

To be (perhaps)

Given at Cal Tech,  
Feb 26 60

The Inductive Inference Problem and the Representation of Information in  
Biological and Electronic Systems.

- 1) What the problem of inductive inference is.
- 2) Criticism of some proposed solutions to the problem.
- 3) "Language-based" inductive methods.
  - a) The methods of Carnap.
  - b) The methods of Solomonoff.
- 4) Relationship to problems of optimum coding of information in:
  - a) The brain
  - b) Chromosomes
  - c) Non-biological information retrieval systems.

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For Introduction of idea of use of min. coding for prob. eval:

In optimum coding of messages, for communication, any regularity in the ~~mess~~ seq. of symbols is utilized to reduce the no. of bits needed to code the message. We use a priori information about the relative probability of various possible sequences of symbols, to reduce the no. of bits needed for coding.

In the system proposed, we invert this procedure and try various methods of coding a given sequence of symbols. The <sup>no. of bits of the</sup> coding method that is most compact, is then used as an index of the a priori probability of the sequence coded. [actually, we sum the a priors of all ways of coding the seq. — only the most compact descn are signif., hrr. (mention convergence probs)] .

the ind. inf. prob.

Poly 2's  
136 of desire.

(1)

A few of Th. Q's that ~~wantable~~ should be answered by  
a satisfactory Theory of ind. inf.

- 1) In any circumstance for any previous history, give a probability for any possl. continuation.
- 2) Give th. freq. ratio for <sup>the. rel. prob. for</sup> large samples.
- 3) Explain why theories devised before emp. data is known, and verified by that data, are given more credence than those devised after data is known, and agree with that data.

We may say that post hoc theory may be ad-hoc - a priori theory is less likely to be ad-hoc. But we feel that whether a theory is ad-hoc or not should be determined by examining Th. Theory itself, and not Th. history of Th. Theory - otherwise we clearly do not understand "operationally" what ~~exacts~~ characterizes an "ad-hoc" theory. Also, ~~therefore~~ it is likely that a theory should have degrees of ad-hocness - not ~~that~~ have ad-hocness ~~for~~ & yes-no property, depending whether Th. Theory was made up before or after Th. expts. were performed. (give Th. Einstein-Milne example)

4) Th. problem of "Geometric Probability" - its relation to ~~your~~ evaluation of a priors. How geom. prob. is a rather special case of diffy in using "Th. principle of indifference".

5) When can "Th. principle of indifference" be used?  
(see 4).

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(2)

6) Th. B.G. (or Max. Coin) problem: What to do when  
2 different freq. counts ~~provide~~ give different probby  
estimates for 1. same event.

7) In (Vol II I think) Polya, there <sup>is a lot of</sup> ~~are~~ some desirata of  
inductive inference systems.

8) Th. principle of parsimony should hold - i.e. greater aprop  
to "simpler" hypotheses.

Z A T O R C O M P A N Y

140½ MOUNT AUBURN STREET · CAMBRIDGE 38 · MASSACHUSETTS · TROWBRIDGE 6-6776

Mar 2, 60 U.S. Penn.

THE USE OF FORMAL LANGUAGES FOR MECHANIZED INDUCTIVE INFERENCE

For many years, standard algebraic curves have been used to smooth, interpolate and extrapolate quantitative empirical data. It will be shown how formal languages may take an analogous role in smoothing and extrapolating qualitative data. Some examples of this kind of extrapolation are the discovery of the general grammar rules of a language, from a finite sample of acceptable sentences in that language. Other examples of induction of this sort in linguistics and mathematics will be given.

A particular type of language, called the "weak phrase structure language", has been investigated at some length, and some of its applications will be shown in inductive inference for multidimensional, as well as linear patterns.

## Th. talk itself:

This will start out with some detailed analogy betw. curve fitting and grammar fitting. Give some actual results of this ~~method~~ "novel" way of looking at curve fitting - e.g. that for n data points, one may have a ~~one~~ or 3 parameter curve b/w "best-fit".

After this, which is to motivate interest in "grammar fitting", for extrapolation, - go into langs in more detail - in particular th. general non-distr. psl. and its various applications. Just mention, but do not demonstrate, th.

use of a TM<sub>2</sub> for multiplicity.

Much of th. material will be th. same as for Th. RCA talk.  
Perhaps some info on use of stock langs. for

- ① MT
- ② IR
- ③ optimum learning of an operator T.M. (reconf. learning).

---

Letter to Gorn: ① Mention "Tree langs".  
② how lang will tally be? ③ Give him more details on talk, as

Mar. 2. '60

Talk /<sup>actually</sup> at U of Penn Seminar.  
4 P.M.

①

1. Defn. of "Lang."

a) Alphabet.

b) Sub-set of order seq's of Alphabet symbols.

c) ~~Lang.~~ Examples: ① English (with letters or words as "Alphabet").

② All strings express whose values = 0

③ All legal thms. That follow from

a fin. set of postulates.

2. Probs. in Lang.

2) GRM

2. Def. of "Grammar"

$a^m k_0 b^m k_1 c^n$

① a) Constructive

b) Decision procedures.

3. Probs. in Lang.

a) Construct  $\rightarrow$  Decis. proc. form (e.g. in math.)

b) Dec. proc.  $\rightarrow$  Constr.

"simplest."

c) Induction; Grm. set of ass's - to find Grammar.

\* ① If one can ask Q's.

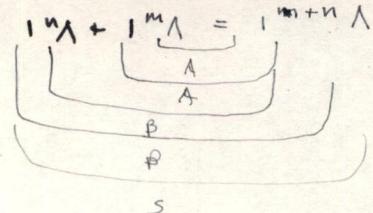
② " " can't " "

4. Examples of simple langs:

a) FSL. gen. by FS Machine.

b) PSL

$$1^n \Lambda + 1^m \Lambda = 1^{m+n} \Lambda$$



S

A  $\rightarrow$   $\Lambda$  =

A  $\rightarrow$  |A|

B  $\rightarrow$   $\Lambda$  + A

B  $\rightarrow$  |B|

S  $\rightarrow$  BA

Mar 2. 60

5. PSL's

More gaul. than simple concat. frgs.

(2)

- a) Chem. Compounds.
- b) MT Give defn.
- c) Use for Multiplic. - Hyper Order frags.

~~Learning, Induction.~~  
~~with Q =~~  
~~W:~~

Questions briefly

Linguist ind. inst.

