 - 40 <sup>← set of functional languages: possibly recursive → 262.12</sup> (which gives more details on how this is supposed to work)

was



UCC

0.1: 268.40

Definition of Universal Turing



Algorithm  
Algorithm

1) For QA Turing:

Given a corpus  $[Q_i, A_i]_{i=1}^n$ . Alg. gives,  $\forall s \ll t$ , successive approxs of  $P(\bullet | Q)$ . which we call  $P_n^s(A|Q)$  (for  $cc \ll n$  essentially  $P_n^s(A|Q)$ ). we want  $\lim_{n \rightarrow \infty} P_n^s$  to be within a constant factor of  $t$  true  $P(A|Q)$  whenever such a  $P$  exists & is decidable by a finite string (varies when  $P$  is partly by continuous params)

Furthermore, if  $t$  true  $P(A|Q)$  is indep of  $n$ , then  $P_n^s$  is "constant factor" will be indep of  $n$  for  $P_n^s$ . (or another way of looking at it  $\Rightarrow n \rightarrow \infty$ , there is an upper & lower bound for  $P_n^s$  constant factor).

Essentially, all I'm saying is that successive approxs. to  $P(A|Q)$  should have conditions of SOL78T3 and  $\epsilon$ . will converge nicely to  $t$  true values, at the proper rate.

N.11.00 Partial rec. func. are effectively enumerable. Better to use them!

One way to do this: (or to ALP): Consider only Prim. Rec. func.

Let  $P_n^s(A|Q)$  be a enumeration of  $t$  func. of interest. We can assign them  $P_n^s = 2^{-n}$  and this is a complete prefix set system  $\sum 2^{-n} = 1$ .

This is not much different from ALP & has all same disad. types.

I ideally, would like to use all functions  $P_i(A|Q) = \prod_{j=1}^n P_i(A_j|Q_j)$  \*  $\sum P_i = \phi$ .  $\phi$  is a prefix of  $P_i(A|Q)$ . List them in order of  $\phi$ .

268.06 GMS  
268.06 GMS 266.28-33 / other decs of a long system that seems to be universal.

At any time, if we use another  $cc$ , it will eventually try to correct function. so it will however be worse than  $t$  correct function by a constant.

But this constant is based on a pairs of various functions, it changes as  $n$  & we progress in the seq. If a long system is any good,  $t$  constant factor, will  $\uparrow$  W.M (I assume!) Hvr, if  $t$  true func is included, any of the systems I consider will probably give a  $t$  by wt. (No! — they will give it by  $\epsilon$  part but  $t$   $\epsilon$  part need not be so large — in fact,

if I don't have a adequate soln to a "Scaling" problem, the  $\epsilon$  part will be "Swamped out" by many, many new conc. data. functions!

In '15 I wrote about a MTM system for QA probs. The functions I try are not probabilistic. But deterministic. are not probabilistic. But deterministic.

are accepted only for a perfect fit over  $z = 1/n$ . For  $z > n$  they give a not infinitely sharp probability distribn.  $\{$  Actually to seq. In '15 I used  $P_i(A|Q)$ , a soft probabilistic func.  $\}$ . Hvr, if, in the problem of  $\epsilon$ , I regarded it as a NMTM, I really want to use probabilistic functions for trials. One simple way is to use deterministic functions w. a "error cost" function for correcting them. Formally, this is the same as the deterministic treatment of '15 ff, but it seems to make search easier. Because we get some reward for every function we try. Also we get (usable) feedback back to  $\epsilon$  search over  $\epsilon$  functions.

1.18  
1.21  
1.29  
1.30

This is from only of  $P_i(A|Q)$  are not probabilistic, but  $\epsilon$  is made up of no functions.

Try to find TELNET on HATS scope.  
② In a Explorer.

0.1: 269.40: There are 2 common ways to get corrections: ① If outputs of function is binary seq., the error would depend on no. of output bits & no. of error bits, I found 2 reasonable functions that did this O.K.

② If outputs real (or complex) m.s. error can give amount of info needed for correction.

A more general form of function (of 269.15, 18) is  $P(A|Q)$ , in which  $P(A|Q)$  can take any form. In 269.15 I used Prim. Rec. functs, so they were enumerable, and I could assign  $p_c = 2^{-i}$  to the  $i$ th one.

But perhaps that is not to Pt.. We can (perhaps) easily find a set of functs for such an  $P(A|Q)$  is "Universal", - Rec will work for a simple problem Rec is "matched" to the set of universal functions. The Q is: when we learn we modify wts on to sequence of functions was search on: Do we retain universality?

If so, what happens to the "constant factor" (does it expand (desirable) or get smaller (Undesirable)?)

Probably its easy to retain "Universality": The big Q's are .13-.14.

269.14 - So discuss +, "Constant factor" problem.

SN Going Back to the "Summary Machine Problem": w. a Computer (ec = 00) Summary Machine, there is no problem (except, perhaps osc (?) ).

For a summary machine that uses only a small no. of codes, the no. will grow exponentially w. corpus length & eventually we have no codes to know to backtrack.

① No way to sort of deal w. this is to have a very large no. of codes - i.e. every bit we receive is an acceptable code, but in most cases, the pc of correction (.01-.05) is very small & the code gets very small pc.

However, we can have to store large no. of codes for a corpus  $2 > n$  because every time  $n$  is, all of the old codes are still valid, but they have different amounts of "correction pc". This seems to deal w. the exponential  $2^n$  in the no. of valid codes in .19-20.

However, the .18-.27 will give lots of codes, I suspect that they will not be good codes, because they are all the same initial function, but w. various amounts of correction for each corpus  $f$ . Think in terms of a  $Q, A$  problem pair sequence. We started w. 1000 functs that map  $Q$  into  $A$ . Each of the functions can do the entire corpus, & each will have corrections for each  $Q, A$ . So, essentially, we try each of the 1000 functs on the entire corpus & we add in the needed corrections for each to get the total bit cost  $\rightarrow$  prob. I don't see much "learning" taking place.

Could I do .18-.27 with new definitions, changes of wts, & "reformulation"?

① would it run? ② would it be universal? ③ would the "constant factor" remain large and to be practical?

Using a "Gray" fit criterion, it would be poss. (perhaps) to use conventional GA (or GP?) to find short codes! The "corrections" need not be part of the code.

01:27:40!  
as for 257. GA GOF (goodness of fit) is concerned: It is simply part of f. in the next  
02 computes the GOF scalar.

03 Hvr, I think the Main Problem: My expected Method for TM is 257.34-. to  
Is it universal? If so, does the "constant" c remain large, - or does it stay  
large and to be practical?

06 Well, in 257.39, we normal (at first) choose  $\tau$  so that "c" (which is  
essentially  $\approx \epsilon$  C.J.S.) is unusually reasonably low.

Perhaps the real "Bottleneck" of "Universality" is "Good heuristics". TM could  
read Math Literature, try to verify proofs, etc., w. the goal of finding heuristics  
in this corpus. Perhaps TM could look at Notebooks of Gauss &

Ramanujan, etc: General books on heuristics might be of some value.  
T. Book "Numerical Recipes" & some books by Knuth may have many heurs.

Also try Carr book (that Ramanujan collected) for heurs.  
My "General Problem Solving" list.

So, is 257.34... "THE Method"? (Many details need to be  
worked out).

SN There is the general Q of "how <sup>short a</sup> algorithm code is "adaptive"? In MTM,  
this is easier to answer, but even then, if we have a very long proof,  
would like something shorter!

20 On the adequacy of 257.34...; This seems to be the way the Sci Community  
works. There is the general Q. of whether "T. true models of Universe" are  
assessable v.2. Part 2. It may be Part by starting out on a different path,  
one would end up w. considerably different models: Some of which might  
be the better in certain Domains, than current "Science".

25 So: I think Part 4 Problem is not "Is 257.34 Universal", but "Is it likely  
to give ~~the~~ good models for various Domains" - i.e. Does it have  
"reasonable" C.J.S for a "True Models" of those Domains. - A system could  
be universal, yet have excessively high CJS for impt problems, for the  $\tau$  SQ  
that we would use for it.

As is, I am assuming that I can give TM an education close to what  
a human would have, plus its ability to read much much more than a human.  
The selection of "what to read" by TM will probably be much different from  
that which a human would choose! So I might want to tell TM what areas to read.

34: 257.39: A way to Non-GL. 257.34 (abit!) when TM is given (Qnts, Anns),  
It tries first to find a function that will solve  $[Q A_n] \approx 1/n$ . (The non-GL problem)  
This can be done by direct search, using a suitable guiding PC function.  
Hvr, one heuristic way to do this is 257.34-. to i.e. Try first find a function  
to do (Qnts, Anns) only, then integrate (unify) this function into the old one for  
 $[Q A_n] \approx 1/n$ .  
(Actually, this is not a bad normalization!)

0.01: 27140: 257.34... can further be genzd. so its more "MCT TM". The Q's can be inv. probs, OZ probs ~~induction of Time Series or Bay induction~~, and f. (t's) can be tree answers to Ruse problems, It would work in an obvious way for inv. problems. For OZ problems, f. Q would be f. problem dcm: M.C.) is CB. ; f. A would be a reasonable result. [This doesn't seem reasonable!]

Anyway Bay induction could be done w. ~~NONA~~ <sup>null Q's is various A's.</sup> ~~arrangement of Q's & null A's.~~

~~Method~~ How to do Time series induction is unclear.

Anyway: A better way would be to do as MCT says: Have 4 (or 5 if want) Q, A as 2 special (mode) ~~is~~ modes: INV, OZ, T.S., Bay induction, QA.

All info from any soln. or trace of a soln. is put into f. ~~the~~ **Grand PD**.

All searches for solns. are simple Lsrch's (except for OZ problems - in which case we have Lsrch over O.T.'s (which are non-simple objects))

f. "Grand PD" also contains info about O.T.'s. Given an OZ prob dcm as input, the "Grand PD" gives a pd. over a appropriate O.T.'s (≡ OPEN. Techniques).

**Def GPD**

There seems to be an inconsi in my ideas about f. **GPD** (Grand Prob. Distribn).

In an OZ problem, f. GPD would give a direct ordering of trials. (a cond. pb., w. f. prob dcm as "condition". On the other hand, in heuristic search, one has sub-goals & f. GPD tells one how to achieve Ruse Subjects.

which is not comparable w. GPD order to INV trials directly. → Note 273.27

0.20 One way out: Given a INV problem: 2 ways to solve it:

- ① Use Lsrch on GPD's directly obtained cards
  - ② Try to break down problem into AND/OR Not & solve it.
- ↑  
 ↳ This partitioning: ② Pass whenever it is reasonable.

0.22 **SN** In all INV probs: A proof that there is no soln. is also an acceptable soln. So usually one tries to find soln and prove there is none (unless one can prove soln. exists, which disproves non-existence of soln).

Actually, 0.20-22 is pretty much a standard Heuristic. At f. Bojning TM will not be to do much in f. direction of finding AND or OR Breakdowns of problems but later, Ruse will become very common. My Goal Soln. of f. AND/OR not very becoming. (Tho I have a severe Ma Recidology, I solve mainly worked on "OR" problems and even in Ruse I'm not so sure of f. soln.)

0.30 273.02

Most Math probs of any diffy at all, are broken down into AND/OR nets of problems. X'ing a problem into an AND/OR net can involve Great Intelligence!

Both AND & OR skills will have to be used.

So: TM would do Lsrch (for INV problems) only if Ruse were "atomic" i.e. not breakdownable into AND/OR nets. Unless any of f. other 4 types of 0.09 could be "decomposed". Sometimes Time series & Bay induction are decomposable,

~~but~~ "OR" by x'ing f. original data in an invertible way.

(This may be done by in the linear → quad → cubic soln. of eqns!)

A time series or Bay, might be better viewed as + AND of several T.S. or 273.01

.01: f. ~~the~~ Bags might be considered as the AND of several Bags.

OZ problems can be formally solved by a monotonic function of the GPC.

In M2R problem  $x \rightarrow \ln x$  or  $x \rightarrow e^x$  often simplifies an optza.

.03: 272.30 Once again on this heuristic: Start out w. Lsrch on a problem: if it isn't solved by a "certain time", then ~~try~~ try breaking it into AND/OR Net.

Priz "certain time" would have to be lnd by TM.

In Solving probz (all sorts) by Lsrch, the Lsrch is not always to find a

.07 direct soln to the problem. — T. Lsrch is on "What to ~~do~~ do next" → (27)

Def Info on tasks of Priz sort is contained in GPD (Grand PD)

.11 [SN] On Updating GPD: In linear regression after n data pts, one has Bag vector of coeffs,  $\vec{a}_n$ , that "fits best": when data pt. n+1 comes in, the search can be re-essayed for a update on  $\vec{a}_n$  can be in a "small region" around  $\vec{a}_n$ . If  $\vec{a}_n$  is a k dim. vector, this search is over a k dim space, say over a small Gaussian hyper space region.

.17 In ordinary linear regression, the data in this space is uniform isotropic; but in non-linear curve fitting, it need not be isotropic. Perhaps the easiest way to do this: the  $\vec{a}_{n+1}$  that gives zero error for the n+1th data pt, is a k-dim space ( $\vec{a}_n$  will normally not be in this space). Draw the shortest line from  $\vec{a}_n$  to this k-dim subspace (it will be orth to the space).

We can then compute just where on that line the "best fit"  $\vec{a}_{n+1}$  should be. The tradeoff is betw. error in the n+1th data pt. v.s. error in all of first of k. data pts.

.23 To what extent is the General problem of updating GPD (for ar by n numeric/symbolic) functions, similar to all -17 in particular, 17-23 ?