Talk lasted ~ 55 min. - wasn't very well organized

Things to discuss with Chomsky:

1. Has he shown that Eng. is not expressable by type 2 langs? <sup>Non CDS?</sup> rather than my counter examples
2. " " " " " " " " " " " " type 1 <sup>CDS?</sup> " ?
3. (a) Th. importance of MT studies, rather ~~than~~ than grammatical studies ~~to~~ to determine "true" structure. e.g. MT of  $L_1$   $\rightarrow$  "Meaning of  $L_1$ ".  
(b) How str. for MT may not = str. needed to construct  $L_1$ .  
(c) How Parsing grammar may not  $\equiv$  construction grammar.
4. ~~Paradox of generalized Postman's theorem for all decidable, finite grammar.~~
5. / <sup>non-dim.</sup> PSP's - are they weaker or stronger than type 2 langs?
6. Stochastic Langs - ~~the~~ a soln. to th. ind. inf. prob.
7. Get reprints:
  - (a) Review of Skinner's book ("Verbal Behavior")
  - (b) " " Greenburg's essays in Linguistics
  - (c) "Formal props. of Grammars"
8. Th. Subclass of SPSL's used by Th. & UofPenn Group for Parsing English  
(a) Can it do  $AB \rightarrow BA$ ?
9. Quick way to tell if 2 PSG's are identical?  
(a) w PSG  
(b) S PSG.  
(c) How equiv. PSG's may form a PSL.
10. How "Dimensionality" may help with 9.) <sup>↑</sup> see PSGency 467.28 for dozen of "dimensionality"

3-4-60

Prob. of Art. Intell.

Gu. &amp; Natl. Bu. Standards.

March 4, 60

~~On Neural Nets (Random Network)~~

Lasted  $1\frac{1}{2}$  hrs.

— rather well given.

$\approx \frac{1}{2}$  hr. on new. ind. inf. idea  
I don't think they got much out  
of that, however. — Too heavy a lot  
of jargonists in audience.

(c)

① Art. intellig. : ~~design ind. inf. system~~

2 dim. patt. discy :

② Idea that soln. to ~~statis.~~ stat. inf. prob. is known  
that prob. is to make work practical II computer  
using neural nets.

③ That ind. inf. prob. is not solved:

e.g. @ T. S. That ~~seems~~ to change statistics.  
Stock market.

④ II lines of inference.

Blue eyes — die at 60, prob.  $p_1$ .

red hair — " " " " "  $p_2$ .

(c)

ASK Q's if particularly interested in any  
topic mentioned.

$$A \cap B = n(nA \cup nB)$$

7-4-60

Idea of talk:

Just what langs. are:

- A. Determ. Ord. langs
  - B. Stoch langs. (
- FSL  
W.PSL  
More Genl. langs.

Most Genl. langs. (In terms. of Turing Machine)  
(i.e. Fixed strings, followed by arb. strings).

1) What langs. are: Some Examples

2) Applics. of "langs." a) M.T.

b) Extrapolation (= concept formation,

(Gestaltian) — E.g. "curve fitting", Char. Recogn., Discovery of "characters", Discy of "invariants"; Scientific Laws, weather prediction,

3) Examples of langs. recog. by finite Automata.

a) FSL      ① Deterministic

② Stoch      (=Markov) .

b) WPSL      ① Determ.: example.

$$\begin{array}{c}
 S \\
 S \rightarrow ab \\
 S \rightarrow aSb \\
 \dots \quad \quad \quad z^n b^n \quad (n \leq 1)
 \end{array}$$

Subs. rules: ① Always ↑ length. of strings,  
② No CDS.

$$S \rightarrow \underline{Np} \cdot \underline{Vp}$$

$$\underline{Np} \rightarrow \underline{\text{Art}} \cdot N$$

$$\underline{Vp} \rightarrow V \cdot \underline{Np}$$

$$V \rightarrow \text{saw}$$

$$V \rightarrow \text{was}$$

$$N \rightarrow \text{Boy,}$$

$$\text{Ma}$$

$$\text{Dog}$$

Multi-dim. ~~PSL's~~ PSL's.

How MT may be a PSL  
for some lang. pairs.

e.g. Ord. alg. to "Polish" notation

~~PSL's~~

Organic Chemicals.

3.4.60

$$\underline{111\Lambda} + \underline{111\Lambda} = \underline{11111\Lambda}$$

$$\underline{\underline{A}} \rightarrow \underline{\Lambda} =$$

$$A \rightarrow 1A1$$

$$B \rightarrow \Lambda + A$$

$$B \rightarrow 1B1$$

$$S \rightarrow BA$$

$$1^n\Lambda + 1^m\Lambda = 1^{n+m}\Lambda$$

$$1^n\Lambda + 1^m\Lambda = 1^m 1^n\Lambda$$

Arith. Multiplic

$$K_0 \underset{\uparrow}{a^n} K_1 \underset{\uparrow}{b^m} K_2 \underset{\uparrow}{c^m} K_3 \underset{\uparrow}{d^n} K_4$$

#### 4) Problem of Induction :

simplest. lang.

Easy if Q's can be asked.

Deferring. lang.

Info recd.  $\begin{cases} \text{say } b \text{ is learned} \\ \text{at present, under} \\ \text{unreal condns.} \end{cases}$

Much diff if error is made.

#### 5) Prob of ~~Induct~~ Induction:

Stock PSL's.

S

$S \xrightarrow{?} ab$

$S \xrightarrow{?} aSb$

genl. soln.

- Several ways to parse giv. S.  
Several "Parsing" routines.

(Stock Gram; S)  $\rightarrow$  prob.

(corpus, Stock gramm)  $\rightarrow$  ~~prob~~ prob.

(corpus, stock gramm, ~~=~~ aprip(gramm))  $\rightarrow$  ~~=~~ aprip.

To ~~measure~~ chose stock Gram  $\rightarrow$  aprip is max.

or more genl., stock exact soln.

- Is hill climbing problem

Idea is to find types of "proximity funs".

SOS talk : May 22-24, 1962 Proby 2478 Orchard  
 Chicago

~~1) Give background of old work.~~

~~a) ERE pap.~~

~~b) Verlin. (unsatisfactory soln.)~~

~~c) Gau. Ind. Inf. Theo.~~

- LA 8 -  
 (Kirsch)  
 sh

2) Present approach is to solv. improving Machine.  
 (with resp. to some criterion)

a) Gau. program improving ~~of~~ machine with resp. to

~~b) Such a machine is pu. probs like itself, to start out~~

~~c) Machine is g.u. itself.~~

~~d) Most probs. of int. ~~can~~ be expressed as H.c. probs. on pgs.~~

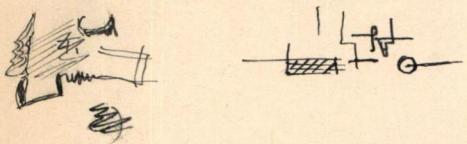
3) first step is simple and inf. machine.

a) Descr. in ~~more~~ little detail.

b) How differs from <sup>my</sup> ① OK approach

② ~~teilburn, Sunnar, Grindalde~~

③ Newall, Simon.



conds. under which opt. approach is reasonable

27 48

fpn. takes much time

or exp. 78 27

(randomness, non opt. search,

∞ search time using "P" search.

↑ Discuss ~~opt.~~ solvability v.s. unsolvability irrelevance

— Need for new opt. search

speed also gives opt. ext. opt.

in uniformly bad (except poor work).

Theory with criterion of solvability with resp. to pu. machine size and time of soln.

Analogy to opt. coding

in noise, using ~~additive~~ various code lengths.



4) a) Next step is improvement of Hours

b) Systematization of hours.

c) Event. of magmas of hours

" " U of set of hours

5) Various work on / pgs imp. prob. — (how differs from Ariyaratna, say)

a) Hours are similar

b) work on hour improvt. prob.

6) Most probs of int

6) Some details of "rules", hours, etc.

$$\begin{aligned} A + B &\rightarrow M + AB \\ A - B &\rightarrow M - AB \\ (A) &\rightarrow \# A \end{aligned}$$

b)  $3 + 4 \times 5 = 23$

$$\begin{aligned} &A + \# B \\ &3 + \$ - (5+2) \\ &3 + \$ - (?) \\ &\cancel{3 + 8 - (2)} \\ &8 - ? \\ &\# . \end{aligned}$$

$$\begin{aligned} &A + \# B \\ &\cancel{3 + \$ - (5+2)} \\ &\cancel{3 + \$ - (?)} \\ &3 + \end{aligned}$$

## SOS cont talk:

- 1) prob. - ~~the~~ Machine to (a) solve diff. non-poly. probs. (adequate vocab. to solve anything)  
 (b) Self-improving - can work on prob. of improving self.

(c) A machine built to ~~optimal~~  
find pms. That are opt. with resp. to ~~certain~~ <sup>any</sup> gn. criterion.  
 (d) Give machine prob. of improving ~~itself~~

- (e) First step is simple ind.inf. machine. - crit. learning.

(a) Like  $3+7 = 10$

(b) Rules are like  $A+B \rightarrow M+A+B$

(c) Randomly constructed from basic Alph. of symbols.

(d) How differs from my work of ~~me~~ ~ 5 yrs ago

① U of abs. not worked out at that time..

② Now I have ~~more~~ apparently workable Gen., ind.inf. theory.

(e) How differs from Kilborn, Soumar, Grimsdale ~~etc.~~, ~ 1959

① ~~me~~ They tried to make a machine that would look like thinking, prob. solving human.

② Concern with randomness "for originality".

\* ~~P~~ <sup>2</sup> Differ. on P,  $\sqrt{P}$ , "optimum" search.

~~V~~  $\sqrt{P}$  faster than P, but "poor" ansn.

opt. faster than ~~P~~ <sup>any</sup>, also "better" but not always realistically faster.

(b) Criteria for success are simplified by reasonable constraints. e.g. search time  $n$  for n possy,  $\rightarrow \infty$  as  $n \rightarrow \infty$ , but we can cut off trials & some "reasonable" n.

(II) ~~Computability, unsolvability~~  
 usually { unsolvability by finite machine } V.S. solvable  
 irrat. { " trivially" solvable } in time  $T$   
 by machine with max. of N.

? (Analogy to opt. coding in noise.)

(3) Improve ~~standard~~ solu. methods,  
" methods of finding ~~new~~ new solns.

~~(4)~~ Systematize of standard soln. methods into compact "notation" / due constraints so that possy. of creating these rules thru a random generating system is max.  
I.e. find ~~good~~ stock of rules

(4) Then work on form optns.

(2) ~~→~~ Hours seem n or identical /,

(5) Rules, hours, etc.

$$3+4 = 7 \quad A+B \rightarrow M+AB$$

$$A-B \rightarrow M-AB \quad \begin{cases} \text{O.K. for probs} \\ \text{with +, -, (, )} \end{cases}$$

$$(A) \rightarrow A$$

(6) ~~3+4~~  $3+4 \times 5$   
tech mult. <sup>div.</sup> first, then +, -.

(2) +, - rule are ~~with~~ context dependent.

$$\begin{matrix} \text{"f."} & (A-B+ \rightarrow (M-AB+ \\ & \uparrow \quad \uparrow \\ & \sim 50 \text{ cont-dep. rules.} \end{matrix}$$

(2) ~~at~~ interpretation & in sync with grouping of CDS rules : e.g.

$$\alpha A + \beta B \Rightarrow \alpha A + \beta B$$

$$\alpha = (, ), +$$

$$\beta = (, -, +, \{ \}$$

(7) some trial numbers.

for ~~AB~~  $A \times B \rightarrow M \times AB$

$10^{10}$  for simple, initial MCS search

50 better for later " "

20 " " opt. search,

~~MCS~~  $10^{-14}$  for raw  $(A-B+ \rightarrow (M-AB+$

(3)

N 1000 better for opt, + experience

log $\alpha$  factor for factorizn.

(+) Genl. method to compute  $\Gamma$  in appr due to  
 $\text{prosp}^{\text{ing}}$ .

Lectures given. To Murskey's class March 24, 1960 (1)

Essentially all of this material was covered in 55 min.  
Before lecture, 3 blackboards filled with diagrams.

1960 Mar 24  
No. 1960 Mar 24  
WED 24 FRI

### Motivation.

### 1. Goals; Ind. Inf.

more examples: (1) M. T. by example

(2) Classification of docs for IR, by example.

(3) Operator extrapolation. Gn. set of "good" 1-to-1 pairs. (appear?)

Mar 24 59 was  
Wed! (1960)

### 2. Concept of Langs.: (a) Alphabet, subset of strings.

Examples: English; binary + ; multiplicity problems; correct algos.

theorems folg. from gn. set of axioms;

### (b) Types of FSL

(2) PSL.

kinds of Grammars:

(1) ~~Constructive~~ Constructive

(2) ~~Table~~ Table method

### 3. FSL's.



M in  $S_3$  at  $t$

Then M emits symbol  $a$ , and goes to state  $S_1$  at time  $t+1$ .