.27 (27) Perhaps an easier way to get heuristic into into GPD: A "soln" to a problem is not just the final soln, but the trace of the soln — w. perhaps emphasis of the "correct" decisions part in the trace. This is analogous to:  $\sqrt{81}$  is not just "9" but the process by which "9" was discovered. A simple case would be the soln. of (non-linear) linear Equs. see 27.13 & 275.03-14 for relevant "Comments" on this →

.32 (27-32) looks like a very important idea that I've forgotten! → 275.05

.33 It tend to think of  $\sqrt{10}$  as an OZ problem (inverse of  $x^2 = 10$  — finding  $x$  s.t.  $x^2$  is close to 10). But " " " " solving known equs as inv. problems, the way can be solved → OZ probz.

One kind of "Hint" for solving linear equs would be to give an example trace. The "degree of hint" would depend on how close to a real problem was the example.

268.40 ← Reviews

5 types of probs:  
1. Inv, 2. Q, 3. T.S. induction, 4. Exp induction, 5. Q.A.

0.1: 273.90 Expt I does since 268

① (269.0) Defn. of "Universality" of a learning Algm.

② Idea that  $\uparrow$  is a guide to small CJs for all opt problems in  $T \& Q$ . 271.06

③ is 269.29 that we certainly have to deal w. "Scaling" problem, if we want "universality"

0.5

④ For t. Model of Inv of 257.34... ; ② <sup>very imp.</sup> ~~Observed~~ <sup>heuristic</sup>  $P, T, Q$  (Solve problem "locally" then <sup>unify</sup> "globally" <sup>Trans.</sup>)

⑤ Generalizing 257.34 : so "Q" is decn of problem (INV, Q, induction, Q.A, ...)

"A" is the correct Answer. (272.01 is in this direction, but not as good!)

⑥ Use of standard AND/OR net for soln (as heuristic) (272.20)

⑦ Defn. of most problems (liko solving exp) is that "A" must be f. ~~Trace~~

1.0

"Trace" or t. soln. (not t. soln.) [Note 275.03: TRACE contains many properties ("slots")

What (beyond <sup>0.5-1.0</sup> ~~Trace~~) must be added to 257.34 to make it "complete"

Inv. Algm? Well several aspects of it haven't been worked out. A big one is (unification/integration) (257.28) — it is a "special case" of f. more general

Def LITM<sub>2</sub>

"Limited TM<sub>2</sub> problem" of making a <sup>hyper pc</sup> ~~hyper~~ model for t. known  $[Q_i, A_i]$  set.

Whoops! — Place is f. original corpus  $[Q_i, A_i]$  set, but more important is f.

Def

~~discovered~~  $[Q_i, A_i^{TC}]$  set:  $A_i^{TC}$  is Trace soln(s) for  $A_i$ .  $A_i^{TC}$

Do we want TM<sub>2</sub> to work on a hyper pc model for  $\sum [Q_i, A_i]$  or  $[Q_i, A_i^{TC}]$ ?

Perhaps BOTH! from a LITM<sub>2</sub> pt. of view  $A_i^{TC}$  implies  $A_i$  (can be derived from)

So they would be equivalent.

How TM<sub>2</sub> (unlimited) is mainly interested in near future & <sup>weighted</sup> ~~some~~ <sup>more distant</sup> future <sup>depending on "horizon" as</sup> ~~future~~ <sup>Given by USER</sup>

01: ~~TM's~~ <sup>space</sup> 273: 27-33: on using the TRACE of TM's Soln. to a problem  
as the TM's remembrance of the Soln. of that problem!

03 Well, the "Soln" can have many "slots" properties: The "Trace" is the most general one;  
The actual final "value" is another (kind of "summary"), The cc is another,  
perhaps other imp. properties of the trace. (was it recursive? Did it have  
loops? What were its I/O Types? Range, Domain...)

Anyway, I had previously been considering using (only) the function  
trace of the Soln. as the "Soln". The "function trace" is the same as the trace,  
in cases where function traces are possible. The trace is more general;  
can be used when there are loops or no recursions. The trace also has cc  
info. in it. Funct. trace - well it does also, since it is the trace for the problem  
in which it is used.

13 So 273. 27-33 is really only a (wild) generalization of what I've been doing  
w. my "Functions as Answers" approach.

Another possible generalization. The trace functions I've been using correspond  
to Deterministic Automata. Now, a more general (but is non-deterministic  
automata (in which a state may go to two or more other states), in its  
probable variant, in which the state transitions have PC (Hidden Markov Models)

**N.B.** The Prob. HMM allows loops of states, it is still much more than  
just a grammar (Phrase structure Trace language)  $\equiv$  PSL's

In MTM we want  $> 1$  soln. to the problem if possible. Do I want to express  
this set of solns as a (N)Deterministic lang., or a stochastic lang.?

The trace of a soln could involve exploration of the parts of a  
Non-Deterministic Lang.

Given a INV problem, giving a stoch lang. as a "soln" is a way of  
narrowing down to PC for Lsearch

$\rightarrow$  **SN** The First GA says that the PC order is best for minimizing cc of soln.

Now, this may not be our goal! We may want to be getting info; in which  
case, we may broaden our search! (Perhaps the Monte Carlo Search of GA?)

In fact this may partly justify the otherwise very -wasteful Monte Carlo Search of GA.  
Now, GA usually (or always) doesn't use its info very well - i.e. it doesn't use more info  
than "poor fit" errors very well. It does get more "Diversity" than simply honed Lsearch.

T. main idea of the TSO: In the initial TSO, I will be very aware of  
all the concs. used in what TM's CS is for all problems. I will use Lsearch for solns. I think  
that given this is the only system that will work! To have an acceptable CS for a problem  
the concs have to have been required by TM. After TM has acquired a reasonable  
no. of good concs, I want to be able to derive TSO's wo. without my detailed  
understanding of their Conceptual Structures. After TM has done another TSO's  
I expect it should be able to continue in less & less care on my part in writing TSO's.

.01: 275.40 T. most immediate goal is to acquire a fair understanding of Algebra (possibly enfl to work somewhere hard prob.). Next, learning to understand English Text about Algebra.

T. <sup>orig.</sup> method sat 274.05-10 should be uneasy to specify. T. ~~entire~~ entire (orig. technique should be expressed int "English soln." of problem.

Hvr, 274.05-10 may help me express T. English soln. in <sup>clear</sup> unambiguous form.

.07 Also in the English ~~is~~ is soln: When a heuristic is found or we just want to incorporate it into "discovered" in a soln of a prob. in the TSC - First Trial, in English, just how this new info is supposed to influence subsequent searches for prob. solns. Then, find a formal lang. in which ~~some~~ <sup>some</sup> modifs can be inserted so as to modify the P.D. expressed by the modif lang, so it expresses the how or the knowledge level from the problem soln.

.13 So the English TSC is solns should be guide language design. By "language", I mean TRMC or "P.D. assoc. w. TRMC".

66  $8 \times 8 = 2$   
 $8 \times \frac{1}{2} = 5 \frac{1}{2}$

At times I don't know just how I want to info in a newly solved problem to influence future searches. — I often have a qualitative idea, but no key as to a quantitative idea. T. quantitative part usually comes from ALP analysis.

→ Hvr, I do have to express what I'm doing in some exact lang, as soon as I do so, ALP is able to give me pc's. I need a lang that can express how as well as "problem solns".

[SN] T. no. of bits in a hour or rule doesn't really measure its pc! Any "OR" statements mean the rule ~~is~~ <sup>has</sup> really/several parallel codes so pc  $\approx$  pc x 2 for each "OR":  
"And" statements divide pc by 2.

So, say to start, I have a lang. to express functions. A set of primitive func's

.25 Consider  $\begin{pmatrix} 1 & 1 \\ 1 & 1 \end{pmatrix} \leftarrow \{ ? \}$  type problems: Say TRM recognizes "nos. & s. symbols" (= nos.)

.26 add, sub, div, mul operators are available; they go from 2 nos. to 1 no.

.27 So it's "natural" to try to represent 2 nos. in the problem to get to solns.

I don't have a lang. for TRM to do such "reasoning".

The fact that "sum", say maps no. pairs into nos., is an "empirical fact" found by TRM thru statistical analysis.

[In general, all of Mops, including axioms, can be regarded as "statistical info" obtained w. very large  $N \approx \infty$ : very likely to have pc close to 1 or  $\phi$ .]

So: I want to show how reasoning of .26-.27 is obtained ~~via~~ <sup>via</sup> the outgrowth of statistical observation on the corpus. It may be possible to assign  $\phi$  pc's =  $\phi$  to natural ideas if I like. — i.e. the generating P.D. should be at least flexible!

There is the general Q of how to express various constraints (obeyed by "necessary" into the P.D. in a way  $\rightarrow$  such could still be used effectively. <sup>sp50a 277.29 is 32</sup> For good ideas in this. F had this idea that P.D's could be expressed in many different ways? Back 277.40

one by trial in probabilistic Analysis was to view a P.D. in various ways - but enabling Soln. of a problem. Viewing in various ways is a Major Scientific Heuristic. (e.g. change of coord system; Time domain  $\leftrightarrow$  freq. domain; Minz  $\leftrightarrow$  Maxz; GRC  $\rightarrow$  monotonic function of GRC; )

One (apparently "IMP") idea is that a Trunc formulation can express any derivable P.D., & this form is easy to implement Lsrch.

One apparently "simple" way to create a Trunc from a P.D. is to list the strings in PC order, then assign PC's via Huffman Coding.

Even finite string has a PC, so one starts w. null, 0, 1, 00, 01, 10, 11...

& assigns PC's to each ~~str~~ via a known P.D. We then & somehow assign Huffman Codes to them.  $\leftarrow$  (No! P.D. is wrong! want to assign Huffman Codes to all strings of some length (since  $PC_{str} \leq PC = 1$ )).

So first assign codes to 0 & 1, then assign codes to 00, 01 & 10, 11: The code for 00 sig. will be "i" code for 0, w. extra bits.

$\rightarrow$  This will not work! A code for an n bit string will be n bits long!

Perhaps read Cover-Chang Program. (But actually, I don't think this impl. int. presump problem: 2)

So a imp. Q is: Is it feasible to put all P.D. into Trunc form for Lsrch?

(Can I do as Lsrch w. a less constrained form of P.D.) All I really need is cond.

(or strings) in PC order. (Perhaps knowing  $\leq$  at each pt. in derivation could minimize relay need for exact knowledge of PC ordering)

Anyway, I want to look at a P.D.'s that I will be using, see how various Heuristics affect their PC ordering: see how they affect Lsrch.

As I see it: I. mean Q is, how problem solns affect a P.D.

(Since Heur. can be expressed as "Prob. solns" w. suitable CSZS), in terms of ordering of PC ( $\frac{PC}{CC}$ )

We don't want to ~~use~~ approx. ordering of trials to leave out any very promising ones

It could include many apparent low PC trials. — This is an analysis of relative badness of different kinds of errors in ordering trials.

One way to get reordering suggested by a Heur! To look at reordering that occurred in the Methodical Pseudo-Cases Post-discovered & Heur in Qstr. — Perhaps

make an "analogue" reordering in a problem that the Heur is to be applied to.

Every time a problem is solved, a "demon" is created to look for probs of that type in the future. (or for "Analogous problems!"). Periodically, various demons will be united (integrated), perhaps w. some compression as well.

Model of Satisfying Pandemonium.

A nice lecture 32: It can deal w. OSL. It is can be an Imp way to

deal w. "scaling" (280, 34)

01: 274.40: OK: Back to <sup>ANLTS</sup> Q of 276.25 i.e. Hour of 276.26-27.

'slots'

It is poss. that TM has studied f. operators statistically & "knows" much about their properties.

[N.B. random nos as test objects, it's unlikely that T.M. would discover that division by zero is imposs.] Perhaps the best way to put this info to TM would be by "hint" or

(Some kind of "Telling". Another way: use  $\frac{3}{4} = .75$  but  $\frac{3}{0} = 1$ ,  $\frac{4}{0} = 1$   
or  $\frac{3}{0} = 3$ ,  $\frac{4}{0} = 4$  etc. OR  $\frac{3}{0} = 1$  (most poss. float).  $-\frac{3}{0} =$  most neg. poss. float.

Another way: T. special nos,  $\phi, 1, \pi, e, 2, 3, -1, -2, -3$ , have special properties. Another  
Lena's  
Hypothesis

One nice heuristic that <sup>Lena's</sup> ~~great~~ <sup>useful</sup>: When a new object type was discovered/invited,

AM would investigate its properties in a systematic way: There was a certain ~~from~~ set of "slots" & it would fill each of them (to varying degrees).

But Back to 276.25 "in English": Perhaps stay in English more: Not too much formalizn. at this pt. Yet! The "details of formalizn." of 277.29, 32 are 4 p.!

T. hour 276.26-27 can also be in Eng., As a separate problem, we might ask how TM acquired that info.

So do 276.25 w. at least 2 hours! ① T. operators mapping 2 nos. into a no.

② The similarities of the structures of  $3+7, 3 \times 7$ , and A of ~~to~~ add  $3, 7$ ; Mult  $3; 7 \dots$

The general idea of ANL (recursive interpretation of expressions) would be ~~very~~ easiest in a recursive lang. a/c one having a stack.

A Main line of r'sch: That we may want to concentrate on "ordering of args."

So, in English, figure out rules for ordering args, then ~~find~~ <sup>find</sup> way to assign pc to these things.

These 2 operations may interact, but see if it's poss. to do. 20.

So: we start "knowing" T. function needed will be a combn. of t.

4 binary alg. funcs is perhaps <sup>other</sup> other functions. Since final func. must <sup>have</sup> numeric output,

the reasoning about "Types" (numeric v.s. Symbolic) can be easily formalized via "Type language/algebra."