① Can be recognized by FS Machine. ② Constructable from "state diagrams".

Use in psych. testing by Chomsky Miller.

simple

Exists / discy procedure for G, if Q's decidable.

### 4. ~~PSL~~ PSL

example of essentially non-FSL:  $a^n b^n$ .

PSG:

$S \rightarrow ab$

$S \rightarrow a^nb$

cannot be recog. by FS Machine —  
e.g. Human. — man. neg = 0.

~~Simple English Grammar~~ is not PSG — but ~~PSG~~  
Grammar of Eng. in Q — innov.  
by Yngve.

Eng. as PSL:

$$S \rightarrow NP \cdot VP$$

$$NP \rightarrow Art \cdot N$$

$$VP \rightarrow V \cdot NP$$

$$V \rightarrow Saw$$

$$V \rightarrow Was$$

$$N \rightarrow Boy$$

$$N \rightarrow Men$$

$$N \rightarrow Dog$$

$$Art \rightarrow The$$

(2)

~~REMARK~~ ① Construction always ↑ length of string (or remains same), ② finite alph.  
 $\therefore$  lang. decidable.

∴ several & simple decision procedures.  
 e.g. ① Bar-Hillel (not very practical)  
 ② Two of mine.

Another form of PSL:

$$S \rightarrow a b$$

$$S \rightarrow a s b$$

$$a \times S \times b \subset S$$

$$a \times b \subset S$$

$$S \rightarrow A b$$

$$S \rightarrow B D$$

$$A \rightarrow D S b$$

$$A \rightarrow a S S$$

$$D \rightarrow b A$$

$$D \rightarrow d$$

$$\dots$$

$$\dots$$

$$\dots$$

$$\dots$$

$$A \times b \subset S$$

$$b \times D \subset S$$

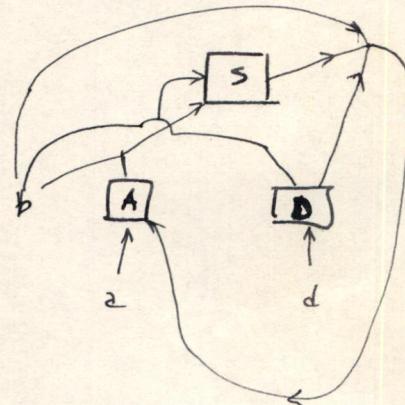
$$D \times S \times b \subset A$$

$$a \subset A$$

etc.

These x's may be

any operations



A, b, etc. may be classes of any kinds.

Gives Great Generality.

"Basic Loop" form of fSL's, PSL's. ??

ordinary

PSL

$$a^n b^m c^p d^q e^r$$

$$a^n b^m c^p d^q e^r \text{ impossible.}$$

Is possl. with more genl. PSL's like

$$\text{e.g. } (a, b) \times (c, d) \rightarrow a c b d$$

Ex samples of ~~PSL's~~ PSL's:  $1^n \lambda + 1^m \lambda = 1^{n+m} \lambda$

$$1^n \lambda + 1^m \lambda = 1^{n+m} \lambda$$

$$\begin{aligned} S &\rightarrow BA \\ B &\rightarrow \_ IBI \\ B &\rightarrow A + A \\ A &\rightarrow 1AI \\ A &\rightarrow \lambda = \end{aligned}$$

Also subtraction

for multip's of 2 nos. we don't have PSL, but grammar is a PSL.

" of 3 nos., Gramm of Gramm of Gramm is PSL, etc.

M T  
first explain  
"Polish"  
notation

$$\begin{array}{ll}
 Q \xrightarrow{\quad} a & N \xrightarrow{\quad} - \\
 Q \xrightarrow{\quad} a & N \xrightarrow{\quad} s \\
 \xrightarrow{\quad} b & \xrightarrow{\quad} + \\
 \xrightarrow{\quad} b & \xrightarrow{\quad} A \\
 \xrightarrow{\quad} c & \xrightarrow{\quad} I \\
 \xrightarrow{\quad} c & M \\
 \xrightarrow{\quad} (Q N Q) \\
 | \quad | \quad | \\
 I N Q Q I
 \end{array}$$

Example:

$$\begin{array}{c}
 a I (b + c) \\
 \cancel{X} \cancel{I} \cancel{X} \cancel{I} \\
 M a I A b c I
 \end{array}$$

Note: Do "+" substit.  
befor "M". Practice this  
before lecture.

State of induction problem:

PSG discy with Q's, can be done. So MT could be done  
but (1) large no. of Q's.  
(2) ~~No~~ errors give trouble.

PSG discy w.o. Q much harder — much progress —

A tectological soln obtained. — (≡ Hill Climbing prob.) —

# Several hours obtained — adequacy unknown —

Gauß. soln. Ind. inf. prob.

Stock langs were mentioned in only a very cursory way,

Fri May 20, 1960

This was the 2nd part of  
the lecture of Mar 24, 60 on

## Talk to Marvin's Class!

Topic: 1) Stock PSL's

2) Genl. Ind. inf. by coding - how connected to

3) 1956 Ind. inf. Machine

- how to compute utilities - actual examples

4) How to compute U's for Pandemonium and GPS.

5) Use of for curve fitting,

33.95.05

$\frac{8}{2} (a_{k+l})^{k+l} \times \frac{1}{2}$

$\frac{8}{2} (a_{k+l})^{k+l} \times \frac{1}{2}$

Method: ① Go thru Pandemonium, showing where epis. prob's arise  
- how U<sub>total</sub> is needed

② Go thru & find learning variables

Showing where U<sub>total</sub> is needed.

③ Present genl. Proc. of ind. inf. Give simple example of

Markoff chain using "F" coding.

④ Show how curve fitting is done: ① Normally - what difficulties?

② How done by coding

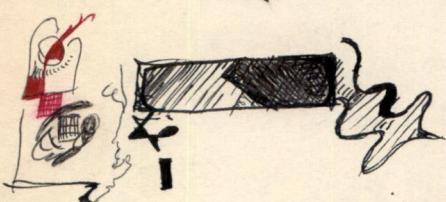
{ ~~How RMS error is used~~ }  
~~By special notation for Gauss distribution~~

2 extreme kinds of Gaussian - how avoided.

Show how PSG's are coded: Show how two cases

be done with

FSL

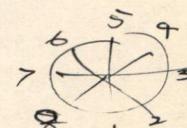


1 2

(=, 1)

= 1 (=, 1 0 1)

1 0 1 1 0 / = 0 , = 1



= 0 0  
0 0 | also

0 1 |

also 1 1 2 x (=, 1 1 )

ng (H.)

" " " (=, 0 0 )

⊕ 1 1 0 0 1  
0 1 0 1 0  
—————  
1 0 1 1 1

⊕ 1  
|  
1

⊕ 1  
|  
1

Fri May 20, 1960 for Marvin's class.

## Actually Gn:

① Pandamonium: combs of ops.

② use of neg. & kn. probcs.

③ " " upw. probcs, with defns, and Utility

$$U_{\text{child}} = f(U_{\text{parent}}, \boxed{\text{Emp. Usefulness}})$$

④ Dart T.M.

⑤ ⑥ = use of  $\frac{1}{\sum 1}$

⑦  $\sim \frac{1}{\sum 1}, \sim \frac{0}{\sum 1}$ , etc.

⑧ use of  $\frac{1}{\sum 1}, \frac{0}{\sum 1}$ , etc.

⑨ " "  $\frac{1}{\sum 1} \times ( =, \frac{1}{1})$

$\frac{1}{\sum 1} \times ( =, \frac{1}{1}) \leq \text{etc.}$

$\frac{1}{\sum 1} \times m,$

⑩  $\oplus$       
$$\begin{array}{r} 1001 \\ 1010 \\ \hline 1011 \end{array}$$
       $\left. \begin{array}{l} \text{use of } \frac{1}{1} \text{ only} \\ \cdots \quad | 0 \\ \quad \quad | \\ \quad \quad | \end{array} \right\}$

and ⑪ 
$$\begin{array}{r} 1001 \\ 1011 \\ \hline 1001 \end{array}$$
       $\left. \begin{array}{l} \text{use of } \frac{1}{1} \\ \text{use of } \frac{1}{1} \times (\oplus, 1) \\ \quad \quad | \\ \quad \quad | \end{array} \right\}$

⑫ Coding method of ind. inf. / Not too much detail  
some discn. of n.b. PSG discy.

⑬ Some applic of ⑫ to usual for Pand. and to hill climbing.

The delivery of tables was good. Topics ⑫ and ⑬ not explained very well.

Talk to Marv's class Wed May 16, 62.

On or on Coding Method of Ind. Inf. How is it "solved" now, and how well?

1. What is problem? Give examples: weather, Horse racing, Sc. laws, stock market, trial steps in Math proofs, curve extrapolation
2. Why is it worth solving? → we'd like to do it better, than we do now, perhaps with machine aid — perhaps learn to combine processes of human experts.
3. a) What's wrong with the obvious solutions?
4. b) " " other proposed solns?

4. What is my solution? How does it differ from others? How does it overcome difficulties other theories have trouble with?

Perhaps try to combine 3) and 4).

My soln.: 1) That all induction probs. can be reduced to induction on very long symbol strings containing all info. that is used in th. induction. (Perhaps give examples).

2) I use Bayes' Rule: Give example of how used:

$$\begin{aligned} & - \text{a b a c } \text{ a a b a} & P_1 = 1 \times 10^{-5} \\ & - \text{a b a c } \text{ a a b b} & P_2 = 3 \times 10^{-5} \\ & - \text{a b a c } \text{ a a b c} & P_3 = 2 \times 10^{-5} \\ P(a) : P(b) : P(c) & = 1 : 3 : 2 \end{aligned}$$

3) I can compute a priors. (This has been always been diffy of using Bayes). — I do this by concept of "simplicity" of a descn. (is ~ to Occam's Razor).

4) How  $\begin{array}{c} 111111 \\ 111110 \end{array}$  seems simpler than  $\begin{array}{c} abcabc \\ abcabcab \end{array}$  — and has a simpler descn.

in English.

Also  $\begin{array}{c} abcabcabc \\ abcabcabc \end{array}$  has simpler descn ("3 - abc's.") vs.  $\begin{array}{c} abcabcabc \\ abcabcabc \end{array}$

5) A more rigorous formulation:

$$M(\bar{T}) = \bar{M}T \quad (\bar{T} \text{ is string, } T \text{ its descn.})$$

$\uparrow$  Universal Machine (not necessarily a Turing)

a prior of  $T \approx 2^{N(\bar{T})}$ .

6) Better include other descns. of some  $\Sigma$ .

$$\text{so } \sum_i 2^{N(\bar{T}_i)}$$

Discuss  
Patt.  
Discy  
Thoreau  
proving.

Mention  
① Occam's  
② Principle of  
minimum  
description  
length  
③ Huffman  
Coding  
④ Shannon's Coding

6) (cont) This wouldn't converge in its own simple ~~form~~ form itself — we can ~~converge~~ patch it up to make it converge, but instead of Marrying its beauty — ~~never~~ consider alternate formulation!

7) Th. fixed code length method.  $R \gg N(\overline{P}_{\min})$ .

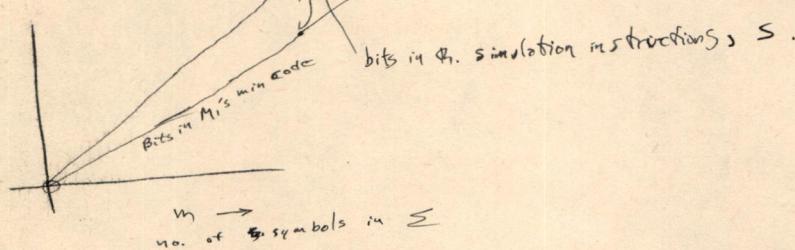
$$\frac{\cancel{N(R, P)}}{N(R)} \quad \left| \begin{array}{c} \text{lim} \\ R \rightarrow \infty \end{array} \right. \quad \frac{N(R, P_A)}{N(R, P_B)} = \frac{P_A}{P_B}$$

Show why ~~start~~ ~ same as 6).

8) Why 6) is machine independent.

First explain about "simulation instructions".

$$\text{i.e. } \Delta T, M_2(S\Delta T) = M_1(\Delta T)$$



pp 16, 17  
of ICP

9) Th. "All PEMS Method".

$$M_1(D_i \Delta T) = P_i(T)$$

$\nwarrow$  punct.

$$\frac{P_i(T_A)}{P_i(T)} = \text{probly, if } P_i \text{ is "normalized".}$$

$$\leq f(Q_i) P_i(T).$$

pp 27 - 31 of ICP

(Define Normalized PEM?).