The 4 out binary arith operations are all t. same w/ types on  $\mathbb{I}/\mathbb{O}$ . — So this is a big

simplifn. of t. problem. For complexity level of 1 ~~the~~ functions, there are only 4 poss. type mpps.  $m_1, n_1 \rightarrow n_2$ : for modes 1,1; 2,2; 1,2; 2,1:

[Also, there is t. poss. of <sup>2</sup> functions w. no input ② Unary funcs of m puts

The only unary funcs we have are  $x$  (Identity),  $x+x$ ;  $x-x$ ;  $x^2$ ;  $\frac{1}{x}$   $\leftarrow$  unless  $x=0$

Also "unary" funcs:  $x+2$ ;  $x-2$ ;  $x \cdot 2$ ;  $x \div 2$ . — So sort of, 2 funcs, but 2 can have diffrt exp. in  $x \div 2, x \cdot 2$ .

Re: 30-31 drop it for a while; Just concentrate on t. 4 arith operations & this particular

"Type" heuristic. One trouble is that TM has had no previous experience w.

function generation, so it couldn't have done this hour. 281.06

that hour just now, because t. problem is so simple. In fact, Much (or all) of TM's early lang. will be w.o. hours. It will use "range" EB's for solving these early probs,

but, in general, t. probs will be "easy". After this phase of frams, various hours can be discovered, because there is a large ext corpus of data tabase on which

to base TM's discovery of hours. (A part from OSL discovery, that needs

Oct 5, 00 Nature: 2 parts on Conc. Ling  
Learned, other Comments



.01: 278.40: only 1 or 2 cases... actually "1/2" cases)

.02 So just try to do a fair amt. of +. TSO w.o. "Heuristics". - Even if (CB) is quite by. When TM has enuf experience" I may then try adding sequences of data for TM's discovery ~~of~~ of hours; see what CIS is needed: A large CIS may be tolerable, since it could take many yrs, for t. Sci. community to discover 2 newheur.

T. "w.o. Heuristics" of .02 may be a bit extreme! take:  $x_1, \dots, x_5$  5 arguments.  $3+7=10$   
4 binary functions:  $5 \times 5$  poss. ~~with~~ input configurations for each:  
So we quickly find ~~we~~ Add  $x_1, x_3 \rightarrow x_5$  ;  $add x_3, x_1 \rightarrow x_5$ .  
We get  $+, -, \times, \div$  in pairs may: now w.  $x_1, op, x_2 \rightarrow x_5$  when we use random ~~operator~~  $op_i = \text{random}(+ - \times \div)$  we still get good corpus compression, but not "perfect" (whatever that means!) .19

[SN] In "Batch Mode", TM might develop "Curiosity": various other behaviors patterns, ~~but~~ <sup>appropriate</sup> "Creative Scientist" rather than a "Pure Engineer".  
How Piz works: TM finds that "experiments", "investigations into the properties of functions" - involving "using functions" all do result in often useful abs for future problems. Hvr, unless TM has a v.g. criterion for "interestingness", i. ~~the~~ long-run yield of Piz behavior will be small.

So, t. Sci. Community (i.e. Organic Evolu) develops "Criteria for interestingness".

.19: .11 Some useful functs  $f(x_i, x_j) = T$  if  $x_i = x_j$ ; else F  
T, F is somehow used to control other functions.  
 $f(T; \alpha) = \alpha$  ;  $g(F; \alpha) = \text{undecided}$ .  
The way to do it "correctly". The exact Mechanics of how to have Piz functs (primitive or non-primitive) controlled by "Ops" is not yet clear.  
I.e. "ob-of-algebra, cereals were used."

[SN] On 250.34-40; 251.01-02; 251.20-27 I discussed just what the Bottlenecks were, after the Saarb TSO's, i.e. how I have since ~~developed~~ developed methods to deal w. these Bottlenecks. It would be well to expand (a) just what were the Saarb TSO's (b) More detail on the bottlenecks i.e. just how I would now be able to deal w. them.

First, the TSO's themselves: (1) The ~~ANC~~ ANC TSO and its w. recursive evaln. of Alg. expressions. Expressions were in Polish notation, A pushdown stack was used in the "derby lang" of the Model: We Paul may have suggested that part. (2) A TSO to learn to solve linear alg eqns i.e. thereby discover the eqnvt of the "Laws of Algebra". (3) A given (substitution i.e. "disubstitution") heuristic, used for solving linear corpus, Recn, when  $\sqrt{x}$  was added/soln of quad eqns Recn when  $\sqrt[3]{x}$  was added as primitive, soln of cubic eqns.

.01:279.40! Bottlenecks ① Difficulty of Writing TSO's ② The  $\neq$  Solns. obtained only use  
 .02 computer solns. of previous problems (no sub-trees of functions used). ③ The solns.  
 didn't scale well - b.c. TSO continued, & no. of concs in many fully, so ~~the~~  
 f.p.c of the concs  $\propto n^k$  it became more & more difficult (more cc) to solve  
 problems. Problems w/ "soln depth" of  $k$  required  $cc \sim n^k$ . In human prob

.04 Solving,  $cc \sim$  constant or a slowly  $\uparrow$  funct of  $n$  - more like  $\beta^n$ , where  $\beta$  is about indep  $n$ ,  $\rightarrow$  .34  
 $\rightarrow$  Idea of task has  $k$  params; AND/OR 2 tasks gives a new ~~task~~ task w/  $k$  params; Also try to prove any task is imposs. ... This constrains  $cc$

.08 Since Search: Several impt. developments; ① Sort of understanding of Soln. of AND/OR nets (WDA problem) ② Soln of MCT ③ Better  
 .09 understanding of TM's concs.  $\rightarrow$  281.01 ④ Some general Heuristics for solns of TSO's:

Q.B. Find  $F_n \Rightarrow A_n = F_n(Q_n)$ , then (Unity Integrator)  $F_n$  intot. previous soln upto  $n-1$ .  
 This test was done using Ob-Op algebras  $\hat{=}$  observing "correlations" b/w.  
 certain Ob outputs  $\hat{=}$  the successful use of certain Ops.

.18 Re: .01: ① Difficulty of writing TSO's: Seemed much eased by MCT - since a much  
 larger scope of "problems" could be put into the TSO. In particular, the use of  
 "Learning Definitions and vocabulary." : ~~Common~~ (Definitions are usually "Told" to a human  
 student). One effect of this is that the need to discover useful sub-trees  
 in useful functions, would be much relaxed.  $\hat{=}$  A Mixed Blessing! -  
 since we do want TM to have this skill - ~~but~~ ~~the~~ ~~time~~ ~~long~~ ~~coming~~ ~~from~~ ~~it~~  
 may ~~be~~  $\hat{=}$  [This is because the "useful sub-trees" (like  $x^2$   
 of maybe  $\sin x$ ?) would be found as "definitions"  $\hat{=}$  would  $\hat{=}$  be  $\hat{=}$  "Final Solns  
 to problems" (.01-.02)  $\uparrow$ .

.25 Also, I had the idea that I should be able to use practically  
any TSO usable by humans, - just as long as it didn't contain need for  
 R+W. Specific info: (That I might be able to insert such info into TM,  
 or modify TSO solns not needed, so: use TSO from Human

Text Books. ② Re: Subtree discovery: see (.18-.25) But also it may be  
 that the TSO's I was giving, simply didn't have the complexity of concs, such  
 that subtree discovery was needed. { That it would seem that in solving  
 .34  $\rightarrow$  Subtree discovery would be useful! } ③ on "Scaling" (see .02-.06): The  $\beta^k$   
 is obtained by finding suitable heurs, for each conc., so TM "looks at the situation"  
 $\hat{=}$  this suggests certain concs should be used; Reuse  $\hat{=}$  the p.c's of these concs enormously!  
 Also, see 2-77.32 for a possl. way (Demons) to realize heurs of this kind: Also  
 way to discover them.  $\rightarrow$  (see 283.32)



01: 28.40: **(4)** TM<sub>2</sub>'s Gore; (280.08-.09) Main breaker: that Much of TM<sub>2</sub>'s Gore must be "USA supplied" e.g. t. Horizon's perhaps t. reqd of TM<sub>2</sub> cc to TM<sub>1</sub> cc (no perhaps this is part of t. "Horizon"). "Values" like relative cc to spend on "Cancer cure," v.s. "Theory of Every Pump," must be USR supplied.

deficiencies?

→ could I then just take the Soarb ANL system & modify it to fix its deficiencies?

06: 28.34: ~~Re: this objection~~ that TM has no history at this initial pts. so don't have "rnd hours": I should be able to "bend the rules" a bit; to enable hours at this point. I want to understand this heuristic (loop/insertion) as soon as possl.

Well, overpass T. (say for just lny. & a lny operator notations is quite simple — no more near universal. It only has num, num → num functions! It has no Boolean tests, no way to implement recognition of strings, etc.

I was thinking of a simple functional language w. definitions implemented via PC's "precursor" notation. It assigns PC's to codes of the codes in perhaps a better way than simple T-mcs would — since it automatically forms over many codes to get PC's. At present, I can start w. any set of Basis functions, & it can generate all compositions of them, & make definitions & uses definitions of any function create. Now it can't yet, do loops or recursion.

One way to introduce loops ~~and~~ w/o recursion, was my use of functionals. I think I can do both loops & (simple) recursion using functionals. I have written about how to do

loops recently, using this ~~same~~ formalism:

```

z = 3
for z = 1 to n
  z = (z+3)(z-3)
next.

```

The inputs to the loop are "3", n, (z+3)(z-3)   
 ~~real~~ Integer function ~~(real)~~   
 (real → real)

The output is real no ("z"); I. input is (z<sub>0</sub> (= "3")), n, f (real) → real;

```

z = x0, y = y0
for z = n0 to n1.
  y = f1(x, y); x = f2(x, y)
next.

```

input, x<sub>0</sub>, y<sub>0</sub> ~~real~~ ; n<sub>0</sub>, n<sub>1</sub> ; integers   
 f<sub>1</sub> f<sub>2</sub>   
 f<sub>1</sub>: real, real → real; f<sub>2</sub>: real, real → real   
 output, x, y real; y real;

11.64  
13.27  
4.23  
(3.27)<sup>11</sup> = 11.64

32 (L) ~~F(0) = a~~   
 for ~~z = 1 to n~~ z = 1 to n   
 ~~f(z) = G(f(z-1))~~   
 next.

← This is beginning to look like the loop form of a recursion! (R)   
 ~~F recursion!~~ (1) f(0) = a   
 (2) f(n) = G(f(n-1))   
 Defines f(n) for ~~n~~ A integer ≥ 0.   
 Which is also done by

So (32L), f. loop form is equiv to (32R), f. loop form, but is of lower cc (usually)   
 but, (32L) seems to have a more complex defn. I think Prad in fact it does not,

282.01

Bilg.

ABCde ABCDE  
ABCde ABCDE

.D: 281.40: In Part 1982 Lanet Paper (why AM seemed to work), he gave an example of recursive defn of "2 strings being of = length." Could I ~~simply~~ just ~~turn~~ into a loop? Perhaps it is poss. (even easy!) for "simple" recursions (is this form. rec. functs?).

.07  It looks like I could <sup>use</sup> ~~use~~ Z14 "recursive" formalism to define loops & recursive functions, in terms of constants & previously defined functions, and get suitable ops for the functions defined. (35)

.06 So what I need now, is some more primitive functs. to enable TM to ~~recognize~~ recognize conditions (ops) & control functions OPS.

What I want, is a nice way for Boolean ops to control numeric ops.

A poss way:  $F(True, f(x)) = f(x)$ ,  $F(False, f(x)) = \text{undefined}$ .

I don't like this because it could lead to inconsistent ~~expressions~~ expressions.

or  $F(T, f(x)) = f(x)$   $F(F, f(x)) = \emptyset$ .

we want a funct to be  $F(x)$  if  $\alpha = T$ , but  $G(x)$  if  $\alpha = F$ .

so  $S(x) = F(\alpha, f(x)) + f(\Gamma\alpha, G(x))$ .

We would define a new funct:  $S(F(x), G(x), \alpha)$  <sup>real</sup>  $\downarrow$  <sup>Boolean</sup>  
Analogous functs can be defined if  $(F \rightarrow \text{Boolean})$  or  $(\text{Boolean} \rightarrow \text{real})$  or  $(\text{real} \rightarrow \text{Boolean})$ .

Functs of this sort would be used (I think) to map  $3+5$  into  $\text{add}(3,5)$ .

& recognize "+"  $\rightarrow$  "add".

Maybe Types of vars: real, integer, Boolean, string.

Note! Recursive functs are normally defined for integers only. The expansion to reals

can be done by say  $\text{sin}'(x, n) = [n \cdot \text{sin}(x)]$  so we can get arbitrarily close approxms to  $\text{sin}(x)$ .

This is not, tho, the way I had recently been considering defns of real recursive functs. The usual  $X!$  is an example of a recursive funct

is Oh,  as long as it is clear that  $x$  must be an integer in this type of defn.

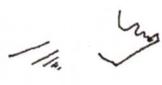
It could be used to define  $X!$  for all reals if one ~~defines~~ <sup>all</sup> gave values on

Say  $(0, 1)$  as a boundary cond. — But in the case of  $X!$  this would be difficult!

.35: (06) Anyway, This Z14 technique is fairly general, so I could end up w. a universal density function on all finitely describable functions. "Universal" in the sense that every describable function has  $pc > 0$ .

This is not yet <sup>at</sup> ~~close~~ to the universality of the Universal PC's assoc. w. UMS. UM's 283.01

Abcd.



01: 282.40! Each <sup>integer</sup> finite string (usually, if not always), defines a function: Usually many integers will define the same function.