~~f<sub>i</sub>~~ = fraction of strings of length  $R$  ( $R \rightarrow \infty$ ) that are "Doms of  $Q_i$ ".

10) Some applicns: ~~Dynamical~~ Bernoulli Seq,  
 (b) Codes using daths (give approx. formulae)  
 (c) Arith learning

11) Mantic <sup>Random Redundant</sup> Machine Method.

11)

## A method for Ind. Inf.

## 1. Some induction probs:

- a) Weather
- b) Horse racing
- c) Sc "laws"
- d) Trial steps <sup>trial sub-goals</sup> in Math proofs
- e) Curve extrapolation.
- f) Chess, checkers { Give areas of induction  
- finding good pieces to opt., etc.
- g) Info retrieval: Devise new categories,  
for ~~the~~ already indexed docs.
- h) Stock market

## 2. Relation to arb. infell. probs.

- a) ~~Human language~~ Patt. Recognition: Letters, spoken speech

- b) Theorem proving: When successive xforms: Set of observational results: What to do next:
  - a) what xform to use.
  - b) what new xforms or observations to devise.

- c) Simulation of entire human: plus built-in constraints.

Model of human: small set of wtd. "goals": Uses entire ~~the~~ life strings of observations to determine th. results of a contemplated action. (Also uses "built-in" info). Mention ancestral data - acquired thru evolution, as alternatively treatable by
 

- ① longer corpus (less el. way)
- ② short corpus but modified machine.

## 3. Classical Bayesian probability:

- a) We will use probit model in which we extrapolate long strings, containing all of the info. That we ~~will use~~ will use in induction. Mention Analog, Digo. conversion for R.W.

In the case of man, this would include evolutionary data for some form.

$$b) P(z|h) = \frac{P(h|z)}{\sum_j P(h|z_j)}$$

Show how it's done  
e.g. in 10, 12

$P(h|z_j)$  is th. a priori.

give example:  $\begin{array}{ll} abba & \cdot 1 \times 10^{-5} \\ abbb & \cdot 2 \times 10^{-5} \\ abbc & \cdot 3 \times 10^{-5} \end{array}$

- a) Simple things more likely (Occam's R.)

- b) More numerous causes make more likely (Bayes)

Princ. of similitude  
Huffman coding  
(a little detail here)

## 4. How to get a priors:

- a) Simple things more likely (Occam's R.)

- b) More numerous causes make more likely (Bayes)

## 5. How to get a prior's:

- a) My method: Use of "Turmacs"

Mention 3 tape Turmac, with input, both tapes  
(Fixed <sup>code</sup> string length, R)

output "

Memory "

$$\textcircled{3} P^*(a, T, M_1) = \lim_{R \rightarrow \infty} \frac{N_T^R}{N_a^R}$$

$N_T^R$  is with resp. to  $M_1$ .

" th. no. of input strings of length R, that are devns of T.

If  $M_1(s)$  begins with T, then "s is a devn of T with resp. to  $M_1$ ".

c)  $P_{\text{R}}$  is implementation of "Principle of Indif"

(2) Bayes

(3) Occams  $\approx R \dots$  (Slowest)

"short" d.cns are more numerous.)

Mention that  $2^{-N_{\text{shortest}}}$  is one poss. approx., (imp. for later analysis)

6) 2 other ~~similar~~ models: a) sum of all pair's

A <sup>normed.</sup> pair is an ~~significant~~ op. that assigns probas to strings.

$$P'(z, T, M_1) = \sum_j P(\text{pair}_j, M_1) \cdot P_j(z, T)$$

It can be shown that for a certain "goodness" criterion, this model is at least as good as  $R$ . best pred. method.

#

b) 3 type machine is model of universe. - i.e. To "explain" all things that man has ever experienced - including his interaction with the ~~real~~ world.

c) The randomly constructed machine for extrapolation. The problem of "is a randomly constructed <sup>universal</sup> ~~universal~~ machine useful?" As a model of an operator ( $\text{input} \rightarrow \text{output}$ )

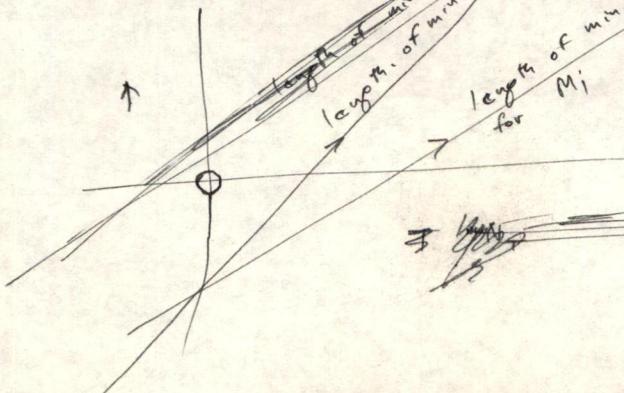
7) Diffys with Gen. Theory

a) Are predictions indep. of what Turmacs are used?

① Idea of "simulation instructions"

$\# \text{ If } \forall x, M_1(\alpha^x) = M_2(x)$   $\alpha$  is  $M_1$ 's "simulation instrns for  $M_2$ ".  $\# \exists \alpha \Rightarrow$  for all universal turmacs,  $M_1$ , and any machine  $M_2$ .

②



Note this deft. may be rigorously true for ensemble average  $T$  over all  $T$ 's.

$\# ( = \text{length of } T)$

7) Diffys (cont)

b) ~~Diff~~ Measuring fullness of

lim  
 $R \rightarrow \infty$

$$\frac{N_{T_2}^R}{N_T^R}$$

Ratio may be meaningful - tho.  
Num. and denom. don't

It may be possl. e.g. to show lim. exists — i.e.

that  $\frac{N_{T_2}^R}{N_T^R}$  is an ↑ funct. of  $R$ , for large and  $\Delta R$ 's.  
or that the fraction of codes ~~eventually halting~~  
~~not halting~~ in Time  $T$ ,  $\rightarrow 0$  as  $T \rightarrow \infty$

Difficult philosophical Q. involving meaningfulness even then.

Hvr., approx. are impf.

perhaps mention th. epist. "importance theorem" correspp. to Th. unsolvability of Th.  
[halting prob.]

8)

Applications: a) Bernoulli Seq.

b) Codes using defns.