**SN** T. funct. is defined by a sequence of integers. The upper bound of each <sup>int.</sup> sequence is uniquely determined by the integers that occurred before it.

Can I somehow map all <sup>(one)</sup> integers into functions? Well, yes: Since I have a p.d. on functions, I can assign integer code words to them, using that form a prefix set.

But, since  $\sum p_i < 1$ , all integers without ~~proper~~ strings will not necessarily represent strings of functions.

Anyway, I guess f. Q is: Given a finitely <sup>probably</sup> decidable density function on all

finite decidable functions, will the density function on functions of 282.35

be multiplicatively "Majorized" ( $>$  it for all functions (within const. factor))?

Since each funct. is represented by a finite set of finite strings,

then the universal p.d. on finite strings (the "discrete" d.f.) will induce a universal d.f. of functions. (maybe!) **10** Is where I have been before in discussing

Universality. (269.01 ff)

5:5 → 7

**SN** It looks like, recently, I have been "flaying my arms about," w.o. good direction: Perhaps go over where I am, what has been done & what needs to be done! Perhaps look at previous reviews of this Q.

1.5%  
28104  
3150

**SN** In QATM, the certain sets of QAs are in undecid. sets (Bess), the "Sequencality" the "what comes before what" in a T.S.Q. is of vital importance. It may be well to think of (Sequencal)

any T.S.Q. as being essentially a T.S. problem! (Except for "Baten mode" thing)

On the other hand, it would seem easy to write T.S.Q.'s for TM! If I know the concs needed & their hierarchical structure (the "concept net"), I should be able to make up examples, & TM should not have much trouble learning it.

Concs, ~~using~~ using Languages like 282.35. The main problem (perhaps) is to have adequate hints, so we can "scale up". ~~It is~~

In general, a Hint must be added not to narrow down the choices too so that info needed for choices does not ↑ (much, if at all) as concs ↑. (is 277.32 adequate?) [See 280.02-.06; 280.34-.40.]

I think in my sol's analysis of T.S.Q.'s in "Conc nets", I did not take the "scaling" problem. i.e. I that that a "conc net" when obtained, would be easy to

insure TM could derive the needed concs. **NO SO!** It hours of .32 are needed,

if the CDS is to be kept below some upper Bnd/ ~~is~~ as required in .32.

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01:283.40: So, it would seem that what I should do is devise a conc. net for + set of  
probs I want to solve, then find heurs that suitably reduce +, CJS's.

If necy, any conc. should be learnable by TM thru induction. Perhaps, for practice  
see if I can do this for arby concs.

T. simplest kind of conc. is first defined in "Computational Ling Theory" (Valiant et al.)

Some examples: ① an example of <sup>correct</sup> addition:  $3+7=10$ ; T. "example of addition"  
is the conc. very examples:  $7$ ;  $7+$  (meaningless);  $3+7=2$ ;  $3 \times 7=21$

Perhaps learn "addition" example such "correct addition" example

My mind is rather vague or f. forgg. concs. — just what I want them to be just how  
they are to be combined, used. "correct" : "addition" could be a combination

concs.

**SN** Suppose I simply took <sup>certain</sup> English words that referred to concepts, i.  
Gave TM examples of them. This kind of info, would later be  
of use to TM in Ling to understand English text.

**SN** A (perhaps Novel) approach to TSC Design: List problem types I  
want TM to solve. Give exgs./funcs./things that solve them: Give several  
alternative solns when poss./relevant. The funcs. are closer to a conc.  
net than d. problems. (I.e., for humans, the English (vague) descrs of the problems  
have vital heuristic associations.

So, perhaps in Line w. Lehat's AM <sup>is Eurisco</sup> Each conc. will have various slots!  
Some will relate to exgs, funcs: Ppms: Recursive, non-recursive forms, ~~etc.~~

But also Associational Base [Lehat said that humans found this more useful,  
(usually) for devising heurs, rather than ppms] — This would include "name"  
<sup>seems very reasonable:</sup>

of + conc. (In English — mnemonic, meaningful for human debugging & following operators  
of TM). When conc. <sup>was</sup> devcd/introduced, T. Context of the conc. <sup>where it occurs:  
what kind of prob  
it occurs in</sup>

Also, the "subject area" (Algebra, Chemistry, etc) <sup>specialization of conc.</sup>  
We may devise a "Special Language" for TM to deal w. the Assoc  
slots "into".

In 24 "Soln" can mean several things! 3 most imp't, are!

- ① Single number
- ② ~~Expression~~, giving "1" as function problem devcd
- ③ Proc Trace 285.01

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ABCdefg  $\int_{-\infty}^{\infty} e^{-x^2} dx$   
ABCDE

\*③ "TRACE" of the soln(s).

For very simple probs (is some not so simple), T. Trace is r. same as  
f. function (soln.) definition: It is a pgn (or equiv.) that defines f. function.  
In other cases, f. trace will be a sequence of steps that result in f. soln. final soln. As a simple  
example, f. final function might be very simple because of cancellations, or substitution  
of a ~~very~~ very simple expression for a complex one. T. trace shows these cancellations & substitutions  
being done; T. "final soln." does not.

One (sometimes) easy way to teach, is to give an example of working of a specific  
problem (This was the usual way they used to debug genl. solns in the very old days of Math.)

Anyway; TM must then generalize this specific soln. so it is able to work similar problems.  
e.g. show how to solve linear eqns: 2 linear eqns in 2 unk, 3 linear in 3 unks...  
Prove can TM generalize to N eqns in N unks. <N eqns in N unks.>

So: Try out 284.22 ff: Some possible elements of the T.S. Q,

3+4 = [?] problem? Soln, sum 3, 4; desired trace (at first) sum 3, 4;

This trace does not include Unsuccessful trials. It's not sure if this will always

be true! An unsuccessful trial can have impl in the trail leads to correct soln.

- If one has Suitable Hours. Otherwise, not which is Case in .21

Next set of probs. (or sayk prob. w. long Random real): 3\*4 = ?

First soln is mul 3, 4. This compresses to corpus of 3+4 = 7, 3\*4 = 12,

where "3" & "4" are long random nos. If the random nos. are long Enuf, we

can compress further. (w.o. this further compression, we get ~ 50%  
compression). If further compression is ~ 100% (length of random nos. ↑,

(corresponds to SSZ if we have > 1 example but many small  
random nos. - log prob 1 big random no. is equiv. to sum of long list of

many small random nos) → 286.16

In fact we can use .29 ff for MTM to figure out when  
it was solved many (if not all?) Math problems!

→ 286.16

286.01

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01:285.40 Say TM knows what patterns in problems are "random nos." (corresponding to ~~known~~ general real variables.). As lengths of reals  $\rightarrow \infty$ , compression should  $\rightarrow 100\%$ , or for given length  $L$  of random vars, Length of Code of Corpus should be  $Konstant + f(L)$ , where  $\lim_{L \rightarrow \infty} \frac{f(L)}{L} = 0$   
 $f(L)$  could be a constant (or perhaps  $\ln(L)$ )  
 (Hr, in Mem, 0, 1, & neg integers, positive integers, can be exceptions that won't not be caught by random nos. The most common exception (by far) is division by zero (and associated exceptions.)

16: 285.35 (Dropping 285.36 for moment); to continue 285.35;

We need to distinguish betw. "+" & "\*". "In English";  $+ \rightarrow$  sum;  $* \rightarrow$  mul.  
 But we have to find  $+ \& *$ ; Then decide on a functional formalism  $\in$  (Op, Op & algebra?). (The "finding"  $* +$  occurs when  $3+7=?$  also has to be found.

So: 2 problems: 1) Deciding where to nos & symbols (= strings) are.  
 2) Deciding in Formalism for functional formalism  $+ \rightarrow$  sum, etc.

Actually, I don't have to decide at this pt. I have a good idea as to how much "Info" is involved, & that's all I need.

I can make a (recursive) decision at this pt.

When problem  $3+7=?$  comes in: There are 5 positions.

The poss. inputs to "sum" are  $3, +, 7, =, ?$ : Only  $3, 2, 7$  are defined —

"sum" immediately rejects  $+, =, ?$  w/o computing output. This saves a lot of CC, because sum,  $3, =$ , say, doesn't have to be compared w. 10.

In fact, for sum,  $=, 3$ ; we don't even try 3 before rejecting when  $=$  is put into "sum" operator(??)

Next, How do we recognize "+" & use it to "execute" sum?

3+7=?

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01:286.40: Well, try ~~XXXXXX~~ Identity function:  $id(\alpha, \beta)$ :  $\alpha, \beta$  can be strings or numbers; output is T or F. (Boole).

We also need way for Boolean variables to control numeric variables:

One suggestion was  $cn(\alpha, n) = n$  if  $\alpha = T$ ,  $= 0$  if  $\alpha = F$ .  
*(cn: Boolean, n: numeric)*

So to choose \*  $\rightarrow$  sum, \*  $\rightarrow$  mul.

0.06  $sum(cn(id(\alpha, +), sum(n_1, n_2)), cn(id(\alpha, *), mul(n_1, n_2)))$   
A rather complex expression! But much symmetry.

Estimate cost:  $R_{cn} \cdot R_{id} \cdot \frac{1}{5} \cdot \frac{1}{5} \cdot R_{sum} \cdot \frac{1}{2} \cdot \frac{1}{2} \cdot R_{mul}$

5.5.2.2 is 100 already! The symmetry will be temporary to evaluate!  
So we have just ~~sum, sub, mul, div, cn, id, sum~~  $\rightarrow$  same  $f_a(x) = x$ .

? functions. So  $R_{cn} = R_{id} \Rightarrow R_{sum} = ?$  so  $7^4 \approx 2500$

2500 \* 100 = 250,000 =  $\frac{M}{4}$  already! If we didn't have  $\rightarrow$  sub & div it's only  $5^4 \cdot 10^2 = 25 \cdot 100^2 = 2500$  only.

W.o. invoking symmetry better 2 halves  $\rightarrow$  sum. A factor of 4, better.  $\frac{M}{4} = \frac{10^{12}}{16} \approx 6 \times 10^{10}$

Reachable but bad. Since id & sum are sym, we get an additional factor of  $2^4 = 16$  so  $\frac{12^{12}}{256} = 4 \times 10^9$ . Also, symmetry for mul  $\rightarrow$

we get an additional factor of  $4 \times 4$  so  $2.5 \times 10^8$ .  
I we did this ~~not way~~ "sub & div"  $\rightarrow$  in 20 & 21,

However, while these symmetries  $\uparrow$  cost they don't influence best or least, which is the real problem.

If we could implement Random choice w.o. replacement, we'd get

pc! Pseudo random trials ~~would~~ do it. Perhaps HAST coding would be more general.

Not always! This present case Appears to be a Special Case in which least  $\gg$  best. — whether it is or not, it would be, how many

C  $\rightarrow$  spend on that trial? But, when this is not relevant, we can get  $\approx$  cost to control search! So: When is it not relevant?

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.05: 287.40

While 287.20 maybe of great eventual import, I may want to return

to main track: How to implement the symmetry of the 2 halves of 287.06  
— is how to get more heuristics in, in general.

A different track! Can parts of the function of .06 have compressions  $\geq \frac{1}{2}$ ?  $\square$

.10

More reasonable! Try to implement the idea of finding which functions work  
for each problem, then "correlate" the functions w. the problem & cons.

Suppose that we had found equiv to 287.06 as solns. to many different probs.

I have indicated a Rod on 287.06 No constant invariant & constant constrained  
parts of eqs. The variables over  $\alpha, t, \text{sum}, \mu, \text{MV}, n_1, n_2$

So cost =  $50 \times 50 \times 28$   $2500 \times 28 = 70000 = 70k$

This would be the cost of using the function 287.06: we multiply by the cost  
of the function itself (which is probably high).

So at present,  $\odot$  seems like a more reasonable approach!

What we do, is first get a set of pairs:  $\begin{cases} 3+7=? \\ \text{add}(3,7) \end{cases}$ ;  $\begin{cases} 3 \times 7=? \\ \text{mul}(3,7) \end{cases}$  ect.

So this becomes a new Q.A. problem. To a human, it seems trivial, but what tools  
are needed/used? "=?" are constant! 3,7 correspond to 3,7 (low redundancy)

+  $\rightarrow$  add; \*  $\rightarrow$  mul. But how to implement this?  $\odot$  .30  $\square$

No ob of  $\frac{1}{2}$  was seen "correlates w. it of "create sum"  $\square$

.19-.26 may be an instance of a more General (heur): perhaps: "look at various  
pairs/solns: Arith, Crossover (combining) from for total final solns. Mutation (Crossover)

Should be part of normal Lsrch. They are usually "OSL" cases. "OSL" cases.

In .20 we want to find what 3 is a function of; what 7 is a function of;

what "add" is a function of. Clearly  $3 \rightarrow 3$ ;  $7 \rightarrow 7$ ; I. mapping could be made by "correlate".

Another way to look at it: "functionality" In .20  $3+7 \dots = 3 \times 7$  diff. in only 1 symbol  
ad 3,7 = mul 3,7 .. " " " "

So if functionality were to be betw. these symbols,

On "correlation"  $\begin{pmatrix} \dots \\ + \\ \dots \end{pmatrix}$  is a production of "add" w. "100%" accuracy so  $pc \approx 1$ .  
In .20, we had to test various symbols in top row for efficiency in  
producing symbols of bottom row. This is good because it works in "Grey" cases  $\rightarrow$  289.05

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05: 02840! as well as "Black & White". This "correct" is a standard term for detecting "causal/by".

06 One more reason I'm not 100% happy w. 288.20-25, .30-.40! I don't see it in a "standard form" as coming from a real or ~~hypothetical~~ TSO.

But perhaps drop objection for a while. Later, I ~~will~~ will (I hope) have experience w. Discovery of heurs, & I will then have ideas about how to better deal w. .06.

11 So! I've more or less gotten TM to do  $3 \frac{+}{\div} 4 = ?$ . T. ~~is~~ <sup>CJS's</sup> ~~is~~ <sup>is</sup> overall very small. First each  $3 \frac{+}{\div} 4 =$  is learned, individually, then 288.20 is used followed by the "correct" study of 289.35. This is all pretty much in "English" so f. details have yet to be worked out.

Next: to learn evaln. of arby alg. expressn. Best have all notations in Polish. This is simplest. Later, a prob. for TM will be with ~~from~~ betw. Polish  $\leftrightarrow$  rev. Polish  $\leftrightarrow$  infix  $\leftrightarrow$  Polish w. ~~from~~, etc. Polish

Perhaps a fundamental operation for TM, is substitution of expression for a variable or ind. operation  $expression \rightarrow expression$  or  $expression \rightarrow variable$ . Another possib., is use of push-down stack.

$+ (3, 4) \rightarrow sum(3, 4)$  ~~it knows~~ it knows : to get ~~stack~~  $\frac{3}{7}$   
 $+ 3, * 8, 9 \rightarrow sum(3, mul(8, 9))$ . This is not very interesting! TM just does  
"  $\rightarrow sum$ , "  $\rightarrow mul$ , a fc. ~~The stack is not explicitly used.~~

perhaps have TM Inn infix  $\rightarrow$  Polish  
Just try this out! See if any interesting things are found. [Perhaps try Polish  $\leftrightarrow$  reverse Polish.]

If may be easier, more "consistent".

~~3, 4, + Polish~~ ~~sum, 3, 4 Polish~~  $3, 4, +$  Polish /  $sum, 3, 4$  Polish |  $3 * +, 4$  infix /  $sum, 3, 4$  Polish

In general, the ease of discovery of anything will depend critically on the notation.

Also, I could try parens w. Polish & r. Polish. : Any of these variations don't make much difference in learning  $+ - * \div$  ~~individually~~ individually. See if look for differences (if any) in more complicated combinations of  $+ - * \div$

137 Don't pol, rpol. T. problem now is evaln. of arby alg. expressn. [with r. pol (= rev. Polish)  $\rightarrow$  Polish notation]  
 $3, 4, +$  Rpol |  $3, 4, +, 7$  mul \*  
 $sum, 3, 4$  pol. |  $mul, sum, 3, 4, 7$ .  
write out some poss. final solns) But I'd like: see if I can add TM to it (Thom)

A desirable soln: replace  $3, 4, +$  by  $(3+4)$  obtaining  $7, 7 * , \div$  evaluate this.  
perhaps a recursive program! I  $3, 4, \frac{+}{\div}$  occurs, rewrite expressn w. its evaln. Representations  $\rightarrow$  290.0)

0.1: 289.40 no longer poss. If result is number that's the result.  
The idea of "rewriting" is of "Recursion" could be primitive or heavily hinted  
concs (heavily hinted means taught w. many big hints — like examples of word problems,

SN Use of example traces of solns. might be an easier way to do early training  
than giving simply probs & solns. I may use a mixture: Use the "Trace" example  
only for probs too hard for TM to learn other way.

Actually, 289.37 isn't such an unlikely thing to try. Say TM knows about substitution  
(& Rewriting). This substitution always ↓ no. of elements by 2, so it does "move toward a  
soln."

289.37 works for any of 3 lang. x/cn problems! — It x fms prob. into a new prob. that  
seems simpler than original! The "OR" net. — which I considered to be a major  
"primitive" planning heuristic. → So This Looks Pretty Good! It is in English — so  
its still quite flexible

1.15 Int "OR" plan "Any way I can simplify the problem?" Well, in the past, substitutions  
taken (in form of evalns) always ↓ T. length of an expression — (One possl. "GPS"  
measure of vector hill ht.), so its a good thing to try. → See 1.35 for **OBJECTION!**

SN T. routine of 289.37 is not really "recursion". It is more like a "Do loop  
w. the "UNTIL" or "while". As such, it has less cc than "normal recursion". Most simple  
recursions can be easily represented as loops of this sort, & the acc pc of dcrn is  
identical to that of recursion, because it has the same defining "parameters".

2.24 SN Solving Eqs of all kinds by progressive "simplify" (1.15) is a commonly  
used technique. The use of an invariable substitution is a "special case"  
(as m. such. of linear → quadratic → cubic ← possibly quartic & possibly  
quintic, since in all cases, one adds a new kind of function that enables  
y. soln. to be found (for linear quad cubic, its linear inversion  
 $\sqrt{x} \approx \sqrt[3]{x}$ ; for quartic & quintic, I don't know yet — perhaps look  
at soln. of quintic (.)

Substitution (or perhaps inversion of substitution) should be primitive in  
the language or very easily defined from primitives.

I want to estimate pc of pc of pc "soln" of .37; Also estimate its cc,  
since I need to know  $\frac{pc}{cc}$  (or  $\frac{cc}{pc} \approx c/s$ )

3.35 Using the "OR" hour of (1.15) **Whoops!** in (1.15), TM doesn't yet know what  
"doing a left substitution leaves the value of the expression invariant." ← These are all concepts  
foreign to TM at this point. Would it be feasible to teach TM these ideas  
before having it approx acquire the hour of (1.15)?

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06:290.40: I m. to teach TM

About equality: TM is invariant under equal substitutions & other unary, binary, etc. x fms: e.g. if  $a=b$  then  $f(a)=f(b)$  for any  $f, a, b$ .

Maybe not exactly true if  $F$  is floating pt. function! Tho, TM works probabilisticly;

These relations are usually true infra (so 99% accuracy); later TM will try to find how to get closer to 100% accuracy by looking at error cases:

Perhaps it could ln about the "division by zero anomaly" this way!

First teach what equality "is": Examples, pos & neg.

**SN** pos & neg examples: There are usually far fewer models that need be considered

if neg. as well as positive examples are included ... ~~But still~~ One can have

very A.M. models (w + & - cases) but v. A.M. models look very A.M. - They have very small pc.

so  $3=3$   $3=4$  (no):  $3+4=7$  ← This is rather complex! TM has to find

the sum operator in its internal lang. An imp't Q, perhaps is "In what order to introduce concs to TM?"

perhaps first teach "identity", then equality. Identity is a relation betw. strings & strings or nos. & nos.

so: Is  $3+7$  a string or a no.? In Lisp, maybe, it's a list. Its evaln is a number. So maybe identity should relate strings to strings only.

$3+7$  is not "identical" to 10 bc "3+7" is not "10" because evaln. is implied and "equals".

"identity" can be a primitive conc (string  $\alpha$ ) = (string  $\beta$ ) means (evaln of  $\alpha$ ) = (evaln of  $\beta$ )

I may want equality of 2 nos  $x=y$  to be primitive: it ~~is~~ is tested by ~~it~~.

evaluating  $x-y$ : if result is zero, then  $x=y$ . TM will ln that if  $x=y$  then  $y=x$ .

TM will ln. to evaluate the function Solve ( ) :

.35 e.g. Solve (X,  $X+3$ ) = -3

.36 eval (  $\frac{3+7}{\text{string}}$  ) = 10

01:29:40! The present approach seems v.g. perhaps review recent work! Have I been "driftly about?"

Superficially, the OR plan of 29:15 is an English dem. of how to solve a problem; Trouble is, it does seem to use several conce. that seem distant from "primitives".

So it suggests 29:06 ff <sup>i.e.</sup> ~~start~~ TO teach TM what "equality" means:

SN This somehow seems closely related to teaching TM what "quantity" meant - But seems more "exact"!

29:06 ff is beginning to sound like LISP! Distinction betw. strings & evaln. of strings, etc. Perhaps all of y. concerns that I had about what ~~it~~ meant

by various expressions: (e.g. distinguishing betw. archn of a string & t-string itself) 18 would be automatically taken care of by LISP.

T. slowness of LISP can be taken care of in various ways!

- 1) LISP → Fortran 2) People in Genetic Prgms translated some Kozo's LISP stuff into Machine lang. & a/o CC, etc.

Perhaps have TM run LISP (as a TSOQ!); Another possy is to run MAPLE.

18:00 Another thing I was Confused about, that LISP deals w. in a possibly o.k. way: T. idea of Binding temporarity: An assignment statement is only true, until t. next modifn. of t. Variable.

Also, t. idea of Local v.s. Global variables: In Basic, we use local variables in FUNCS. All other variables are global.

Also: I have a file on "Functional Languages": It includes a long review Art. on functional langs

SN A poss. way to deal w. large (or oo) CC of facts in GA. Use of L such: i.e. For each GA run, select best have a k value, & truncate a trail as soon as CC.PC > k. For t. next GA run, do k ← 2k.. Pick some reasonable value of k to start t. Series of "GA runs".

30 SN On t. possy that t.  $\geq 141$  d.f. of  $Rec(\mathbb{Z})$  LISP functions, is a universal d.f. on all functions. To show this: Consider these functions:

$F_1$  maps integers into LISP functions: it is able to map all poss. functs from integers.

$F_2$  maps integers into integers (essentially what a UMC does); this gives Discrete (counting) universal D.F.

$F_1(F_2(\text{integer}))$  maps integers into functs w/ universal D.F. on functs.

$F_1 F_2$  is a function realizable by LISP - it has  $\geq \phi PC$ . (finite cost).

So if we give LISP random inputs, ~~this~~ <sup>this D.F.</sup> will "Morozize" ~~the~~  $F_1 F_2$  Discrete (counting) universal D.F.

34 functions - so if, too, will be a universal D.F. on functions.

Q: Is this a non-trivial result?





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1. Main goal of TM is "compression". Ideally, this also makes the future work of compression easier. One part that would make it easier is if "significant" (significant) lower codes are included. These are codes one would normally "back track to" (not significantly)

Theory Revision:

Would "indexing" of corpus be of use here? Perhaps list all things one wants to do to make future tasks of future, easier.

- At least 4 kinds of future tasks:
- 1 Augmentation of Corpus - we have to add new stuff. Production of future's perhaps best way to do this (also see 4)
  - 2 Modifi. of tasks/goals of system ("S.M. Maintenance"). If system is maximally modularized (so each part of system must also have alternative S.W. codes ... (ways of doing it)), this makes Modifi. easier.
  - 3 System should have many "adjustable params" to deal in changes of appln. of system.
  - 4 Theory Revision : when to produ. system of 1 no longer seems to work adequately.

Marcus:



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This is a reply to Marcus Hether (and partly to part of Jürgen Schuitshuber's "Lazy way to run").

Consider the problem to be RTM, w.  $h$  not specified but CB specified. Each ~~run~~ "trial" by TM is somewhat expensive, <sup>by t. cost.</sup>  $\rightarrow$  cost of the response will, in general, be computed differently from TM's internal compn.

At first approx, consider RTM w.  $h=1$ . This is a non-zero "straight OZ problem". For  $h=2$  the problem is to make 2 trials  $\exists$  the best of 2 is max. This allows "experiments" (which  $h=1$  does not allow). (I think Jürgen was concerned w.  $h=1$ , only). <sup>"horizon" = no officials to be used.</sup>

If TM has intelligence  $\geq$  that of user, this can be a very dangerous activity! TM will try to manipulate the user in getting it a high score.

For  $h > 1$ , I think the problem may be a "Dynamic Programming" problem. There are also aspects of the (unsolved)  $G = G(t, x)$  problem, in which  $G$  decreases w. delay.



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Int. Problem of 1.18-30 At each point in the process, we have a sequence of paintings, Goodness  $f_n$ :  $[p_n, G_n]_{i=1}^n$ .

09 → We could regard it as a simple 0-1 problem, we want a painting  $p_n \rightarrow G_n$  is max, & we want to find it time T.

12 We would <sup>have to</sup> use a rather sophisticated OT if we wanted anything of much value in a reasonable time. → (Note 4.12!). An OT is any thing that gives discovery strategy.

The Method 1.18-30 is perhaps a greedy method, in which each choice of painting to present, is the "Best poss. that TM can do at that time."

More General (Less Greedy) OT's allow for "Experiments".

By allowing the most General kind of OT's (those decidable to a TM) we get the best possible soln by LSuch.

20 So .09-.12 really is a "Theoretical adaptive" soln of the problem!

I was thinking the "Cure Cancer" (research direction) problem, was close to the "Paint on account of a good painting" problem.

In the painting problem, feedback for each "Trial" is a scalar.

24 (It could be more info, like LSuch a more detailed discn. by the "Patron" of just why he liked/disliked the particular "Trial".)

25 Anyway, in "Cure Cancer" the feedback is in a very general form.

26 Superficially, if we generalize the idea of OT, it could deal w. any form of feedback; so it could deal w. the feedback of .24-.25 and even the very general type of A.B. in 126.

Finding a Good OT of this more general kind is the same kind of problem (w. what looks like an identical type of soln) as my older, simpler OT's w. only scalar F.B.

33 Furthermore GPS w. a vector score, could be implemented by any more general OT.

My impression of the OT's used in "LSuch": That one would best use only 1 OT — even! Using > 1 OT means loss of info before OT's — so OT's can't use into the better OT's have requested — They may even duplicate trials

i) Most soln probs are solved by 0-1 OT. The invention of a good FF for a INU prob. to convert it to a 0-1 prob. is a skill that TM would acquire early.



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.06:2.40 Made by other OT's.

If trials are very Expensive, they would be very inefficient!

Solving the "Most promising" OT Thus far considered by TM could be quite good — if the OT selection was like I envisioned it in MCT.