Δ appr of string

$$\approx f_A + f_B$$

$$\frac{m f_{AB}}{2} \left( \frac{f_A \cdot f_B}{f_{AB}} - 1 \right)^2$$

$m$  = no. of symbols in original seq.

cost of defining

$$\propto \approx A \cdot B$$

"ref. savings"  
in code cost.

Note ~~the~~  $m$  factor —  
so expt. is large, if  $m$  is  
even if  $\left( \frac{f_A \cdot f_B}{f_{AB}} - 1 \right)^2$  is small

This was written as Fortran

Computer program - using a kind of hillclimbing.

c) Grammatical discovery for CF PSL

Assignment of appr to grammar, and

"Goodness of fit" to corpus.

How Gram. discovery  
can be used for  
MT discovery —  
(using special kind of  
PSL).

Hvr., model is still unsatisfactory, tho it seems  
to be a bit useful. Model seems reasonable, but doesn't  
entirely correspond to ordinary CF Grammar. (i.e. corresponds to  
a "unique pars PSL")

7  
2) Artificial learning. Design of machine that could begin problem  
of improving itself.

Wed

Talk: Dec 16, 64 : Marvin's class.

3PM

Bldg 10, Room 275

Discuss. ind. inf. : Show how it is main problem in various art. cut. probs: E.g. ① Learning of any kind, ② Learning char. recogn. ③ Learning to ① play ~~chess~~ chess ② play ~~good~~ chess ④ Learning 2 lang. (what this means - i.e. learning relati. betw. events in R.W. and strings of symbols.)

Disc. of Bayes' Theorem. — how depends on  
Apri. distribn. of all possl. universes <sup>use</sup>

Disc. of various forms of com:

Disc. of th. random Operator method - th. problem of  
"Randomly constructed" ~~times~~ Times (define random in this case)  
Relevance to "random nets".

Applications to stoch. Grammars

Look at some old Notes for this "same" lecture.

New Developments : Work on th. calc. task

Solving problem ② By Slagle.  
① .. myself.

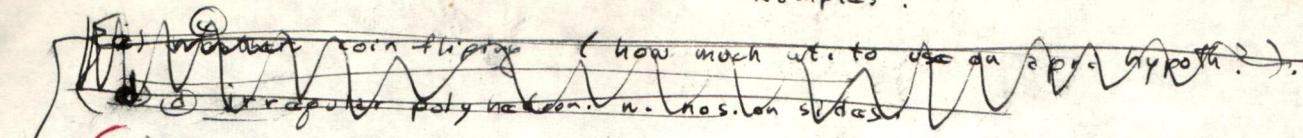


May 11, 66

Gu in Marvin's class May 11, 66 : 4-270  
at MIT.

4 PM

I. What is inductive inf.? examples:



(a) symm loaded dice  
(b) "symm" dice.

$$\begin{aligned} a &= \text{trials w. faces \& up} \\ b &= \text{\# trials} \\ \frac{a}{b} + \frac{x}{b} &= 2 \text{ prf.} \\ \frac{a}{b} + \lambda \frac{b}{b} &= \end{aligned}$$

$\rightarrow$  Sci. Laws [my main introdn. - "Sci. Method" - How to get known hypotheses that fit past data, and are likely to extrapolate well.]

Charles Fort.

Example of hypothesis that fits all data, but doesn't extrapolate well.

$\rightarrow$  first. Curve extrapolation. 10 pts fit w. 10 params? Just how many

params to use? (compromise betw. good fit and few pts.)

Q. of "how many params" is rigorously meaningless.

$$\sigma_{\text{true}}^2 \approx \frac{\sigma_{\text{observed}}^2}{N} = \infty \text{ for } M=N.$$

h) Theorem proving:

- 1) what xfun. to try next. (small set)
- 2) what subgoals to work toward.
- 3) Gen. problem of tree search.

i) Chess, checkers:  $\rightarrow$  takes large tpe. seq. to learn.  
1) best move within (no. constraints)  
2) " " within constraints.

QUESTION 3) Break-down of prob. : Play out, then evaluate.

(A) How to construct - creation of new chars, by combn. of old, wts. to various chars. - open or closed sets.

(B) which move traces to try (parl. search prob.).

J. Patt. recogn.

1) Examples of letters A, B, C. Then new shape: to categorize. analogy to curve fitting. Perceptron: tpe. till 100% correct

Then what is expected future accuracy: we have express. in

Curve fitting, but none for more genl. patt. recogn.

K. Gu. set of as's to find grammar.  $\leftarrow$  examples:  $\{aabb\} \neq \{bbab\}$  mirror lang.

Ref.: L. M.T. i) Gu. bunch of x/tu. pairs  $\rightarrow$  mirror lang.

① to form x/tu. rules

② " " grammar rules.

③ use new source s., to find targets.

$S \rightarrow aSb$   
 $S \rightarrow bSb$   
 $S \rightarrow ab$   
 $S \rightarrow ba$

Hill climb  
gradient  
Ordering  
Completeness

A. th. of Tckas approach: Make gram. to fit old examples

B. Russia's approach: make simplest mach to x/t. known's.

C. Faulk approach via "Distance"

1. Ramon Faulk  
Watson & Ross. Corrl.  
Box 218 Yorkt. Hts. N.Y.

2. Eugene Landenbach.  
Leng. res. Corrl.  
Box 7247, Univ. S.E.  
Austin 12, Texas

My 11, 66

2

D. my approach: Grammatical extropn. - like corrections,  
use of given "generalized lang" - in which are  
~~pairwise~~ pairs of exch. pairs

S

## II Gen. solns.

a) ~~All~~ induction probs are expressable as  
series extropn.

b) Bayes' idea : a prop.

- - -	c b a	a	.01	}
- - -	c b a	b	.02	
- - -	c b a	c	.03	

prob of c =  

$$\frac{.03}{.01 + .02 + .03}.$$

c) Take other strings w. diff info one ~~wishes~~ to  
wishes relevant (use more than necessary).

c) Univ. machines: Turmaching:  
computer w. inf. expandable memory.

Input, output, Universality.

$$M_i(x) = M_v(D_i \Delta x)$$

$\rho_s$                        $\tilde{\alpha} \approx 2^{-N}$

N = shortest dcm.