In MCT, we have this "Grand P.D." that looks at a problem (i.e. "conditions") & outputs a p.d. on all poss. soln. trials. In the old style, if the input were a QZ problem,

.12 it would output a p.d. on all OT's w.r.t. that problem — A possibility is that as TM

.13 matured, it would end up w. almost all w.t. in one P.D. — seems likely!

[ I was concerned that in the "Cure Cancer" problem of 2.20, the results of experiments would be "prohibitive" — But in fact, all results of any nature are "prohibitive" as far as TM is concerned! ]

SN It would be well to integrate logical/mathematical reasoning into "Lsrch" or

x MCT — since much development of OT's involves reasoning of this sort.

I did write some about this in  $\Sigma$  last 6 mo. ... try to find it!

But do go into the "Cure Cancer" problem in some more detail! I think I did Not

Solve it, last time around.

→ SN perhaps the idea on non-Lsrch ~~is~~ suggested by .12-.13 would be the best way to deal w. the G = G(x,T) type of QZ problem!

→ SN for "Any Time" problems, use Levin's Time-shared version of Lsrch for QZ probs

In General, if G(-) is expensive, Assumed Normal Lsrch may be rather poor.

In "Cure Cancer" prob is a QZ prob w. expensive Grc! ① C of Grc may be large & ~~is~~ constant & known by TM. ② C of G may be known in advance for each trial — by a formula f(x) <sup>(problem)</sup> ~~is~~ given to TM. ③ ~~is~~ C of Grc is only known by TM as its own indexed p.d. from previous observation of G, cc pairs.

→ This last seems close to the "Chess" problem. In Classic ALP, one can't even get a d.f. for the cc of a trial — but in Resource Bounded ALP, one might  $\frac{1}{2}$  legitimately make an approx. guess.

If "Cure Cancer" is an  $\approx$  INV problem, (so one knows when it's been done — or a certain threshold of goodness of soln is assumed) then the ideas of the first Gambling house form are relevant — one wants to minimize E of  $\Sigma$  cc for soln. is found.



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06:30: In General, t.

Methods of MCT can be used. w.o. using Lsearch. Tho, in many cases, Lsearch

is an OPTIMUM.

W.R.T. OZ problems, Lsearch <sup>O.K.</sup> seems ~~fine~~ for induction problems. — a. Near sequential } Note:  
or unordered — say w. fixed corpus. Lsearch is v.p. for finding the unnormalized PC of  
a Corpus.

12

T. "Method of 2.09-12" automatically tries to "simulate" (Expensive Goro is an OZ problem:  
if it does this in a non-cl. way. } for even OZ problem, TM finds  
a P.D. over appropriate OT's!  
→ See 302.27

Normally, in induction problems, one does not use Lsearch (int. visual sense) for trying  
cond. codes. ~~But~~ (in which any trial is or is not successful)

Usually we arrange so that every trial results in an acceptable code: we do this by  
compensating amount of "correcting" that would be needed to repair a "non-code" in into  
a fitting code. More Generally, since induction is an OZ problem, TM  
recognizes it as a special kind of OZ problem (all OZ probs are "special" since t.  
don't know of the problem before running what ~~kind~~ kind(s) of OT's will be tried), and uses  
special OT's to solve it.

Hvr, there is a common type of induction problem in which we do use Lsearch:  
These are the induction problems that I had in early Algebra learning, — like ANL.

We don't use Lsearch for difficult INV probs (we usually re-formulate them as OZ  
probs, w. suitable FR ... or as GP's probs w. vector Goro (2.33), ...)

→ Yet, INV probs should be optimally solvable by Lsearch: "If all needed hours can  
be put into v. "Grand P.D."" □

→ For OZ probs, if they used Lsearch is "all hours into v. "Grand P.D."" "Then it would, indeed,  
be optimal — for some reasons for INV probs. 301.15

30

I want to look at Several hours: to what extent can they be expressed as Modifies  
of the "Grand P.D."?  
Take it, AND/OR Not "Pro" heuristic

**Remember:** In most INV probs, we're searching not for just a soln, but for a strategy  
that will solve the problem. Lsearch over near "strategies".

In the "Cure Cancer" problem: In view of past info, what is strategy w. max prob of solving problem?  
— one w. min expected CC of solving problem? ← First G.H. theorem.

→ A heuristic would be part of the decn of any strategy. This idea of a strategy is on 5.06



N.B. 18-40 should be in Bulgaria perhaps more Hutter PE 1 + Hutter, → Belg 296 + 300. Belg 295 → on Hutter.

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06:4.90! To Mm. Loast — but can it deal w. "Quick Start" → <sup>Actually Quick Start is perhaps hours limit. couldn't ATM speed by very much! The expected</sup> <sub>CS is always → CJS = CJS.</sub> <sup>hours</sup> <sub>Pej</sub> → 301.11

Re: Use of Hours: Ordinarily, only 1 or 2 will apply in a given case; so want not much of an "exponential explosion": Once a hour is chosen, it could closely guide t. soln. of the problem (not much ↓ in PE).

11 G.P.S. is ~~and~~ AND/OR planning over fairly general (hours, applicable to almost all problems. G.P.S. for ENV. problems: AND/OR rules for (I think) both or 2 ENV.

13 Another Very General Hour ~~rule~~ "Use analogy to <sup>Successful</sup> ~~substantive~~ Soln. of known problems"

Using hour in this manner ("When a problem occurs, find assoc. hours to guide soln.") Makes it sound like AM, Euricos etc ... Loast — But it certainly sounds much different in spirit from Loast! — Certainly no "Looking by Brain Surgery"!

18 SN In retrospect: One of the most important theory problems that I recently <sup>recent</sup> published. I guess by Debra: My TSO's are much less "stunning": Much longer CJS than Loast. — Also, maybe always ran into was teaching TM Definitions of various concs. My mind was very vague as to what relationship was betw. many concs. & examples of their conc.

21 I had hoped that my reading about details of "LISP" would help here. → 24

22 T. 3 Hours of .11-.13 are really quite imp't hours! Used almost always (G.P.S. & And Ornett) "Analogy" used <sup>not successful soln.</sup> may be less.

24 (21) In .18 & .21: I think my & own internal ideas of what concs. meant, were too vague: E.g. t. ideas of "quantity". — Yet vague as they may be, concs. of this sort can be very imp't. in lang! I think the problem was that I did not recognize this conc. I had in mind was really quite vague!

So, T. Q is: how do I implement this vague conc? — More Generally how are vague concs. conveyed ("implemented") to TM?

T. oral / quote notation of LISP is probably very useful for the ~~dealing~~ concs. — but still vague concs will occur, & I need mean in other form — just how to deal w. this is when to deal w. it.

Wrt. explicitly vague concs: Perhaps just give myself lots of examples & give a no. (maybe PE) giving how much the conc. is represented by each example.

Thinking vaguely is an imp't. method of invention / design.

Perhaps "Fuzzy Reasoning" is ≈ what I want.

Bulg.



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06:540

The hours like 5.11-13 ~~do seem~~ do seem expressible as mod. of t. pd. What Ray says is: This hour has a pc of .3 of success (T. hour itself will be a sequence of instructions (some of them of form  $\text{pr}(x) \leq t$ ) on how to solve the problem)  $\leftarrow$  T. hour is expressible as a mod. of t. Gpd

11:300:07: [ON Quiz About]: Perhaps it would be poss. for TM to discover t. "Quiz about" hour by "Logical Reasoning", rather than [usual methods of hour dcry]. I haven't really examined t. role of Logical reasoning in problem solving & hour invention.

15:299:30: (Lesson to ~~OT~~ OT probs... & optimality of): T. idea in OT probs is to use Lesson over e. P.D. or OT's. So, say a person (non TM) has a better way to work a particular OT problem than TM. Then a must have a reason to choose a particular good OT for that problem, & that reason must be based on past experience w/ Logical reasoning. If those reasons were understand built into TM's GPD, it should be able to get about the same results.

20 The arg. of .15-20 would seem to hold for "practically any" OT problem type: - Including those w. very expensive eval. func. So t. work pt. (if any) of .15-20 (underoptimality of Lesson for TM probs as well) is t. "Logical reasoning" part: (also in (12)). "Logical reasoning" is a special case of probabilistic reasoning - but we pc close to  $\phi$  it.

26 So f. Q is: How can TM learn to reason "Logically"?

Well, suppose we first teach TM Math & Formal Logic in a purely theoretical way, so it can solve problems but knows no relation betw. (Math & Logic) & other problems that it is given. We then give TM problems in which its math/logic knowledge is relevant, & it could find there is an "analogy" betw. math/logic solns, & t. solns. of problems,  $\beta$ .

It m. be also be poss. to teach TM Applications of math/logic along w. t. theo. understanding of math/logic. "Practical Applications" are w. t. TM's own normal problems.

Try to find a "practical problem" for TM, in which math/logic would be useful.

Wall: TM's work. - in. holly, TM is mostly Lesson, but it could be made aware of t. more general goal of min E(cc) for total soln. or for "T. horizon time".

An early approach to had to ANL did use logical reasoning! I didn't know how to do it, huh.  $\rightarrow$  305.06

Bugs



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00: on Summary Machines & Prediction.

Say One has a corpus, C, & one has <sup>found</sup> several pems that are not bad for this corpus.

Predictions can be made in 2 ways:

1) With most of the several pems.

2) Devising new pems: ~~These~~ use cons used in the "several pems", w. appropriate wts.

**"THEORY REVISION";**

Hvr., T. Mechanics of .11 is not clear: It may be that 10 is <sup>almost</sup> always used - unless it seems to not work anymore; In which case one goes to .11 in "Theory Revision" mode  $\leftarrow$  .35  
to not work anymore: In which case one goes to .11 in "Theory Revision" mode  $\leftarrow$  pilot.

.16 D3.000:  $\geq 141$  using 2 ~~com~~ computers lang. (like Lisp, say) generates a Universal P.D. on strings.

One (Apparent) by Q is: Can one generate a Universal d.f. on functions this way?  $\rightarrow$  .23

Some recent writings (within last 10 or so yr of Bug) suggest that this is not very ~~important~~ important - that what is more important is a good TSCQ. Even if the d.f. on funcs was Universal, it could assign a very small pc to the "correct" function. A good TSCQ assigns by PL to ~~the~~ known soln., even if the d.f. on funcs is not Universal. (SEE 293.16 for Bib. of refs on Universality)

.23 .16 If we had a nice way to comp strings into functions, that would do it! (Say we used funcs of single strings only). We might be able to ~~do~~ this very easily in "Lisp" by restricting to some symbols in the Alphabet that generates "Lisp expressions". (Note 293.19 on this)

.25 .16-.25 May have a very simple soln. I'll just have to think about it in more exact detail! (Say via Beg induction)

.27 Anyway: In MCT, I was thinking of 2 kinds of induction problems being "special kinds of problems" - the other 2 kinds are OZ & Env. probs. In fact, Induction probs are treated by MCT as "just another OZ problem": Th. GPD looks at the induction problem, then because it is an induction problem, it uses special OT's for it. The nature of the OT will depend further, on whether it's seq. extmpl. or uncond. Beg induction, & whether the params are continuous w/o discrete.... Also the source of the problem will help determine the OT. **OT.**

Well, "Theory Revision" may be a standard kind of OZ problem: but in induction, if OZ is poss., the OZ version of the problem becomes more complex (?)





Conc

01: (293.235-38)R : "Expressing a ~~conc~~" means that we use "before it" so it becomes a single word, w. ~~conc~~ an associated pc. This enables us to "compress" by using the Conc.

[284.22] is a simpler way to design TSC's. It's not as complete as a Conc. not, but closer to a TSC. [ See Also 303.35 ff ]

05 So, in view of (293.235 R) ff, all I need is a good TSC, a lang. adequate to express its needed Conc. "Z141" <sup>Along w. "LISP"</sup> will perhaps be adequate for obtaining pc's of concs.

So how does elaborate treatment of OZ problems in MCT fit into .05 ff?

Well: MCT is about GPD updating. How is .05 related to GPD updating? — Presumably GPD updating is just another OZ problem. Like most OZ problems, it has special techniques for doing it.

[SN] Like OZ probs, each INV prob. can have (a particularly appropriate way(s) to solve it. GPD looks at an INV prob. & gives a PD over soln techniques for that particular INV problem. I had assumed that GPD would simply give a PD for the Lsrch of ~~any~~ any INV prob. presented to it: (Probably) not so! As I noted in the post — Most INV probs are solved as OZ (or GPD) probs, not via a Lsrch.

→ It looks like I am gradually Abandoning Lsrch as a Universal Prime Problem Solving Method!

— Tho in many circumstances, it does seem to be optimum.

Also, it may be that many ostensibly non-Lsrch methods can be (usefully) expressed as modifications of the Lsrch. (Rare is, of course T. "Quick Abort" problem!)

24: 303.40 Consider all sorts of probs, at all levels: e.g. "Cure Cancer", "Devise Good method Priority for physics"; "Devise V.E. pointing from sacred set of paintings (do it for poems, music, etc.)". Make big list of interesting problems that I'd like TM to be able to solve. Chess, Checkers, (Good eval. funcs; Cheap, effective)

29 On Prob. Solving in General! First time one solves a particular kind of problem, it's pure Lsrch.  $\frac{C_i}{R}$  depends on the pc of the primitive lines used to describe soln; Only "Simple" probs (simple wrt to primitives) are practically solvable.

Next, one solves probs by "OSL" find pattern in past or ~~part~~ part of the present problem & use "soln. ~~techniques~~ techniques.

Next, when one has 2 or more examples of a problem type for it is easier to decide on pts. of similarity of the probs. & soln. so Lsrch for soln is much reduced.

If it is poss. to solve probs w/o the OSL phase: The first & second times one solves the problem it is by pure Lsrch in both cases. After the 2nd soln, one recognizes it is ~~not~~ <sup>prob. & soln.</sup> ~~not~~ <sup>of previous problem.</sup> By eliminating OSL as part of soln. method, one is probably at a very big disadvantage, but it is still

37 poss. to be TSC's & require "fly intelligence" ← (perhaps) —

In the SAARB work on TSC's, I ran into a "SCALING" problem:

Spec  
→ 306.01  
→ 305.06

Logical / Mathematize / Reasoning:

How TM can do this,  
" " " Learn to do this.



301.12

303.31

06: 301.90

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(See 303.30-31)

08 Somer areas where TM uses Math to do induction:

1) Linear Regression: we want a set of coeffs to minz.  $\sum \text{sq. error}$  — an OZ problem.

In General, each OZ prob may have its own Soln. mechanism. Consider a normal analytical OZ problem: To find  $f$ , max of  $\sin x + 3x^2$ . People kn how to do this. We could teach TM to find  $f$  extremum this way. It would first have to know diff. calculus. (which is one way: probly Archimedes could have worked it w. dif. calc!)

2) There has been much work done on Continuous optzn: Info Based Complexity: Joe Traub et al.

Also, on discrete optzn. (to some extent). TM could be "taught" all of this.

D.10.00

Buf.

01: 304.90: I put ~~all~~ solving of all problems in "Memory" w.o. indexing them, so pc of many use  
 →  $\frac{1}{N}$  (N = no. of probs solved) — A clearly non-viable method of prob. soln.  
 This might not be too bad if one accessed many once in the soln. of a  
 problem: But for 2 or 3 ~~acc.~~ many accesses, it. process becomes ~~unworkable~~ quickly of  
 too low pc.

Some simple methods of indexing: (1) Recency of occurrence (2) Source of problem  
 (Math, Physics, Chem, etc). (3) Similarity of structure of problem definition to that of previously  
 solved problem ("Analogy"). (3) is perhaps most impt.

So, Given a problem: Subproblem is: What is/are  $\nu$  previously solved  
 problems? (or previous ~~un~~ solved probs?) → To avoid unsuccessful techniques of the past.

04: 304.37: ~~On~~ Actually, how much extra trouble is OSL? ( $\nu \phi!$ ) —

w.o. OSL, when a new problem comes in, we look for "induction systems"   
 that have been obtained w. SSZ  $\geq 2$ . This does involve some searching.

An induction system is  
 a problem soln.  $\geq 2$  problems  
 common to  
 a set of n f.  
 corpus

Here, the searching is easier than in OSL, for 2 reasons: (1) There are many more  
 "solved problems" to search over than "induction systems" (perhaps not quite so!

when we ~~search~~ we normally search over  $\epsilon$  total of solved probs that have not been  
 put into induction systems + induction systems:  $\epsilon$ . Cardinality of  $P_{\nu}$  sets is  
 usually  $\ll \epsilon$ . set of all solved probs; it perhaps not ~~is~~ <sup>much</sup> larger ~~than~~  
~~set of~~ set of all "induction systems"

(2) In an induction system, the relevant features of  $\epsilon$  problems have been  
 "distilled out" (isolated) — This makes it much easier to tell if it is relevant  
 to the new problem. On the other hand, comparing an unsolved problem to a solved  
 problem — it may be difficult to decide out relevant pts. of similarity.

24

On the basis of (11-25), it is not always clear that one might save any cc  
 at all (by comparability even) by not ~~doing~~ doing OSL.

29!

Re 304.29 ff: (Can prob solving ~~be~~ <sup>be</sup> mainly by "SSZ based reasoning")

Often we will not find previous problems or "induction systems" that will solve the present  
 problem or be relevant to it. Pure search is not often the way to go.  
 We'd like (at least) to be able to ~~search~~ do search over combinations of concs  
 (larger than primitives) — But the system of 304.29 ff. only puts prob solns.

in "induction systems" in memory (i.e. "defines" (Recall). There is no mechanism  
 to obtain intermediate sized concs: (only ~~primitive~~ primitive concs & "induction systems")

One (not completely A.H.) method: Factor the "induction systems" to ~~get~~  $\uparrow$  ~~the~~  
 pc of the entire set. The "factors" are sub concs of all sizes.

This "factoring" is part of a fairly novel part of prob. solving: i.e. compression  
 to all-over-again would plus far. ~~What~~ we need do search over the parts ( $\equiv$  concs)  
 to solve problems. It may be that our ~~current~~ ~~present~~ ~~method~~ ~~using~~

307.01

01:306.90  
solns of previous problems (could) be a special case of Lersch, — so would have an integrated system

I have been considering 2 kinds of General Prob. Solving Methods:

05 T. Older Method: All probs solved by Lersch: T. Pd for each Lersch is a cond. P.D.; P. "condition" being to problem down. The unproved assumption is  
→ Prob all hours are expressible as Modulus of G. P.D. (<sup>rank</sup>G.P.D.) (It is known that "Quotient" is not included)  
A. (perhaps) associated assumption is that this particular form of th. hours can be obtained from the Data that a "Human form" hour was obtained from.  
— This "Data" includes logical reasoning.

11 T. newer method: 304.25 - 40, 306.01 - 10, 29-40: Idea is that many problems are always either solved by new Lersch or by finding probs. (or sets of probs) that they are  $\sim$  to, & using  $\sim$  soln. methods.  
T. new method seems closer to the way I solve probs, but I'm not sure about its 'completeness'. Could I do T.S.Q. from Elementary Algebra, using Proof Method?

15 D.12.00 Part of the "older" approach was to try to do T.S.Q.  $\sim$  to that of Heun's — doing, say, Elementary Algebra. How this fits into the <sup>older</sup> Model of .05, is not immediately clear! It seems to be like the newer method of 11. — Perhaps I can integrate ~~the~~ .05 & .11!

One idea is that I would do .15: that .05 would enable me to express all ~~the~~ prob soln. each way as Hours: This perhaps .11 would be a major heuristic.

A Main idea of (older).11: That whenever I (or anyone else) solves a problem, it is by putting together concs. that desc. to soln (method), so <sup>"adequate"</sup> a problem becomes to a composition of its subconcs — usually by solving simpler problems.

A (recent) idea on writing T.S.Q.'s; <sup>303.35</sup> Announce a larger set of problems, w. one or more "solns" (= method of soln = "trace"). From this, set of ones can make a conc. net & order the problems suitably.  
303.35 is 284.22 are on this =

30 Another (perhaps related idea): To write out how I solve probs on every level (of English). E.g. "How to evaluate Algebra Expressions": & Find a part that I can evaluate. Evaluate it & substitute it, obtaining a new expression. Recurse ~~until~~ to a point until I have a pure no. or until I can't find any sub expression to evaluate.

I could write a Lisp prog to do this: T. Lisp prog would be "factored" into concs. that would be irremovable from other problems.

As a hour for above; A substn. of an evaln. "Simplifies" the expression — thereby bringing it closer to goal. This would be an "Adequate" hour to solve the problem.

It is an example of an "OR" decomposition of a problem. (AND/OR nets)

Pro "Simplifying" a shorter expression is usually "Simpler", Hrr. m. b. present conc, 308.01  
309.01  
Spec

The Horizon problem: Paper unclear as to how to define <sup>final</sup> goal. Says one wants to get (max) ~~total~~ per unit time to be max over "long time". This is equiv. to max total yield for "long time". So one would to solve problems first. (always first) —  
 So one would never do ~~first~~ non-meta problems.

One way to fix it. May  $\rightarrow$  to spend say 50% on meta <sup>probs.</sup>, 50% on non-meta probs.  
 Also, it may be nice to put time scale on meta probs: how far into future is it concerned?  
 So at least 2 params needed ① i. %50% ② t. time scale.

An automatic time scale might be found in t. inability to predict nature of future problems to more than (say) 10 yrs into future. (This 10 yrs would be as ~~span of~~ life of TM  $\uparrow$  beyond met of Sci community)

So, anyway, since I will be <sup>assigning</sup> TM lots of params, I have no qualms about giving it these params. People who want their machines to be "truly autonomous" don't like this, but ~~it~~ is certainly don't want a "Truly <sup>nominal</sup> autonomous machine".

Bugs.

01:307.40 ~~getting~~ getting monotonically shorter "equivalent probs" would usually be adequate to solve the prob.

One big complaint about the SAARB ALSH soln. was that it was not the way a human would solve the problem, so it was needed to find the identical useful concepts in the soln. In 307.30 ff we are close to the way a Human could solve it. We do seem to need the concept of "evaluation" — which may be a subtly ~~of~~ ~~the~~ ~~idea~~ ~~so~~ ~~we~~ ~~can~~ ~~make~~ ~~it~~ ~~in~~ "primitive".

10 One big direction of the TSO work was to start at the beginning's work up to a very Very Smart Machine. A Perhaps Better Approach would simply work on "patches" of TMS training at various levels, then "patch" the patches together. Working on patches at various levels will give me a better idea of what the real problems of TSO design & TMS Learning Algorithms are.

It certainly isn't a new idea, but I haven't really been doing much in that direction. An extreme case of it would be to take an expert "Expert System" (such as a Symbolic integration program in Maple or Mathematica or ...) and ~~then~~ slowly convert it to a Lrng system. — Try to find out how each of its routines could have been "discovered".

16.9.90

ON MUTATIONS, <sup>(Recombination)</sup> **CROSSEVERS** :  $\geq 2$   $SSZ=1$ ,  $SSZ=2$  vers.

On mutations  $\geq 2$   $SSZ=1$  ( $L=SSZ+1=2$ ). This is fine. We can use any regy. we can think of <sup>(seem to be)</sup> appropriate to Real Domain:  $\neq 2$  a basis for generating f. mutated form of  $t$  parent.

In the case of Recomb.  $SSZ=2$ , ( $L=SSZ+1=3$ ), we aren't about f. same situations as  $SSZ=1$ ; we are much controlled by regys observed in the General Domain of  $\epsilon$ -problem. For each such domain, we must learn how best to design recomb. techniques.

For Recomb., the main idea that ALP contributes is that child should have as many <sup>common</sup> parts of parents as possl. (but having part from one parent is also good (a mutation))

As before, my impressn. is that in certain domains, a well designed mutation scheme can be much better than an inappropriate Recomb. algm.

One could evaluate a given Mut. Alg. using f. "present population". We could get its mean & var. in predicted  $G$  of child.

Similarly we could evaluate a recomb. Alg. (for 2, 3, 4 or any no. of "parents").

**A META Problem:** To devise new (Mut/Recomb) Algs. & select best ones (A GA-type problem). What influences what Mut, Recomb. to use for this "Meta problem"?

Also, the Goal for a (Mut/recomb) Alg. is not so obvious! We want an M/R algm that maximized "rate of 1 of ~~the~~ Guides".

↳ An alternative View: To get a good, cheap pd out of existant Corpus of Cands. ( $\equiv P(X, G)$ ). This is in the Direction of  $\approx$  "TM<sub>2</sub>"

Another view of it, would be that we mutate or recombine ~~parent~~  $\approx 2$  (small?) population of (Mut/recomb) algs. (eventually, this scheme might become "Recursive" so this mode of mut/rec. could also be (mut/rec)ed.

Re: Human Creativity: An experienced Scientist will solve diff. problems rapidly: his pd's for final solns are narrow, but often correct. - His searches are smart. Often, hwr. they will be not interesting solns.

The novice Scientist will have a less narrow search. ~~algm.~~ It will be much slower in finding a soln to a problem, but because of diversity of trials his solns, to problems are less ordinary, and he may solve problems unreachble by the "experienced Scientist" w/o having found <sup>useful</sup> ~~useful~~ perfect things along the way.

A very successful experienced Scientist will have a somewhat different direction of search than most. Also, if he spends lots of time, he will eventually go to strange, unusual places and find great discoveries.

Very poor Scientist's Errors: Use Excessively Elite Srch. → 186.01



8.21.00 Bulg.

16 off needs  
duration of 179 -  
Princeton, 166

Genido / 76.21  
Mesa Verde. 172.11.34

### IPC of Human!

The IPC of (i) Deep Blue, the machine that beat Human world chess champ.

Said to be ~  $10^{12}$  flops. Very vague in terms of bits/sec, hvr.

Got some idea of speed by ~~no.~~ no. of board moves/sec. ← which may vary.

How, no. of "bits" in a board move is very unclear; well from retro, I can get no. of flops in a bd. evaln.

→ Perhaps read up on just how Deep Blue actually worked

The speed of "Blue Gene" is to be  $10^{15}$  flops (or  $2 \times 10^{15}$  flops)

Check on this by other comparisons, or other estimates of speed of Blue Gene.

"Blue Gene" speed is also given as multiple of Deep Blue.

But much of this can be value in const.

What Human Computing does well Fast parallel ops (perhaps associative processing, ~  $10^{11}$  bits/sec.

(2) Fast I/O retrieval. This could be, by far, the most massive amount of computation done. The amt. of HW (dendrites) used, could be enormous.

→ This last could be imp. for OSL: to find situation in past, ~ to present problem or "relevant" to it. "Associational" memory: Perhaps done by retro-coding.

So large "Content Addressable Memry" would be a very cheap way to get what appears to be "Enormous IPC". — Hvr, at present time there is not much market for "CAM", so it (perhaps) not cheaper than what is now, the conventional way to do in parameter retrieval.

The fast opted is associative (it may be tough - the this can be slow) need not be used in a TM of great intelligence.

Latest civilian Super Computer cost/performance. \$ 45M for 6 T flops:  
\$ 7.5 mill / flop = \$ 7.5 per M flop, \$ 7.5 per G flop seems high!