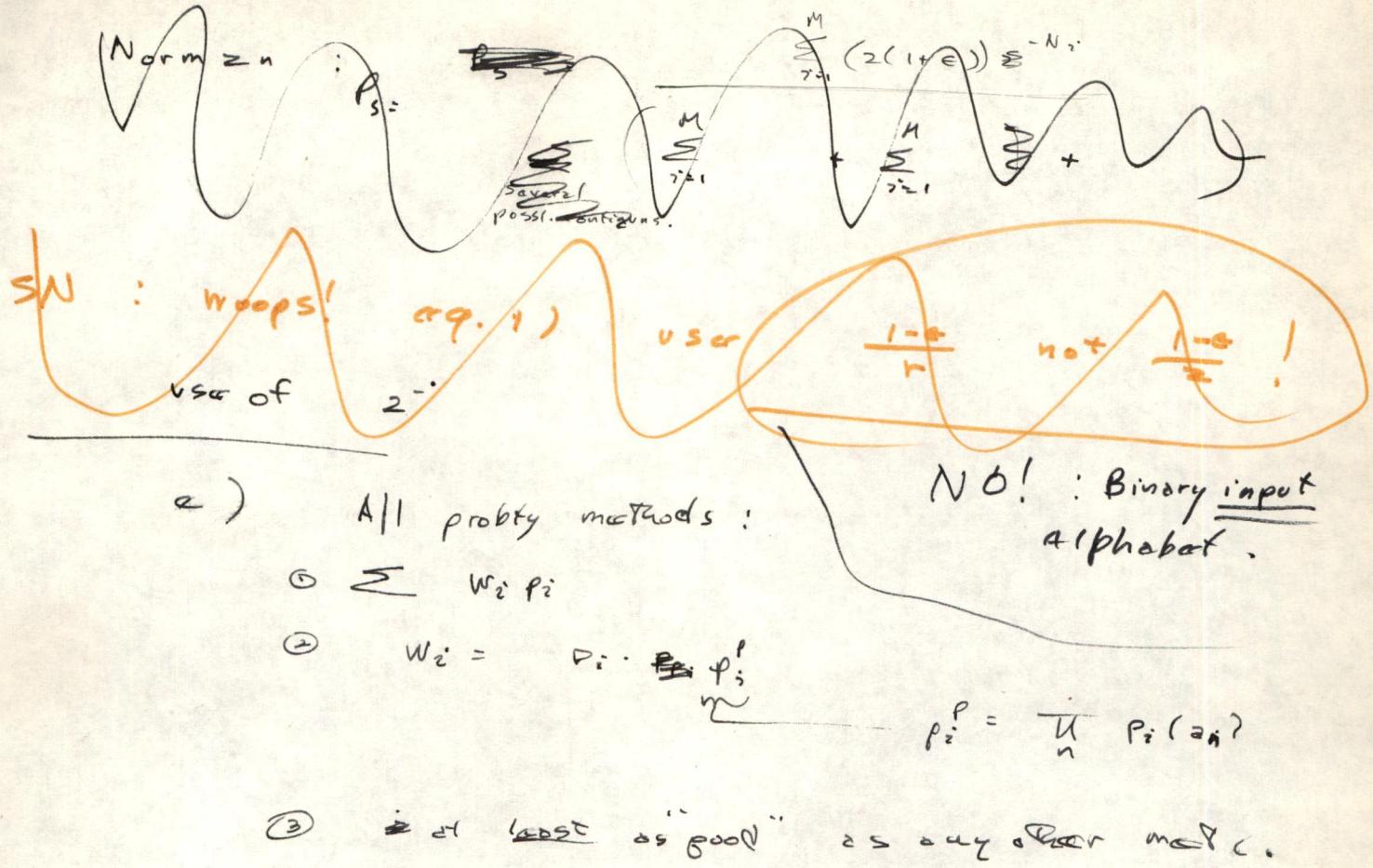
d) ~~exp~~  $\approx \tilde{\alpha} \sum_{i=1}^{\infty} 2^{-N_i}$ .  
 $N_i$  = length of  $i^{\text{th}}$  dcm. of S

$$\alpha \approx \lim_{\epsilon \rightarrow 0} \sum_{i=1}^{\infty} ((1+\epsilon)2)^{-N_i}$$

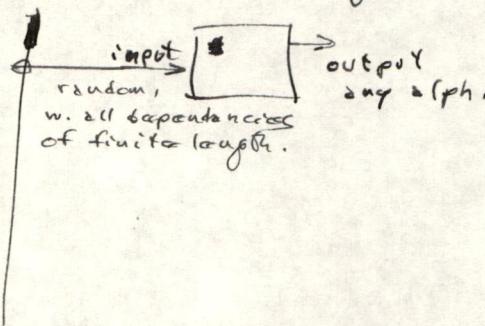
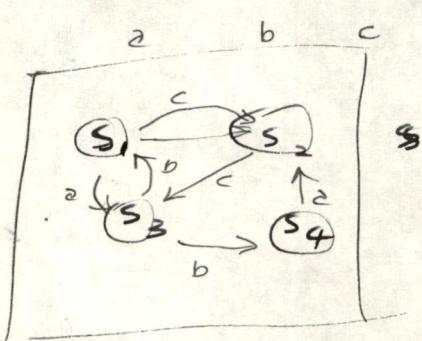
Also take future continuations into account.

My 11, 66

3



f) Model of universe: E.g. finite state "model" of statistical strings,



g) Fixed string method. to get a prior of S.

put in all strings of length 10^6

M strings start w. S.

take out all strings ( $< 10^6$ )  
 $\underline{\quad}$   
 $= N$

$$\text{prob} = \frac{M}{N}$$

h) All + very prob. equiv.

My 11, 68

4

h) Does prob. vary w. nature of Univ. Machine?

SN

Use = probable strings made of universe,  
to see if my model treats it —  
since this model clearly has a diff. "physics"  
than my model.

SN<sub>2</sub>

Perhaps use "all pars" model ~~is~~ to deal  
"indip. of Tormac" problem.

Idea of Universality:

$M_1, M_2$

~~P<sub>i</sub>~~ from  $M_1$ , ~~P<sub>i</sub>~~<sup>2</sup> from  $M_2$ .

"over of ~~subset method~~"

$$2^{N_{T_i} + N} = 2^{N_n} = N$$

I took  $\sim \frac{1}{2}$  hr. for PP 2, 3, 4! Complaint was that I didn't show just how my own work was useful in solving  $\ddagger$ . probs. of Paper 1.

T. utility of & general inf. Theory: Simon, Newell, tried for 4 yrs. to find a service to learn new hours for GPS, by dividing a suitable lang., etc. With Cmii, I think I would know how to go about this much more effectively.