An upper bound on human IPC: cost per flip in eggs is  $E_n \cdot \text{Time} \cdot h$

So  $E_n = \frac{h}{t}$ ;  $\frac{1}{t} = \frac{E_n}{h}$

$\frac{1}{t}$  is bits/sec for 1 bit;  $\frac{1}{t}$  for N bits w.  $\frac{1}{t}$  sec. →  $\frac{NE_n}{h}$  Joules used.

$\frac{E_n}{h} = \frac{E}{h \cdot t}$ ; Power is  $\frac{E}{t} = \frac{h}{h \cdot t}$ ;  $\frac{1}{t} = \frac{E}{h \cdot t} = \text{Power for } \frac{1}{t} \text{ bits/sec.}$

So  $\frac{1}{t} = \text{bits/sec} = \sqrt{\frac{E}{h \cdot t}} = \sqrt{\frac{\text{watts}}{h}} = \sqrt{\frac{\text{watts}}{6.626 \cdot 10^{-34}}} = \sqrt{\text{watts} \cdot 3.929 \times 10^{16}} = \text{bits/sec}$

$\sqrt{\text{watts} \cdot 3.929 \times 10^{16} \text{ bits/sec.}}$  for 25 watts (human brain)

Thus is only  $1.942 \times 10^{17} \text{ bits/sec.}$  ~  $2 \times 10^{17} \text{ bits/sec.}$

How much of the 25 watts is used for computing, is unclear. //

There may be a big cu Qd reasoning, hvr - ; // prog. w. bits per sec or power may give ~ of power for such // prog!

Also, t. Q of how much power (if any) is needed for Memory access

ESL

A poss. model for EBL: A problem set is given in a particular domain, in which one has much "knowledge", both domain specific & logical skill.

There is an effort to solve (or almost solve) the problem deductively, using heuristics ("knowledge": but heuristics is a fair amt. of CC involved in the process of deduction).

So: Next time a "similar" problem occurs (presumably JM has good and relevant category concepts to realize particular relevant "similarity") it reduces the CC of deduction considerably by patterning after the previous case. This is a bit like CBR,  
(3 OSL)

Bslg.

$G(x) \cdot f(t)$  : "super OZ problem".

on the "super OZ-problem":  $G(x), f(t)$  :  $G$  is conc for candidate  $x$ ,  
~~where~~  $f(t)$  is monotone & func of time; Both  $G$  &  $f$  are known to TM.  
Find  $x$  in time  $t \Rightarrow G(x) \cdot f(t)$  is Max.

[More generally Given  $G(x, t)$  w.  $G(x, T_1) \geq G(x, T_2)$  if  $T_1 < T_2$ .]

Use techniques of MCT to deal w. this:

TM has many cases of  $OT_i (G_j(\cdot, \cdot), G_{j,i}, T_{j,i})$

each  $i, j$  will usually have several (often many) "k" trials w/ varying diff.  $x_{j,k}, T_{j,k} \approx G_{j,k}$  values.

$OT_i$  is...  
Optza. tough because  
This is true, for each  
 $OT_i$  will have a single  
supply criterion that  
may or may not be met.

From data on many  $OT_i$ 's :  $G_j$ 's (TM's) (like experience)

TM is able to obtain a cred. p.d. giving  $Pr_{OT_i} (OT_i, G_j(\cdot, \cdot), G)$

It is the p.d. of  $OT_i$  giving to  $G$  for problem  $G_j(\cdot, \cdot)$ .

From this and (.11) cond. p.d., we obtain  $Pr_{OT_i} (OT_i, G_j(\cdot, \cdot))$   
which is the probability that  $OT_i$  will have the best (over all  $OT_i$ 's)  $G$  for  
for problem  $(G_j(\cdot, \cdot))$ .

Using .13, one does an Lsearch over all  $OT_i$ 's. ~~is~~  
The usual Q comes up. "When does one stop" — Each  $OT_i$  tells one  
as part of its data. "when to stop"

.16 is wrong. One simply picks the <sup>simple</sup>  $OT_i$ . That is most likely to

give max  $G$  for problem  $G_j(\cdot, \cdot)$ . The data used for p.d. of .11 and .13 (which is directly derived from .11 w/o any new data)

say  $Pr_{OT_i}$  (a prob. will) includes info for several  $T_{j,k}$ 's for each  $OT_i$  ( .07-.09 )  $\approx$  ( (.07-.09) ) The Data is (.07-.09) The  
Results p.d.s are .11 & .13.

.26 O.K. Now consider regular OZ problems. It was not (I believe)  
evident to show that Lsearches (practically) near optimum for OZ probs  
(the it's second to best for INV problems) — Could it be best for  
Normal OZ problems as well, ~~with the latter~~ (i.e.  $f(t) = \text{constant}$ )

The soln. of .19-.20 is best? i.e. just pick the "Best  $OT_i$  that is  
most likely to be best" & check with it.

In both the  $G(x), T(x)$  & the classical OZ problem; As we work on the  
problem, the p.d.'s of .11 & .13 may change, but we cannot usefully use that  
info directly. What we want to know is the p.d. over the  $OT_i$ 's involved  
in a jump to those  $OT_i$ 's. In the case of <sup>many</sup>  $OT_i$ 's this involves a "startup cost" —  
one can often use data from trials ~~for~~ for an  $OT_i$  for info on ~~the~~.

.37 prospective new  $OT_i$ 's.  
In <sup>much</sup> of the future; One must spend time computing probabilities  
that various  $OT_i$ 's will be best. There is a nice trade off betw (2.14.01)

→ 2.14.05

01:21:37 that time is  $t$ , time used to make TRIALS <sup>themselves</sup>. In  $t$ , Pogo discussing I have  
 2 sound that cost of  $2$  trial is  $\gg$  usual cost of problem making PC  
 estimates. We note, here, that: CC spent on PC estimates can  
 be ably large: it's not clear how much CC to spend on them!

"On use of  
 forth" for  
cond comp.

05:21:37 In general, for even "regular" OZ probs. It would be best to start out w.  
 1.  $OT_1$ . That is most likely to be "Best". Work out until stay w. that  $OT_1$ ,  
 unless/until  $t$  data on cards tried thus far (or any other info), makes it  
 clear that (including cost of switching & start up costs), it is not the  
 Best  $OT$  is no longer  $OT_1$ , but  $OT_2$  — so we switch to  $OT_2$ ,  
 then to  $OT_3$  or may be back to  $OT_1$  — depends on how things look.

The Success of this method will depend much on how Good  
 one's  $P(t)$  is. — but  $t$  some can be said about normal LSch  
 for OZ or INV probs

14 **Advantage of picking a (in Normal OZ probs)**

Of picking the "Best"  $OT$  & staying w. it until it no longer looks Best!

16 If there are several  $OT$ 's all about equally Good — all "at top" of  
 the Goodness Range — Normal LSch will spend about the same amount of  
 time on each of them, rather than just pick one and work on it

Usually to end  $t$  — This last is usually a most efficient way,

One serious disadvantage of this last approach is that we will get  
 much less data on "non-top"  $OT$ 's, so we will tend to not find  
 anything better! It is an "Elitist self-reinforcing Hypothesis"

→ Is this Criticism also true to the G(x) · F(t) case?

- ①  $\frac{PC}{CC} \text{ vis } \frac{2^{-kcost}}{CC}$  ;
- ② Failures in many II ~~proc~~ procs,
- ③ MONTE CARLO TM (MCTM)

In 1999, world production of 32 bit CPUs for computers was ~~~ 100M units~~ 100M units.  
 M units at 10<sup>9</sup> bits/sec is 10<sup>15</sup> bits/sec;  $\equiv$  IFC of "Blue Gene".

10<sup>15</sup> may be > (human, so 100M units may be ~~max~~ max of sci. community - so  
 "Over Parachute". In 10 yrs, IFC  $\rightarrow$  x100.

One problem w. (1) machines of this number, is failure of individual uproc  
 [IBM Blue Gene] is supposed to grow away of dealing w. this.

Another way write by Monte Carlo procs. In 1990 (or 1991) I did  
 a study of Mt Carlo choice of cond<sub>i</sub> to try. The prob of trying  
 a particular cond<sub>i</sub> was  $\propto$  its  $PC_i^{E-1}$  (or was it  $(1-PC_i)^{E-1}$ ?)

Anyway, the goal at that pt. was to get to effective use of  $\frac{PC}{CC}$   
 as ordering of trials rather than  $\frac{2^{-kcost}}{CC}$ .

If it works  $\odot$ , it might also be a good way of dealing w. occasional  
 of individual uproc.

In general, my work/interest in Monte Carlo methods of such has been  
 motivated by the poss- use of "Crumby Components".

Correction of Errors in Languages / <sup>from</sup> (Grammar): Several "Takes" on My:

.02

1) Recent stuff I wrote Wolff, is my correction grt. - I had 2  
Somewhat different "Solns." - Hvr, .06 of 13 to write my to do it!

2) ~~Method~~ Method of correction used in ~~the~~ linear / n.l. regression; The  
model gives a prediction <sup>of error</sup> which we have a p.d. in ~~the~~ "correction".

.06

This method might be ~~the~~ adapted to Language prodn,  
Use ideas in my version of of 57813 for Languages! - So that  
for languages, each bit in the corpus is given a p.d.

.09

In fact, .06 ~~is~~ <sup>is</sup> ~~an~~ u-p. way, since we get from  
the error theorem, an expected error for ~~the~~ ~~Best~~ ~~RMS~~ error  
(~~is~~ ~~error~~) <sup>like number?</sup> for the prodn.

Gram Err Thm.  
GE Thm

Call the analog of 57813 for unworded finite strings "J. Grammar  
Error Thm." v.s. 57813 "The Time Scores Error Thm"  
or "Regression Error Theorem" So us "TSE Thm" = 57813 or its corollary.  
TSE Thm TSE Error Thm

Hvr, "Symbolic Regression" usually may refer to  
(~~is~~ usually does) unworded ~~finite~~ finite strings.

Hvr, I have to work out more details of .06. Just how its applied  
to all sorts of langs. - I think the corrections are to be applied to each bit  
of the corpus as it is generated. This Area Needs More Work!

In hill climbing, momentum is often used to guess at direction (size) of next step: i.e. Say  $\vec{x}$  is the current vector, & we are trying to find  $\vec{x} \Rightarrow G(\vec{x})$  is max. ( $G \equiv G(\vec{x})$ ).

$$\text{"Momentum"} = (\vec{x}_t - \vec{x}_{t-1}) \cdot (G(\vec{x}_t) - G(\vec{x}_{t-1})) = \vec{m}_t$$

Our next trial,  $\vec{x}_{t+1}$  would then be  $\vec{x}_{t+1} = \vec{x}_t + k \cdot \vec{m}_t$ , where  $k$  is a factor to be measured by USR.

Actually,  $k$  depends on our estimate of the second derivative of  $G$  w.r.t.  $\vec{x}$ , & we can estimate it empirically from past (perhaps  $X$  window) data.

$$.10 \quad \text{say } \Delta G = m \Delta x + \frac{1}{2} s (\Delta x)^2 \quad (s \equiv \text{second derivative})$$

$$\text{we want } \Delta x \Rightarrow \Delta G = \text{max} \quad m + s \Delta x = 0 \text{ so } \Delta x = -\frac{m}{s}$$

We find  $m$  &  $s$  by doing a curve fit over at least  $r$  set of data

.13. pts. (or use an  $X$  window of width  $r$ ).

We can only do .10 & .13 once, but, since it keeps  $\vec{x}$  on a simple st. line in  $\vec{x}$  space. After we do .10-.13 once, we might do a trial in a random direction. — Hvr, size of step is unclear.

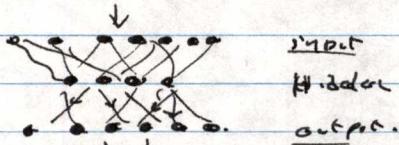
Size of step could be related to the "Noise level," which we could have obtained in the previous .10-.13 calculations.

Bulg

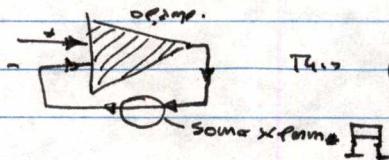
ANN, Fractals, Fractal Compression, CFG-discovery

07.22.90 Discussn. of Simon ( Grad Stud. w. J. Pollac at Brandeis.)

3 layer ANN



Output is fed back to hidden layer: This is analogous to



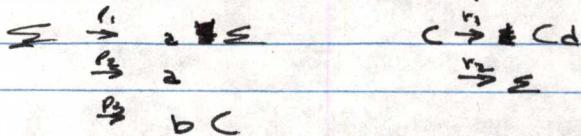
Say "A" is a Parsing Algm. — Say its a Matrix Parser w. Real (not Boolean) wts. — Suits for a stochastic CFG (or CDG)

The params of A w/o t. wts in t. ANN are adjusted using standard ANN w/o GA rules.

I Guess that we want to adjust wts. of ANN: Params of H so that t. input. output of t. ANN is to reproduce its input.

Doing Matrix Mult. w. Reals, is much more expensive than using Boolean values! So one might use stochastic instead Boolean values in t. Matrices! — This would then be like IFS (Iterated Functional Systems). Instead of a probly value of P<sub>ij</sub> in a matrix element, T<sub>ij</sub> element would be 0 or 1; ("i" w. probly P<sub>ij</sub> hrr.)

Consider a CFG:



Here, we have 2 N.T.'s: S & C: They correspond to Matrices.

The a, b, c correspond to wtd. addition rules on Matrices.

There are 3 terminals: a, b, c.

We could start w. 2 vars (supp no of possl. / production. rules for each N.T. So S would have 10 probly values assoc. w. it.

As we continue t. process, hrr, the var ~~is~~ discover that only a few probly values are >> 0.

we might start w. t. Grammar

